

Al's Electronic Class Room



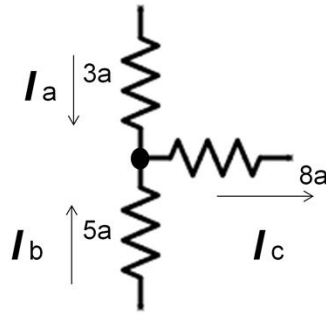
Advance Circuit Analysis

What will be covered

- Kirchhoff's Current Law
- Kirchhoff's Voltage Law
- Method of Branch Currents
- Node-Voltage Analysis
- Method Of Mesh Currents
- Circuit Applications Of Kirchhoff's Law

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Advance Circuit Analysis



Kirchhoff's Current Law

$$I_a + I_b - I_c = 0$$

$$3a + 5a - 8a = 0$$

Or

$$I_a + I_b = I_c$$

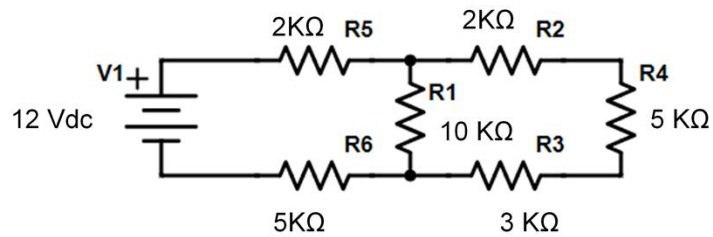
$$3a + 5a = 8a$$

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Kirchhoff's Voltage Law

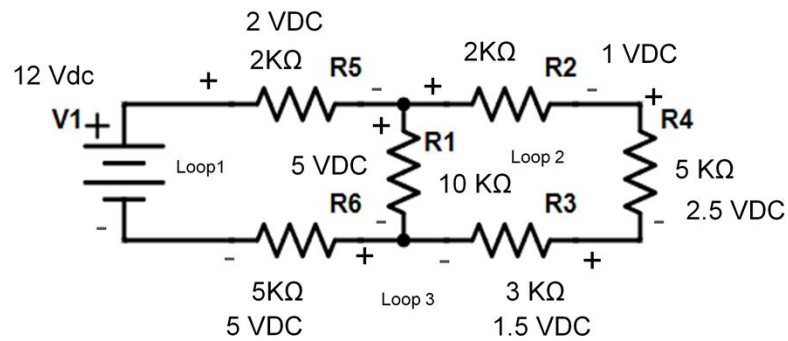
Voltage around a close loop must equal Zero



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Kirchhoff's Voltage Law



$$\text{Loop 1} = 2 \text{ Vdc} + 5 \text{ Vdc} + 5 \text{ Vdc} + (-12 \text{ Vdc}) = 0 \text{ Vdc}$$

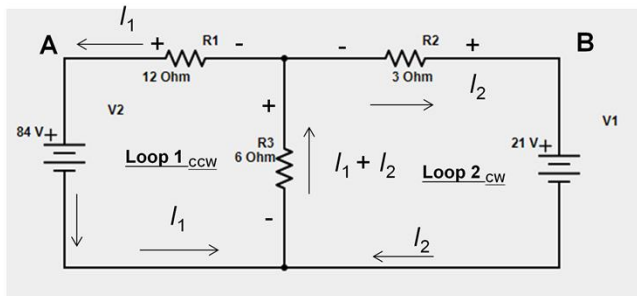
$$\text{Loop 2} = 5 \text{ Vdc} + (-1.5 \text{ Vdc}) + (-2.5 \text{ Vdc}) + (-1 \text{ Vdc}) = 0 \text{ Vdc}$$

$$\text{Loop 3} = -5 \text{ Vdc} + (-1.5 \text{ Vdc}) + (-2.5 \text{ Vdc}) + (-1 \text{ Vdc}) + (-2 \text{ Vdc}) + 12 \text{ Vdc} = 0 \text{ Vdc}$$

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Method of Branch Currents



$$\begin{array}{ll}
 1 \text{ Loop 1 From A} & 2 \quad 84 - R3 (I1 + I2) - R1(I1) = 0 \\
 84 - VR3 - VR1 = 0 & 84 - 6I1 - 6I2 - 12I1 = 0 \\
 \text{Loop 2 From B} & 84 - 18I1 - 6I2 = 0 \\
 21 - VR3 - VR2 = 0 & -18I1 - 6I2 = -84
 \end{array}$$

$$\begin{array}{l}
 3 \\
 21 - R3 (I1 + I2) - R2 (I2) = 0 \\
 21 - 6(I1 + I2) - 3I2 = 0 \\
 21 - 6I1 - 6I2 - 3I2 = 0 \\
 21 - 9I2 - 6I1 = 0 \\
 -6I1 - 9I2 = -21
 \end{array}$$

$$\begin{array}{l}
 4 \\
 3I1 + 1I2 = 14 \quad \div -6 \\
 2I1 + 3I2 = 7 \quad \div -3
 \end{array}$$

$$\begin{array}{l}
 5 \\
 9I1 + 3I2 = 42 \quad \times 3 \\
 2I1 + 3I2 = 7 \quad (\text{Sub})
 \end{array}$$

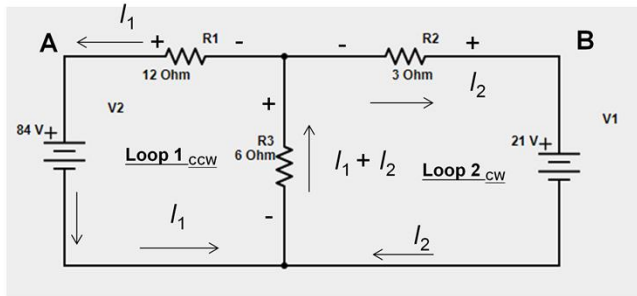
$$\begin{array}{l}
 6 \\
 7I1 = 35 \quad \text{Find } I1 \\
 I1 = 5 \text{ Amps}
 \end{array}$$

$$\begin{array}{l}
 7 \\
 2I1 + 3I2 = 7 \\
 2(5) + 3I2 = 7 \\
 3I2 = 7 - 10 \\
 I2 = -1 \text{ amp}
 \end{array}$$

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Method of Branch Currents



$$I_1 = 5 \text{ Amps}$$

$$I_2 = -1 \text{ amp}$$

$$I_3 = I_1 + I_2 = 5 + (-1) = 4 \text{ amps}$$

$$VR1 = 12 \times 5 = 60 \text{ Vdc}$$

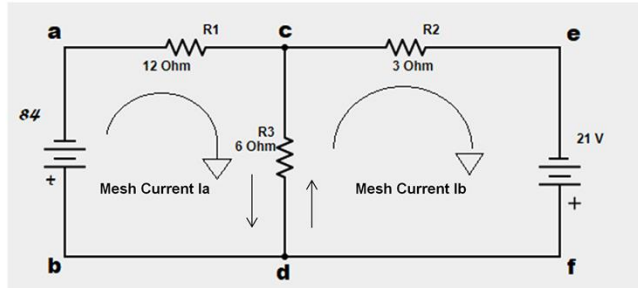
$$VR2 = 3 \times 1 = -3 \text{ Vdc}$$

$$VR3 = 6 \times 4 = 24 \text{ Vdc}$$

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Method Of Mesh Currents



- Mesh Currents are not Branch currents they stay the same.
- Voltages created by its mesh current add, and voltages created by non native Branch current subtracts.

Mesh Current I_a
 $18 I_a - 6 I_b = 84 \text{ V}$

Mesh Current I_b
 $-6 I_a + 9 I_b = -21 \text{ V}$

Mesh Current $I_a \quad \div : 2$
 $18 I_a - 6 I_b = 84 \text{ V}$
 $9 I_a - 3 I_b = 42$

Mesh Current $I_b \quad \div : 3$
 $-6 I_a + 9 I_b = -21 \text{ V}$
 $-2 I_a + 3 I_b = -7 \text{ V}$

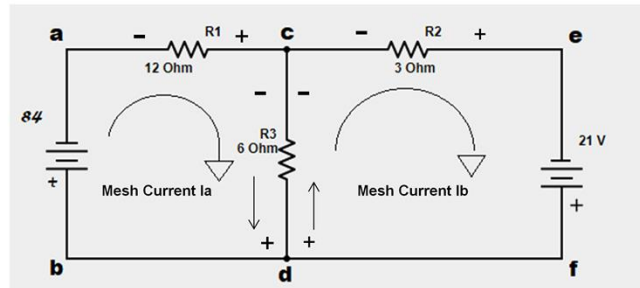
$9 I_a - 3 I_b = 42$
 $-2 I_a + 3 I_b = -7 \text{ V}$
 $7 I_a = 35$
 $I_a = 5 \text{ amps}$

$-2 (5) + 3 I_b = -7 \text{ V}$
 $3 I_b = -7 \text{ V} + 10$
 $3 I_b = 3$
 $I_b = 1 \text{ amp}$

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Method Of Mesh Currents



- Mesh Currents are not Branch currents they stay the same.
- Voltages created by its mesh current add, and voltages created by non native Branch current subtracts.

$$1a = 5 \text{ amps}$$

$$1b = 1 \text{ amp}$$

Mesh 1a

$$(-60 \text{ Vdc}) + (-24 \text{ Vdc}) + 84 = 0$$

$$VR1 = 5 \text{ amps} \times 12 \text{ ohms} = 60 \text{ Vdc}$$

Mesh 1b

$$VR2 = 1 \text{ amp} \times 3 \text{ ohms} = 3 \text{ Vdc}$$

$$VR3 = (5 \text{ amp} \times 6 \text{ ohms}) + (-1 \text{ amp} \times 6 \text{ ohms})$$

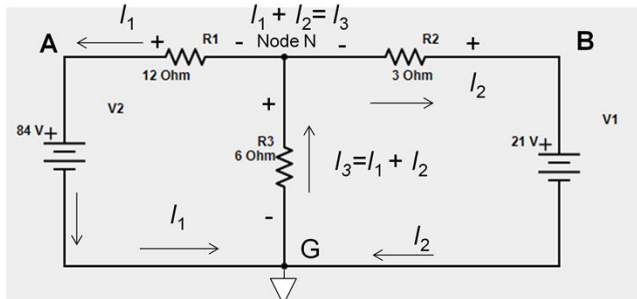
$$(-3 \text{ vdc}) + (-21 \text{ Vdc}) + 24 \text{ Vdc} = 0$$

$$VR3 = 30 \text{ Vdc} - 6 \text{ volts} = 24 \text{ volts}$$

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Node Voltage Analysis



$$I_1 + I_2 = I_3$$

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} = \frac{V_N}{R_3}$$

$$\frac{V_1}{12} + \frac{V_2}{3} = \frac{V_N}{6}$$

$$\frac{84 - V_n}{12} + \frac{21 - V_n}{3} = \frac{V_n}{6}$$

$$84 - V_n + 4(21 - V_n) = 2V_n$$

$$84 - V_n + 84 - 4V_n = 2V_n$$

$$168 - 5V_n = 2V_n$$

$$168 = 7V_n$$

$$168/7 = V_n$$

$$V_n = 24 \text{ Vdc}$$

$$V_1 = 84 - V_n$$

$$V_1 = 84 - 24$$

$$V_n = 60 \text{ Vdc}$$

$$V_2 = 21 - V_n$$

$$V_2 = 21 - 24$$

$$V_2 = -3 \text{ Vdc}$$

$$I_1 = \frac{60 \text{ vdc}}{12 \text{ ohms}} = 5 \text{ Amps}$$

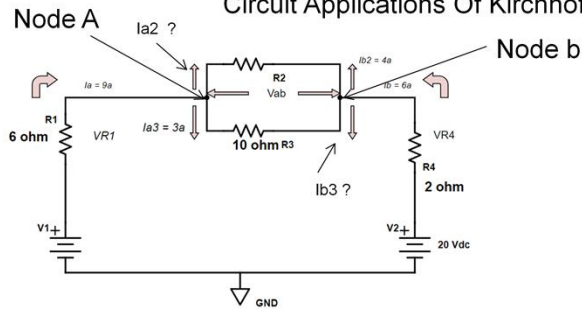
$$I_2 = \frac{-3 \text{ vdc}}{3 \text{ ohms}} = -1 \text{ amp}$$

$$I_3 = 5 \text{ Amp} - 1 \text{ Amp} = 4 \text{ Amp}$$

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Circuit Applications Of Kirchhoff's Law



$$I_{a2} = 9a - 3a ; I_{a2} = 6a$$

$$I_{b3} = 6a - 4a ; I_{b3} = 2a$$

$$V_{ab} = I_{a3} - I_{b3} = 3a - 2a = 1a$$

The Current flow thru R3 is from left to right & the total current flow is 1a (3a from Lft. to Rt. & 2a Rt to Lft)

$$V_{ab} = 1a \times 10 \text{ ohm} = 10 \text{ Volts}$$

$$V_{R2} = 10 \text{ Volts} / (6a - 4a) = 10 \text{ Volts} / 2a = 5 \text{ ohms}$$

$$V_{R1} = 9a \times 6 \text{ ohms} = 54 \text{ Vdc}$$

$$V_{R4} = 6a \times 2 \text{ ohms} = 12 \text{ Vdc}$$

$$V1 = + V_{R1} + V_{ab} - V_{R4} + V2$$

$$-72v = 54V \text{ dc} - 10 \text{ Vdc} + 12V\text{dc} - 20\text{vdc}$$

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