

**Vocabulary**

Word	My own description	Illustration/Example
Arithmetic Sequence		
Common Difference		
Sequence		

**Arithmetic Sequences**

An arithmetic sequence is a \_\_\_\_\_ of numbers where the \_\_\_\_\_ is the same between each number and the next/previous number.

**Choose one of the two options to correctly complete the sentence:**

In other words, to get the next number in an arithmetic sequence, you ( add or subtract / multiply or divide ) by the same number each time. This number is called the \_\_\_\_\_.

To find the *common difference*, just \_\_\_\_\_ one term from the one before it.

Examples:

What is the common difference in the pattern 11, 19, 27, 35, ...?

1) Choose two terms that are next to each other: \_\_\_\_\_ and \_\_\_\_\_

2) Subtract the second term from the one before it:

\_\_\_\_\_ - \_\_\_\_\_ = \_\_\_\_\_ ← common difference

3) Double check that the pattern works for the other numbers (repeat steps 1 and 2 with different sets of two “neighbor” numbers.

\_\_\_\_\_ - \_\_\_\_\_ = \_\_\_\_\_ ← common difference

\_\_\_\_\_ - \_\_\_\_\_ = \_\_\_\_\_ ← common difference

Did you get the same number each time? If so, it’s an arithmetic series and the number you found is the common difference!

---

## Extending Arithmetic Sequences

---

To find out what comes next, \_\_\_\_\_ the common difference to the last term. You can keep doing this as many times as you need to.

Example:

What are the next three terms in the pattern 4, 7, 10, 13, ....?

1) Find the common difference

$$\underline{\hspace{2cm}} - \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{common difference}$$

2) What is the last term? \_\_\_\_\_

3) Add the common difference to the last term:

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{next term (\#1)}$$

4) Do this as many times as you need to (in this example, you need the next **three** terms)

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{next term (\#2)}$$

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{next term (\#3)}$$

---

## Equations for Extending Sequences

---

Common difference \* the term position - first term = term value

Example:

What is the twentieth term in the pattern 3, 7, 11, 15, ...?

1) Find the common difference:

$$\underline{\hspace{2cm}} - \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{common difference}$$

2) What is the term position? **20**

3) What is the first term? \_\_\_\_\_

4) Plug it into the pattern:

$$\underline{\hspace{2cm}} * 20 - \underline{\hspace{2cm}} = \underline{\hspace{2cm}} \leftarrow \text{20th term}$$

---

## Let's Review

---

Before continuing, make sure you understand the main points of this lesson.

- One type of math pattern is an arithmetic sequence.
- In an arithmetic sequence, each term is separated from the previous term by a common difference. For example, even terms are separated by a common difference of two.
- You can extend a pattern by adding the common difference to the last known term.
- You can write equations to describe a pattern. A sequence equation will include multiplying the term number by the common difference, and then adding or subtracting a constant.
- Using a sequence equation, you can find the  $n^{\text{th}}$  term of a pattern.