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# 11.11优惠可以被预测吗?

## 用组合数给你「加鸡腿」

Machine translation for your reference (unverified)

Hello everyone

各位同学大家好

**各位** (gè wèi) everybody; all (guests, colleagues etc); all of you.

I am Teacher Li Yongle

我是李永乐老师

**永乐** (yǒng lè) Yongle Emperor, reign name of third Ming emperor Zhu Di 朱棣 (zhū dì) (1360-1424), reigned 1403-1424, Temple name 明成祖 (míng chéng zǔ).

Double 11 this year comes earlier than previous years

今年的双11来得比往年更早一些

**双11** (shuāng shí yī) see 光棍节 (guāng gùn jié). **来得** (lái de) to emerge (from a comparison); to come out as; to be competent or equal to. **往年** (wǎng nián) in former years; in previous years.

Many students still play stable

很多同学发挥依然稳定

**发挥** (fā huī) to display; to exhibit; to bring out implicit or innate qualities; to express (a thought or moral); to develop (an idea); to elaborate (on a theme). **依然** (yī rán) still; as before. **稳定** (wěn dìng) steady; stable; stability; to stabilize; to pacify.

The final payment is very hot

尾款付得十分火热

**尾款** (wěi kuǎn) balance (money remaining due). **付** (fù) to pay; to hand over to; classifier for pairs or sets of things. **火热** (huǒ rè) fiery; burning; fervent; ardent; passionate.

Facing merchants with various offers

面对商家五花八门的优惠

**面对** (miàn duì) to confront; to face. **商家** (shāng jiā) merchant; business; enterprise. **五花八门** (wǔ huā bā mén) myriad; all kinds of; all sorts of. **优惠** (yōu huì) privilege; favorable (terms); preferential (treatment); discount (price).

Many students studied in advance

很多同学提前研究了起来

Tell me if a kid

有一个小朋友就跟我说

**小朋友** (xiǎo péng yǒu) child.

He found a chicken drumstick activity for China Merchants Bank credit card	他发现了一个 <b>招商</b> 银行信用卡的 <b>加鸡腿</b> 活动	<b>招商</b> (zhāo shāng) to seek investment or funding; investment promotion. <b>鸡腿</b> (jī tuǐ) chicken leg; drumstick.
This event is quite interesting	这个活动还挺有意思的	
As long as you bind the China Merchants Bank credit card	就是只要你 <b>绑定</b> 了招商银行信用卡	<b>绑定</b> (bǎng dìng) binding (loanword); to bind (e.g. an account to a mobile phone number).
Whether using WeChat or Alipay	无论是用微信 <b>支付宝</b>	<b>支付宝</b> (zhī fù bǎo) Alipay, online payment platform.
Whether it's shopping or dining out	无论是购物还是 <b>出行用餐</b>	<b>出行</b> (chū xíng) to set out on a long journey; to travel afar. <b>用餐</b> (yòng cān) to eat a meal.
(Single Pen) You can draw red envelopes and chicken legs if you brush over 18 yuan	(单笔) <b>刷</b> 满18元就能抽 <b>红包</b> 加鸡腿	<b>刷</b> (shuā) to brush; to paint; to daub; to paste up; to skip class (of students); to fire from a job. <b>红包</b> (hóng bāo) money wrapped in red as a gift; bonus payment; kickback; bribe.
You can draw up to 100 times	<b>最多</b> 可以抽100次	<b>最多</b> (zuì duō) at most; maximum; greatest (amount); maximal.
And there is a super prize of 11111 yuan	而且还有 <b>超级大奖</b> 11111元	<b>超级</b> (chāo jí) super-; ultra-; hyper-. <b>大奖</b> (dà jiǎng) prize; award.
This kid told me he didn't expect the super prize	<b>这位</b> 小朋友就跟我说 <b>超级大奖</b> 他 <b>也不指望</b> 了	<b>这位</b> (zhè wèi) this (person). <b>指望</b> (zhǐ wàng) to hope for sth; to count on; hope.
Just want to ask under normal circumstances	就想问正常情况下	
How big is the chicken drumstick?	<b>最大有可能</b> 会抽到 <b>多大</b> 的鸡腿呢	<b>有可能</b> (yǒu kě néng) possible; probable; possibly; probably; may; might. <b>多大</b> (duō dà) how big; how much; how old etc.
In order to study this problem	为了研究这个问题	
I did a test two days ago	前两天我还做了个 <b>测试</b>	<b>测试</b> (cè shì) to test (machinery etc); to test (students); test; quiz; exam; beta (software).
I got 0.8 yuan, 1 yuan and 2 yuan chicken drumsticks.	<b>分别</b> 抽到了0.8元 1元和2元的鸡腿	<b>分别</b> (fēn bié) to part or leave each other; to distinguish; difference; in different ways; differently; separately or individually.
Can we use these chicken drumsticks	我们能不能根据我抽到的这些鸡腿	
To estimate the maximum value of chicken legs	来估计鸡腿的最大值有多少呢	
The derivation of this problem is a bit complicated in mathematics	这个问题的 <b>推导</b> 在数学上 <b>有一点</b> 复杂	<b>推导</b> (tuī dǎo) derivation; to deduce. <b>有一点</b> (yǒu yī diǎn) a little; somewhat.

But the conclusion is very simple

但是**结论**非常简单

**结论 (jié lùn)** conclusion; verdict; to conclude; to reach a verdict.

After mastering this method

**掌握**了这种方法之后

**掌握 (zhǎng wò)** to grasp (often fig.); to control; to seize (initiative, opportunity, destiny); to master; to know well; to understand sth well and know how to use it; fluency.

Everyone can use this method to estimate the size of chicken legs

每一个人都可以用这种方法来估计鸡腿的**大小**

**大小 (dà xiǎo)** dimension; magnitude; size; measurement; large and small; at any rate; adults and children; consideration of seniority.

Let's first talk about the historical source of this problem

我们首先来说一下这个问题的**历史来源**

**来源 (lái yuán)** source (of information etc); origin.

We call this problem the German tank problem

这个问题我们叫它**德国坦克问题**

**德国 (dé guó)** Germany; German. **坦克 (tǎn kè)** tank (military vehicle) (loanword).

German tank problem

德国**坦克问题**

This question is an example of real application in history

这个问题是在**历史上真实应用过**的一个**例子**

**历史上 (lì shǐ shàng)** historical; in history. **真实 (zhēn shí)** true; real. **应用 (yìng yòng)** to use; to apply; application; applicable. **例子 (lì zǐ)** case; (for) instance; example.

When talking about World War II

说**二战**的时候

**二战 (èr zhàn)** World War II.

The Allies need to estimate how many tanks Germany can produce each month

**盟军**要估计德国每个月可以**产**多少辆**坦克**

**盟军 (méng jūn)** allied forces. **产 (chǎn)** to give birth; to reproduce; to produce; product; resource; estate; property.

Because at that time the tank was the overlord of the land, right?

因为那个时候坦克是**陆上霸主**对吧

**陆上 (lù shàng)** land-based; on land. **霸主 (bà zhǔ)** a powerful chief of the princes of the Spring and Autumn Period (770-476 BC); overlord; hegemon.

You can't beat you with more tanks

你坦克多**打不过**你

**打不过 (dǎ bu guò)** unable to defeat; to be no match for sb.

That has to be estimated. How to estimate

那得估计 怎么估计呢

It has two methods

它有两种方法

The first method is intelligence

第一种方法就是**情报**

**情报 (qíng bào)** information; intelligence.

He can send a lot of intelligence personnel

他可以**派**很多的情报**人员**

**派 (pài)** clique; school; group; faction; to dispatch; to send; to assign; to appoint; pi (Greek letter Ππ); the circular ratio pi = 3.1415926; (loanword) pie. **人员 (rén yuán)** staff; crew; personnel.

What British MI6	什么 <b>英国</b> 的 <b>军情六处</b>	<b>英国</b> (yīng guó) United Kingdom 联合王国 (lián hé wáng guó); United Kingdom of Great Britain and Northern Ireland; abbr. for England <b>英格兰</b> (yīng gé lán). <b>军情六处</b> (jūn qíng liù chù) MI6 (British military intelligence agency).
American CIA penetrated into German occupation area to study	美国的CIA <b>渗透</b> 到德国的 <b>占领区</b> 去研究	<b>渗透</b> (shèn tòu) to permeate; to infiltrate; to pervade; osmosis. <b>占领</b> (zhàn lǐng) to occupy (a territory); to hold.
The intelligence department was placed inside the arsenal to see	<b>情报部门</b> <b>安插</b> 到 <b>兵工厂</b> 里面去看	<b>部门</b> (bù mén) department; branch; section; division. <b>安插</b> (ān chā) to place in a certain position; to assign to a job; to plant; resettlement (old). <b>兵工厂</b> (bīng gōng chǎng) munitions factory.
How many tanks are left in each month	每个月 <b>剩下</b> 多少辆坦克	<b>剩下</b> (shèng xià) to remain; left over.
But except for the intelligence department	但除了 <b>情报部门</b> <b>以外</b>	<b>以外</b> (yǐ wài) apart from; other than; except for; external; outside of; on the other side of; beyond.
There is another solution	还有一种 <b>方案</b>	<b>方案</b> (fāng àn) plan; program (for action etc); proposal; proposed bill.
That is relying on mathematicians	那就是 <b>依靠</b> <b>数学家</b>	<b>依靠</b> (yī kào) to rely on sth (for support etc); to depend on. <b>数学家</b> (shù xué jiā) mathematician.
In the course of combat	在 <b>作战</b> 的过程中	<b>作战</b> (zuò zhàn) combat; to fight.
The Allies will capture some German tanks	盟军会 <b>俘获</b> 一些 <b>德军</b> 的坦克	<b>俘获</b> (fú huò) to capture (enemy property or personnel); capture (physics: absorption of subatomic particle by an atom or nucleus). <b>德</b> (dé) virtue; goodness; morality; ethics; kindness; favor; character; kind. <b>军</b> (jūn) army; military; arms.
Or destroy some German tanks	或者 <b>摧毁</b> 一些 <b>德军</b> 坦克	<b>摧毁</b> (cuī huǐ) to destroy; to wreck.
And these tanks are numbered	而这些坦克它是有 <b>编号</b> 的	<b>编号</b> (biān hào) to number; numbering; serial number.
Some are numbers on the chassis	有一些是 <b>底盘</b> 上的 <b>编号</b>	<b>有一些</b> (yǒu yī xiē) somewhat; rather; some. <b>底盘</b> (dǐ pán) chassis.
Gearbox number	<b>变速箱</b> 的 <b>编号</b>	<b>变速箱</b> (biàn sù xiāng) gearbox; transmission.
What number on the track	什么 <b>履带</b> 上的 <b>编号</b>	<b>履带</b> (lǚ dài) caterpillar track (propulsion system used on bulldozers etc); (literary) shoes and belt.
We consider these numbers to be continuous	这些 <b>编号</b> 我们认为它是 <b>连续</b> 的	<b>连续</b> (lián xù) continuous; in a row; serial; consecutive.
1 2 3 4 up to the maximum	1 2 3 4 一直到 <b>最大</b> 值	
Then you pass the numbers of the captured tanks	那么你通过 <b>俘获</b> 的这些坦克的 <b>编号</b>	

Can it be estimated	能不能估计出来	
What is the maximum number of this tank?	说这个坦克的最大编号是多少呢	
Mathematicians also have methods to estimate	数学家们也有方法去估计	
And the estimated results of these two methods are very different	而且这两种方法估计的结果 <b>差别</b> 很大	<b>差别 (chā bié)</b> difference; distinction; disparity.
Intelligence agency estimates	情报部门估计	
How many tanks are produced in Germany on average every month?	德国每个月 <b>平均来讲</b> 有多少辆坦克 <b>生产</b> 呢	<b>平均 (píng jūn)</b> average; on average; evenly; in equal proportions. <b>来讲 (lái jiǎng)</b> as to; considering; for. <b>生产 (shēng chǎn)</b> to produce; to manufacture; to give birth to a child.
About 1400	大约有1400辆	
This is estimated by the intelligence department	这是情报部门估计的	
And how many mathematicians estimate there are	而数学家们估计有多少辆呢	
Estimated to be 246	估计有246辆	
Very big difference	差别非常大	
Is from 1940 to 1942	是从1940年到1942年这一段时间 <b>里边</b>	<b>里边 (lǐ bian)</b> inside.
It is estimated that an average of 246 vehicles per month	估计平均每个月是246辆	
Finally decrypted after the war	最后 <b>战后</b> 终于 <b>解密</b> 了	<b>战后 (zhàn hòu)</b> after the war; postwar. <b>解密 (jiě mì)</b> to declassify; (computing) to decrypt; to decipher.
What is the actual situation?	那实际的情况又是 <b>如何</b> 呢	<b>如何 (rú hé)</b> how; what way; what.
During this time, 245 German production tanks per month	在这段时间内德国生产坦克每个月245辆	
So you will find the results estimated by mathematicians	所以你会发现数学家们用数学估计出来的结果	
More useful than the top spy, right?	比最 <b>顶尖</b> 的 <b>间谍</b> 还要 <b>有用</b> 对吧	<b>顶尖 (dǐng jiān)</b> peak; apex; world best; number one; finest (competitors); top (figures in a certain field). <b>间谍 (jiàn dié)</b> spy. <b>有用 (yǒu yòng)</b> useful.
How do mathematicians do this	那数学家们是怎么 <b>做到</b> 这一点呢	<b>做到 (zuò dào)</b> to accomplish; to achieve.

How can I pass the captured tanks	怎么能够通过俘获的几辆坦克	
You can estimate the total number of tanks	就可以估计出 <b>总共</b> 的坦克数量呢	<b>总共 (zǒng gòng)</b> altogether; in sum; in all; in total.
This is the question we are going to study today	这就是我们今天要研究的问题	
So to study this	那么为了研究这件事	
We must first understand a little bit of mathematics	我们首先还得去了解一点数学知识	
This is when we were in high school	这就是我们在 <b>上高中</b> 的时候	<b>上高 (shàng gāo)</b> Shanggao county in Yichun 宜春, Jiangxi.
A mathematical knowledge learned is called combinatorial number	学过的一个数学知识 <b>叫做组合数</b>	<b>叫做 (jiào zuò)</b> to be called; to be known as. <b>组合 (zǔ hé)</b> to assemble; to combine; to compose; combination; association; set; compilation; (math.) combinatorial.
Then we have to review this number of combinations first	那我们要先把这个组合数再复习一下	
What is the number of combinations?	什么叫组合数呢	
There are n elements	就是有 <b>n个元素</b>	<b>元素 (yuán sù)</b> element; element of a set; chemical element.
Has n elements	有 <b>n个元素</b>	
We take out m of them	我们 <b>取出</b> 其中的 <b>m个</b>	<b>取出 (qǔ chū)</b> to take out; to extract; to draw out.
How many methods does it have	它有多少种方法	
We call this method $c(n,m)$	这个方法数我们就叫它 $c(n,m)$	
This is called the number of combinations	<b>这就叫组合数</b>	<b>这就 (zhè jiù)</b> immediately; at once.
So how to calculate the number of combinations	那么组合数怎么 <b>计算</b> 呢	<b>计算 (jì suàn)</b> to count; to calculate; to compute.
Let's give an example	我们举个例子	
For example, we have 1 2 3 4 5	比如说我们有1 2 3 4 5	
These 5 people	这 <b>5个人</b>	<b>个人 (gè rén)</b> individual; personal; oneself.
1 2 3 4 Let's talk about 4 people first	1 2 3 4吧 先说4个人	

We want to find 2 of these 4 people to participate in the singing competition

这4个人中我们想找2个人参加歌唱比赛去

歌唱 (gē chàng) to sing.

How many ways do we have?

我们有多少种方法 对吧

Then this is called  $c(4,2)$

那这就叫 $c(4,2)$

Choose 2 of these 4 people

在这4个人中选2个

中选 (zhòng xuǎn) to win an election; to get a position by passing the imperial exam.

Then you can choose 1,2 1,3 1,4 2,3 2,4 3,4

那你可以选1,2 1,3 1,4 2,3 2,4 3,4

Is there a total of 6 methods?

是不是一共6种方法 对吧

So  $c(4,2)$  is 6

所以 $c(4,2)$ 就是6

This is called  $m$  elements out of  $n$  elements

这就叫 $n$ 个元素中取 $m$ 个元素

Give another example

再举个例子

For example, there are 5 people

比如说有5个人

We choose 3 people to participate in the composition contest

我们选3个人参加作文比赛

作文 (zuò wén) to write an essay; composition (student essay).

How many ways

有多少种方法

You are  $c(5,3)$

你这就是 $c(5,3)$

For  $c(5,3)$ , you can think

$c(5,3)$ 的话你可以想

You choose 3 people to participate in the competition

你选3个人参加比赛

Then he won't go with these two people, right?

那剩下这2个人他就不去 对不对

对不对 (duì bù duì) right or wrong?; Is it right?; OK, yes? (colloquial).

So how many ways are there for 2 people left

所以有多少种剩下2个人的方法

There are so many ways to select 3 people, right?

就有多少种选出3个人的方法 对不对

选出 (xuǎn chū) to pick out; to select; to elect.

So we just choose two

那所以我们干脆就选两个

干脆 (gān cuì) straightforward; clear-cut; blunt (e.g. statement); you might as well; simply.

Ok choose two leftovers

好的 选两个剩的

The remaining two people can be 1,2 1,3 1,4 1,5

剩这两个人可以是1,2 1,3 1,4 1,5

2,3 2,4 2,5 3,4 3,5 4,5

2,3 2,4 2,5 3,4 3,5 4,5

So there are 10 ways to leave two people

所以剩下两个人的方法有10种

There are also 10 ways to select 3 people

选出3个人的方法也有10种

$c(5,3)$  is equal to 10

$c(5,3)$  等于10

等于 (děng yú) to equal; to be tantamount to.

This is the so-called number of combinations

这就是所谓的组合数

所谓 (suǒ wèi) so-called; what is called.

It's not difficult to understand

其实并不难理解

The number of combinations has some properties

组合数有一些性质

性质 (xìng zhì) nature; characteristic.

Let's give an example

我们举个例子

What is the property of the first combination number  $c(n,0)$  equal to

第一个组合数的性质 $c(n,0)$ 等于多少

There are several ways to choose 0 people from n people

从n个人中选0个人有几种方法

That's not just one kind, no one chooses, right

那不就是一种 谁也不选 对不对

How many ways are  $c(n,n)$

$c(n,n)$ 有多少种方法

Choose n from n people

从n个人选n个

There is also a way, just select all

那不是也有一种方法 就全选

So both numbers are 1.

所以这两个数都是1

个数 (gè shù) number of items or individuals.

This is the first property

这是第一个性质

个性 (gè xìng) individuality; personality.

The second is the specific calculation

第二个就是具体计算

具体 (jù tǐ) concrete; definite; specific.

What is  $c(n,m)$  equal to

$c(n,m)$ 等于什么

It is equal to  $n \times (n-1) \times (n-2)$  multiplied until  $n-m+1$

它等于 $n \times (n-1) \times (n-2)$  一直乘到  $n-m+1$

That is to multiply the number of m, right?

也就是乘m个数 是吧

也就是 (yě jiù shì) that is; i.e..

Start from n and multiply it by m

从n开始往小了乘 乘m个数

Then the bottom is  $1 \times 2 \times 3 \times$

然后底下是 $1 \times 2 \times 3 \times$  一直乘 也是乘m个数

底下 (dǐ xia) the location below sth; afterwards.

for example

举个例子



c(4,2) is what	c(4,2)就等于什么	
Equal to $(4 \times 3) / (1 \times 2)$	等于 $(4 \times 3) / (1 \times 2)$	
The final count is 6	最后算完得6	
What is c(5,3) equal to	c(5,3)等于什么	
Equal to $(5 \times 4 \times 3) / (1 \times 2 \times 3)$ equal to 10, right?	等于 $(5 \times 4 \times 3) / (1 \times 2 \times 3)$ 等于 10 是吧	
This is an algorithm for the number of combinations	这就是组合数的一个 <b>算法</b>	<b>算法 (suàn fǎ)</b> arithmetic; algorithm; method of calculation.
What algorithm is there?	还有什么算法呢	
For example, n times $c(n-1, m-1)$	比如说n倍的 $c(n-1, m-1)$	
It is equal to m times $c(n, m)$	它等于m倍的 $c(n, m)$	
This is also a formula	这也是它的一个 <b>公式</b>	<b>公式 (gōng shì)</b> formula.
If you don't believe me, just try these numbers in the next generation, right?	你不信你就把这些数往里代试 试 是吧	
We can prove it after the generation is over, we won't prove it	代 <b>完了</b> 之后就能证出来 <b>咱</b> 就不证 了	<b>完了 (wán le)</b> to be finished; to be done for; ruined; gone to the dogs; oh no. <b>咱 (zán)</b> I or me; we (including both the speaker and the person spoken to).
What else	还有什么呢	
And this is called $c(n-1, m-1) + c(n-1, m) = c(n, m)$	还有这叫做 $c(n-1, m-1) + c(n-1, m) = c(n, m)$	
Let's talk a little bit about this formula	这公式咱们可以稍微 <b>说道</b> 说道	<b>说道 (shuō dào)</b> to state; to say (the quoted words).
Why is this	这是 <b>为啥</b>	<b>为啥 (wèi shá)</b> dialectal equivalent of 为什么 (wèi shén me).
What do you mean	<b>啥</b> 意思呢	<b>啥 (shá)</b> dialectal equivalent of 什么 (shén me); also pr. (shà).
That means you have many elements, you have n elements	<b>就是说</b> 你有 <b>好多</b> 个元素 <b>嘛</b> 你有n 个元素	<b>就是说 (jiù shì shuō)</b> in other words; that is. <b>好多 (hǎo duō)</b> many; quite a lot; much better. <b>嘛 (ma)</b> modal particle indicating that sth is obvious; particle indicating a pause for emphasis.
You have n elements	你有n个元素	
I said you get me m	我说你给我取m个	

Then I will ask you first, do you include this number one

那我先问你 你**包含**不包含这个**一**号

**包含 (bāo hán)** to contain; to embody; to include. **一号 (yī hào)** first day of the month; toilet; (slang) top (in a homosexual relationship).

$c(n,m)$  is  $m$  out of  $n$  elements, right?

$c(n,m)$ 就是 $n$ 个元素中取 $m$ 个**对**吧

If you don't include this number one

如果你**不**包含这个**一**号

You just take  $m$  from  $n-1$  elements

你就是从 $n-1$ 元素中取 $m$ 个

The number of methods is  $c(n-1,m)$

那方法数就是 $c(n-1,m)$

If you include this number one

如果你**包含**这个**一**号

What's the result

那有什么**结果**

If you include number one

你**包含**一号的话

You only need to take  $m-1$  from the remaining  $n-1$ .

你只需要在剩下的 $n-1$ 中取 $m-1$ 就行了

Because there is one you have included

因为有一个你已经**包含**了

So this method number is  $c(n-1,m-1)$

所以这个方法数就是 $c(n-1,m-1)$

Can you understand?

大家能听明白吗

Is actually asking you

就是**实际上**就是问你

**实际上 (shí jì shàng)** in fact; in reality; as a matter of fact; in practice.

When taking  $m$  elements from  $n$  elements

从 $n$ 个元素中取 $m$ 个元素的时候

You can divide into two situations

你可以分两种**情况**

One situation is to include it, one situation is to not include it

一种**情况**就是**包含**它 一种**情况**是**不**包含它

If it is included, it is the number of the previous method

如果**包含**它就是前面这个方法数

Do not include it, just the following method number

**不**包含它就后面这个方法数

The two of them add up to this number, right?

它俩一加就是这个数 是**吧**

Alright, let's stop here	好了 性质咱们就说到这	<b>说到</b> (shuō dào) to talk about; to mention; (preposition) as for.
Let's make a question below	下面咱做个题	
Say we talk about science and still do questions	说咱们讲 <b>科普</b> 还做题	<b>科普</b> (kē pǔ) popular science; popularization of science; abbr. of 科学普及.
Because of it	就是因为吧	
Our next question is related to this topic	我们 <b>后面</b> 的这个问题它跟这个 <b>题目</b> 有关	<b>面的</b> (miàn di) abbr. of 面包车的士 (miàn bāo chē dì shì); minivan taxi. <b>题目</b> (tí mù) subject; title; topic. <b>有关</b> (yǒu guān) to have sth to do with; to relate to; related to; to concern; concerning.
So let's do this question	所以咱们把这个题做一下	
Say there is such a formula called $c(k,k)+c(k+1,k)+c(k+2,k)$	说有这么一个 <b>式子</b> 叫 $c(k,k)+c(k+1,k)+c(k+2,k)$	<b>式子</b> (shì zi) formula; mathematical expression.
Keep adding, adding, adding, adding to $c(N,k)$	一直加 加加加 一直加 加到 $c(N,k)$	
Ask you what is after simplification	问你这个东西化简之后是啥	
This is a college entrance examination question many, many years ago	这个是很多很多 <b>年前</b> 的一个高考题	<b>年前</b> (nián qián) before the end of the year; before the new year.
I've talked about this problem before when I talked about math	我以前讲数学的时候还讲过这道题	
Actually this question is not difficult	其实这道题并不难	
Let's take a closer look	咱们仔细看	
$c(k,k)$ is to take $k$ elements out of $k$ elements. Several methods	$c(k,k)$ 就是 $k$ 个元素中取 $k$ 个 几种方法	
Kind right	一种 对吧	
Then $c(k,k)$ can I write it as	那么 $c(k,k)$ 我是不是可以把它写成是	
$c(k+1,k+1)$ right	$c(k+1,k+1)$ 对不对	
Because $c(k+1,k+1)$ and $c(k,k)$ are both 1.	因为 $c(k+1,k+1)$ 和 $c(k,k)$ 都是1	

Then add the second term  
 $c(k+1,k)$

然后再加上第二项 $c(k+1,k)$

加上 (jiā shàng) plus; to put in; to add; to add on; to add into; in addition; on top of that. 项 (xiàng) back of neck; item; thing; term (in a mathematical formula); sum (of money); classifier for principles, items, clauses, tasks, research projects etc.

Add the third item  $c(k+2,k)$   
and keep adding

再加第三项 $c(k+2,k)$  一直再加

三项 (sān xiàng) three items; three events; three terms; tri-; trinomial, ternary (math.); triathlon (abbr. for 三项全能).

The last item added is  $c(N,k)$

加到最后一项是 $c(N,k)$

Then we put the first two  
together

然后咱们把前两项合起来

Everyone, look at the first two  
items, the number  $n$  is the  
same.

大家看 前两项它底下这个数 $n$ 是一样

And the above number  $m$  is a  
difference of 1.

而上面这个数 $m$ 它是差1的

上面 (shàng miàn) on top of; above-mentioned; also pr. (shàng mian).

Does it exactly satisfy this  
formula

是不是正好满足这个公式

满足 (mǎn zú) to satisfy; to meet (the needs of); satisfied; content.

$n$  is the same

$n$ 是一样的

$m$  is a difference

$m$ 是差一个数的

The final result is that we have  
to add one bit to this  $n$

最后的结果是我们要把这个 $n$ 加上一位

And  $m$  we take the larger one,  
right

而 $m$ 我们取大的那个 是吧

We can use the above formula

我们可以利用上面这个公式

利用 (lì yòng) to exploit; to make use of; to use; to take advantage of; to utilize.

So this thing can be deformed  
again

所以这个东西又可以变形

变形 (biàn xíng) deformation; to become deformed; to change shape; to morph.

It becomes  $c(k+2,k+1)$

它就变成了 $c(k+2,k+1)$

变成 (biàn chéng) to change into; to turn into; to become.

That's why this bracket  
becomes the bottom one

就是这个括号变成底下这个了

括号 (kuò hào) parentheses; brackets.

And then continue to remain  
unchanged

然后后面继续保持不变

保持 (bǎo chí) to keep; to maintain; to hold; to preserve. 不变 (bù biàn) constant; unvarying; (math.) invariant.

Add  $c(k+2,k)$

加 $c(k+2,k)$

Then keep adding to the last  
 $c(N,k)$

然后一直加 加到最后的 $c(N,k)$

Then you see if you can put these two together again

然后你看是不是又可以把这两个合起来了

Put these two together

把这两个合起来

Let's use this formula again

我们再次利用这个公式 这么一顿折腾

再次 (zài cì) one more time; again; one more; once again. 折腾 (zhē teng) to toss from side to side (e.g. sleeplessly); to repeat sth over and over again; to torment sb; to play crazy; to squander (time, money).

Can you see how many in the end

最后你能看到是多少吗

It is equal to  $c(N+1, k+1)$

它等于  $c(N+1, k+1)$

Got such a result, okay

就得出了这么一个结果 好吧

得出 (dé chū) to obtain (results); to arrive at (a conclusion).

Maybe some classmates said I didn't understand this

也许有同学说这块我没看懂

看懂 (kàn dǒng) to understand what one is reading or watching.

But it doesn't matter

不过没有关系

没有关系 (méi yǒu guān xi) see 没关系 (méi guān xi).

Anyway, you know to put this big bunch

反正你就知道把这一大串

反正 (fǎn zhèng) anyway; in any case; to come over from the enemy's side. 串 (chuàn) to string together; to skewer; to connect wrongly; to gang up; to rove; string; bunch; skewer; classifier for things that are strung together, or in a bunch, or in a row: string of, bunch of, series of; to make a swift or abrupt linear movement (like a bead on an abacus); to move across.

It can be simplified to the following formula, which is OK

它可以化简成底下这个式子就Ok了

We can go down

我们就可以往下算了

算了 (suàn le) let it be; let it pass; forget about it.

OK, let's use this number of combinations to study

好 我们就利用这个组合数来研究一下

After we captured some tanks

我们俘获了一些坦克之后

How do we use samples to estimate

如何我们用样本来怎么样 来估计

To estimate the population

来估计总体

总体 (zǒng tǐ) completely; totally; total; entire; overall; population (statistics).

Estimate the population with a sample

用样本估计总体

样本 (yàng běn) sample; specimen.

You have to ask what is the distribution of this population first

你得先问问这个总体是什么样的分布

什么样 (shén me yàng) what kind?; what sort?; what appearance?. 分布 (fēn bù) to scatter; to distribute; to be distributed (over an area etc); (statistical, geographic) distribution.

And our problem, we should say it is evenly distributed

而我们这个问题 我们应该说是**均匀分布**

**均匀 (jūn yún)** even; well-distributed; homogeneous; well-proportioned (figure, body etc).

We think the tank number is 1 2 3 4 all the way to N

我们认为坦克的编号是1 2 3 4 一直到N

There is only one for each number, right

每一个编号只有一辆 对吧

When I go to capture German tanks

我再去俘获德国坦克的时候

I also captured randomly

我也是**随机**俘获的

**随机 (suí jī)** according to the situation; pragmatic; random.

So I just wanted to ask

所以我就想问问

If this tank is numbered 1 2...

如果这个坦克它的编号分别是1 2 ...

How much does it go until the N number

一直到多少呢 一直到N号

Then I, the allied army, I captured a few vehicles casually, right?

然后我这个盟军我随便俘获了几辆 对不对

Allied forces captured k vehicles

盟军我们俘获了k辆

There are N German tanks

德国坦克一共有N辆

I captured k vehicles

我俘获了k辆

Obviously this k is smaller than N, right?

很**显然**这个k是比N**小的** 是不是

**显然 (xiǎn rán)** clear; evident; obvious(ly). **小的 (xiǎo de)** I (when talking to a superior).

Then its largest number

那么它的最大编号

What is the largest possible number M

最大编号M可能是多少

What is the largest possible number M

最大编号M可能是多少

Let's first study the probability

我们首先来研究一下**概率**

**概率 (gài lǜ)** probability (math.).

What probability? Let's think about it

什么概率呢 我们**思考**一下

**思考 (sī kǎo)** to reflect on; to ponder over.

You captured k cars

就是你俘获了k辆汽车

The largest number in these k cars is the probability of M, right?

这k辆汽车里边最大编号是M这个**概率** 是吧

For example, you captured 10 cars, the maximum number is 50

你比如你俘获了10辆车 最大编号是50

What is the probability of this? This is called  $P_M$

请问这概率有多大 这叫 $P_M$

What is it

等于什么呢

Let's think about this  $P_M$  means the  $k$  cars you captured

咱们思考这个 $P_M$ 表示你俘获的 $k$ 辆

And the biggest change is  $M$

而且最大变化是 $M$ 的

How many ways do you capture  $k$  vehicles?

那你俘获 $k$ 辆的方法数一共有多少种呢

There are  $N$  German tanks

德国坦克一共有 $N$ 辆

I captured  $k$  of these  $N$  tanks

这 $N$ 辆坦克中我俘获 $k$ 辆

Is it just  $c(N,k)$  so many kinds

是不是就是 $c(N,k)$ 这么多**多种**

**多种 (duō zhǒng)** many kinds of; multiple; diverse; multi-.

So in so many situations

那么在这么多种情况下

In how many cases are the largest number captured by  $M$ ?

有多少种情况俘获的最大编号是 $M$ 呢

For example, this tank

比如说这辆坦克

This tank is the tank numbered  $M$

这辆坦克就是编号为 $M$ 的坦克

It is the largest number we captured

它就是我们俘获的最大编号

The remaining tanks we captured must be on its left

剩下我们俘获的那些坦克必须在它左边

So the number of methods should be in

所以方法数是不是应该是在

Find  $k-1$  among  $M-1$  tanks

在 $M-1$ 辆坦克中找 $k-1$ 辆

So many methods right

这么多种方法 对吗

This  $M$  should be equal to

这个 $M$ 它应该是等于

$k+1$  all the way to  $N$ , right

$k+1$  一直到 $N$  是吧

There are many possibilities for this  $M$

这个 $M$ 有很多种可能

Good  $M$  has so many possibilities

好  $M$ 有这么多种可能

Then on average	那么我们平均来讲	
What is the largest number of these tanks you captured	你俘获的这些坦克中最大编号是多少	
What is this called? This is called mathematical expectation	这个叫做什么呢 这个叫数学期望	期望 (qī wàng) to have expectations; to earnestly hope; expectation; hope.
Means that you may have captured	意思是说你可能俘获的	
The maximum number of this tank is like 10	这个坦克最大编号是比如10	
It could be 11 or it could be 12	也可能是11 也可能是12	
It could be 13 or it could be 14 all the way to N, right?	也可能是13 也可能是14 一直到N 对吧	
In each case there is a corresponding probability	每一个情况下都有一个相应的概率	相应 (xiāng yìng) to correspond; answering (one another); to agree (among the part); corresponding; relevant; appropriate; (modify) accordingly.
How to calculate mathematical expectations	数学期望怎么算呢	
Is to use the largest number in each case	就是用每一种情况最大的编号	
Multiply by its corresponding probability and then take the sum	再乘以它相应的概率 然后取加和	乘以 (chéng yǐ) (math.) multiplied with.
This is called mathematical expectation, right?	这个就叫数学期望是吧	
And the value of M is still the same sentence	而且这个M的取值还是那句话	
From k to N	从k开始一直取到N	
We calculate the mathematical expectation	我们把数学期望给算出来	
This is the most likely largest number in the captured tank, right?	这就是俘获坦克中最有可能的最大编号 对吧	
Then let's count this number	然后我们来算一下这个数	
This number is represented by E	这个数用E来表示	



The mathematical expectation of capturing the maximum value of the tank number

It is equal to  $\sum M$  from  $k$  to  $N$

Then  $M \times c(M-1, k-1) / c(N, k)$

Then we can use the formula we just mentioned

Make a deformation

What can it become

Can become  $\sum M$  equals  $k$  all the way to  $N$

Then  $k \times c(M, k)$  and then divide by a  $c(N, k)$

This is actually an additive form

Then you can use this formula

Add this and change it, right?

I will not write carefully

Anyway, what is the final result

Equal to  $k$  times  $c(N+1, k+1)$  divided by a  $c(N, k)$

Then we put this formula

Use this combination number formula to expand, right?

What is the result of the final expansion?

Is  $k(N+1)/(k+1)$

We finally figured it out

In other words, we can capture  $k$  tanks

There are many possibilities for the maximum number of the  $k$  tanks

But among the many possible maximum numbers

俘获坦克编号的最大值的数学期望

它等于 $\sum M$ 从 $k$ 开始一直到 $N$

然后  $M \times c(M-1, k-1) / c(N, k)$

然后我们可以用刚才我们说的这个公式

做一个变形

它就可以变成什么呢

可以变成 $\sum M$ 等于 $k$ 一直到 $N$

然后 $k \times c(M, k)$ 然后再除以一个  $c(N, k)$

这个实际上是一个加和的形式

然后你可以利用这个公式

再把这个加和给换一下 是吧

我就不仔细写了

反正最后的结果它等于什么

等于 $k$ 倍的 $c(N+1, k+1)$ 再除以一个  $c(N, k)$

然后我们再把这个式子

利用这个组合数公式展开 是吧

最后展开完的结果是什么呢

就是 $k(N+1)/(k+1)$

我们终于算出来了

也就是说 我们可以俘获 $k$ 辆坦克

这 $k$ 辆坦克的最大编号有很多种可能

但是这个很多种可能的最大编号里

除以 (chú yǐ) (math.) divided by.

形式 (xíng shì) outer appearance; form; shape; formality.

展开 (zhǎn kāi) to unfold; to carry out; to be in full swing; to launch.

也就是说 (yě jiù shì shuō) in other words; that is to say; so; thus.

On average, the largest number is this value

平均来讲 最大编号是这个值

It is related to the total number of tanks

它跟坦克的总数量有关

It also has to do with the number of tanks you captured, right?

还跟你俘获坦克的数量有关 对不对

Well, let's say that in the actual sample

那好 我们假如说 在实际的样本中

假如 (jiǎ rú) if.

For example, we captured a lot of tanks

比如说我们就俘获了一大堆坦克

堆 (duī) to pile up; to heap up; a mass; pile; heap; stack; large amount.

In the actual tank sample, the largest number is m

在实际的坦克样本中 这个最大的编号是m

Then we think your highest number in the sample

那么我们认为 你在样本中的这个最大编号

Is the most likely largest number

就是最有可能的最大编号

What it actually happened is the most likely

它实际发生的这个就是最有可能的

So I made this value directly equal to

所以我令这个值直接等于

令 (lìng) to order; to command; an order; warrant; writ; to cause; to make sth happen; virtuous; honorific title; season; government position (old).

$k \times (N+1)/(k+1)$

$k \times (N+1)/(k+1)$

So we can get

这样我们就可以得到

Estimated value of the total number of tanks

坦克的总数量的估计值

It is equal to  $m+(m-k)/k$

它等于  $m+(m-k)/k$

This is a formula that we got after pushing for a long time

这个就是我们推了半天得出来的一个公式

半天 (bàn tiān) half of the day; a long time; quite a while; midair.

Let's explain the formula

我们来解释一下这个公式里面的

Explain the meaning of each letter again

每个字母的含义 再解释一遍

字母 (zì mǔ) letter (of the alphabet). 含义 (hán yì) meaning (implicit in a phrase); implied meaning; hidden meaning; hint; connotation. 一遍 (yī biàn) one time (all the way through); once through.

This m is the maximum value of the sample

这个m就是样本的最大值 样本的最大值

You say you captured 10 tanks

你比如说你俘获了10辆坦克

The largest number is 55, so this m is 55, right  
 This k is the number of samples  
 Number of samples You captured 10 tanks  
 This k is 10  
 Then you calculate it like this, the final N  
 Is the maximum value of the overall estimate, right?  
 Overall maximum  
 We estimate that the overall maximum is this N  
 So we can use the maximum value of the sample  
 To estimate the maximum value of the population  
 This was verified during World War II, right?  
 This is a very effective method  
 So if we captured a tank, the number is 50  
 Let's say  $50 + (50 - 1) / 1 = 99$   
 99 is the maximum possible value of the tank  
 If we capture two tanks  
 If the maximum number is still 50  
 That is  $50 + (50 - 2) / 2$   
 The final estimated maximum value is 74, right  
 The more tanks you capture  
 The more accurately you can estimate the maximum value of the population

最大编号是55 那这个m就是55 对吧

这个k就是样本的数量

样本的数量 你俘获了10辆坦克

这k就是10

然后你把它这么一算 最后算出来的这个N

就是总体的估计的最大值 是吧

总体的最大值

我们估计总体最大值就是这个N

这样我们就可以用样本的最大值

来估计总体的最大值了

那这个事在二战的时候已经验证过了 对吧

这是个非常有效的方法

那么假如说我们俘获了一辆坦克 编号是50

我们就说  $50 + (50 - 1) / 1 = 99$

99就是坦克的有可能最大值

我们如果俘获了两辆坦克

编号最大值还是50的话

那就是  $50 + (50 - 2) / 2$

最后的估计最大值就是74 对吧

你俘获的坦克数量越多

你就越能够准确地估计出总体的最大值

验证 (yàn zhèng) to inspect and verify; experimental verification; to validate (a theory); to authenticate.

This method is actually very effective in life

这个方法在生活中其实很有效

For example, you are in a class

比如说你在一个**班级**里面

**班级 (bān jí)** class (group of students); grade (in school).

Randomly found the student number of a few classmates

随便发现了几位同学的这个**学号**

**学号 (xué hào)** student ID number.

Then you can use the student ID of these people

那你就可以根据这几个人的学号

To estimate how many people there are in their class, right?

来估计他们班一共有多少个人 对吧

You tear out a few pages in a book to show others

你在一本书里边随便**撕**出几页纸给别人看

**撕 (sī)** to tear.

Others can use these pages

别人可以根据这几页纸

To estimate how many pages there are in this book, right?

来估计这本书一共有多少页 对不对

So this method is actually quite effective

所以这个方法其实还是挺有效的

We now use this method to estimate

我们现在就用这种方法来估计

This China Merchants Bank credit card is the size of a chicken leg

这个招商银行信用卡它的这个**鸡腿**大小

How big is the chicken drumstick of China Merchants Bank

招行的鸡腿到底有多大

We know this chicken leg activity of China Merchants Bank

我们知道招商银行的这个**鸡腿活动**

You (single pen) can smoke chicken drumsticks once for 18 yuan

你(单笔)刷满18元就可以抽一次**鸡腿**

You can draw up to 100 times

最多可以抽100次

But we don't know how big this biggest drumstick is

但是我们不知道这个最大**鸡腿**有多大

We might as well make a bold assumption

我们**不妨**做一个**大胆的假设**

**不妨 (bù fāng)** there is no harm in; might as well. **大胆 (dà dǎn)** brazen; audacious; outrageous; bold; daring; fearless. **假设 (jiǎ shè)** to suppose; to presume; to assume; supposing that ...; if; hypothesis; conjecture.

Suppose the chicken leg is drawn from this prize pool

Randomly selected

The probability of each amount appearing is equal

Then its distribution is a uniform distribution

It's similar to this German tank problem

So we can use the size of the chicken legs

To estimate the maximum value of the overall drumstick

Let's make a comparison

If we smoked chicken legs

Its number as the first column is k, right

Then the size of your sample or chicken drumstick

The size of this chicken leg is the second column

Its unit is minutes

Because the smallest interval is minutes

And its largest sample

Or the biggest chicken drumstick I pulled out

Which is the m here just now

This m is the maximum value in the sample, right

假设抽的这个鸡腿是从这个奖池中

随机抽取出来的

每一个金额出现的概率都相等

那这样一来它的分布就是一种均匀分布

就类似于这个德国坦克问题了

于是我们就可以通过抽出来的鸡腿大小

来估计总体鸡腿的最大值

我们来做一个比较 那大家看

假如说我们抽的鸡腿

它的次数作为第一列就是k 对吧

然后你这个样本或者说抽的鸡腿大小

这个鸡腿的大小 样本 我们作为第二列

它的单位是分

因为它最小的这个间隔是分吗

然后它的这个最大的样本

或者说最大的我抽出来的鸡腿

也就是刚才我们这里边的m

这m是样本中的最大值 对吧

池 (chí) pond; reservoir; moat.

抽取 (chōu qǔ) to extract; to remove; to draw (a sales commission, venom from a snake etc).

金额 (jīn é) sum of money; monetary value. 相等 (xiāng děng) equal; equally; equivalent.

这样一来 (zhè yàng yī lái) thus; if this happens then.

类似 (lèi sì) similar; analogous.

次数 (cì shù) number of times; frequency; order number (in a series); power (math.); degree of a polynomial (math.). 作为 (zuò wéi) one's conduct; deed; activity; accomplishment; achievement; to act as; as (in the capacity of); qua; to view as; to look upon (sth as); to take sth to be.

单位 (dān wèi) unit (of measure); unit (group of people as a whole); work unit (place of employment, esp. in the PRC prior to economic reform).

间隔 (jiàn gé) compartment; gap; interval; to divide.

Then what do we estimate by these three numbers	那然后我们通过这三个数来估计什么呢	
Let's estimate the maximum value of this population	我们来估计这个总体的最大值	
The biggest drumstick in the prize pool The biggest drumstick in the prize pool	奖池里的最大鸡腿 奖池中的最大鸡腿	
This is called N	这个就叫N	
Is similar to the tank we captured	就类似于我们通过俘获的坦克	
To estimate the largest tank	来估计最大坦克一样	
This unit is divided	这个单位都是分	
We calculate this way	我们按这种方法来算	
If I smoke for the first time	假如我抽的 <b>第一次</b> 的时候	<b>第一次 (dì yī cì)</b> the first time; first; number one.
I found out that I got an 80-point chicken leg	我发现我 <b>抽中</b> 了一个80分的鸡腿	<b>抽中 (chōu zhòng)</b> to win (a prize in a lottery).
The biggest drumstick is 80 points, right?	那最大的鸡腿就是80分 对不对	
Then I bring this k and m into this formula	然后我把这个k和m我带入到这个公式里去	
$80+(80-1)/1$	$80+(80-1)/1$	
The result is 159	结果是159	
So I estimate that the biggest chicken leg in the prize pool is 159 points	所以我估计奖池中的最大鸡腿就是159分	
I can estimate it just once	就抽一次我就能估计出来	
If I smoke twice	那如果我抽了两次	
There are two chicken drumsticks when I smoke it twice	抽两次的时候这个鸡腿有两个	
One is 80 points and the other is 100 points 1 yuan	一个是80分 还有一个是100分 1块钱的	
Then the biggest chicken thigh in these two is 100 points	那么这两个里边最大的鸡腿是100分的	
I pass this 100 points and twice I can calculate	我通过这个100分和两次我就可以计算出来	

The biggest chicken leg N in the prize pool may be worth it	奖池中最大鸡腿N的可能值了	
Use $100+(100-2)/2$	用 $100+(100-2)/2$	
The result is 149 points	结果是149分	
If I smoked chicken thighs three times	如果我抽了三次鸡腿	三次 (sān cì) third; three times; (math.) degree three, cubic (equation).
These three chicken legs are 80 100 and 200	这三次鸡腿分别是80 100和200	
Smoked a two yuan	抽了一个两元的	
Isn't the biggest drumstick 200 points at this time?	那这个时候最大鸡腿不是200分了嘛	
I then substitute $200+(200-3)/3$	我再代入 $200+(200-3)/3$	代入 (dài rù) to substitute into.
Finally got 266	最后得到266	
This is the biggest drumstick I estimate	这个就是我估计的最大鸡腿	
If i smoke 4 times	如果我抽了4次	
Draw 4 times, for example, we are 80 100 200	抽了4次比如说我们是80 100 200	
Draw another 100 for the 4th time	第4次又抽了个100	
So in this way, we draw a maximum of 200 points	所以这样一来我们就抽中了最大值是200分	
But we smoked 4 times	但是我们抽了4次	
So one more time than before	所以比刚才多一次	
Let's substitute this formula	我们再代入这个公式	
$200+(200-4)/4$	$200+(200-4)/4$	
The final result is 249 points	最后算出来结果249分	
249 points is 2 yuan 4 gross 9	249分就2块4毛9	
If we estimate that we are not far from ten	如果我们这个估计八九不离十的话	八九不离十 (bā jiǔ bù lí shí) pretty close; very near; about right.
Then you draw 100 times if you are lucky	那么你抽100次如果运气特别好	运气 (yùn qì) luck (good or bad).
If you draw the biggest drumstick every time	每次都抽中最大鸡腿的话	每次 (měi cì) every time.

You might get back more than 200 yuan, right?

你没准可以拿回到200多块钱 是不是

Of course, we are just building on a uniformly distributed

当然了我们这只是**建立**在一个均匀分布的

**建立** (jiàn lì) to establish; to set up; to found.

Based on the model

**模型基础之上**

**模型** (mó xíng) model; mold; matrix; pattern. **之上** (zhī shàng) above.

But in fact, a policy given by China Merchants Bank says

但**事实上**招行给出的一个**政策**是说

**事实上** (shì shí shàng) in fact; in reality; actually; as a matter of fact; de facto; ipso facto. **政策** (zhèng cè) policy.

The smallest chicken drumstick with full 18 yuan is 0.16 yuan

刷满18元最小的鸡腿是0.16元

And the biggest drumstick is 11,111 yuan

而最大的鸡腿是11111元

So we don't actually know what kind of model it is

所以我们其实并不**清楚**它是一个什么样的**模型**

**不清楚** (bù qīng chu) unclear; not understood; currently unknown.

To distribute this chicken thigh for everyone

去给大家**分配**这个鸡腿的

**分配** (fēn pèi) to distribute; to assign; to allocate; to partition (a hard drive).

But there is always a dream, if it comes true

不过**梦想**总还是要有的**万一**实现了呢

**梦想** (mèng xiǎng) (fig.) to dream of; dream. **有的** (yǒu de) (there are) some (who are...); some (exist). **万一** (wàn yī) just in case; if by any chance; contingency. **实现** (shí xiàn) to achieve; to implement; to realize; to bring about.

Some students might say

也有同学可能会说

Double 11 simply can't buy so many things

双11**根本**买不了这么多东西

**根本** (gēn běn) fundamental; basic; root; simply; absolutely (not); (not) at all. **不了** (bù liǎo) unable to; without end.

How can it be done with 100 pens?

怎么可能刷满100笔呢

So this chicken thigh is not sincere enough

所以这个鸡腿给的**不够****诚恳**

**不够** (bù gòu) not enough; insufficient; inadequate. **诚恳** (chéng kěn) sincere; honest; cordial.

Let's calculate an account

我们来算一笔**账**

**账** (zhàng) account; bill; debt.

According to some company surveys

根据一些公司的**调查**

The average monthly consumption of the subjects they surveyed is 4800 yuan

他们调查的**对象**中平均月**消费**是4800元

**对象** (duì xiàng) target; object; partner; boyfriend; girlfriend. **消费** (xiāo fèi) to consume; to spend.

61% of the 4,800 yuan is paid by third parties

这4800元中有61%都是通过**第三方****支付**

**支付** (zhī fù) to pay (money).



Which is carried out by WeChat Alipay	也就是微信支付宝进行的	
Another 23% is done by bank card credit card	还有23%是通过 <b>银行卡</b> 信用卡进行的	<b>银行卡</b> (yín háng kǎ) bank card; ATM card.
Only 14% are transacted through cash	只有14%是通过 <b>现金</b> 进行交易的	<b>进行交易</b> (jìn xíng jiāo yì) to carry out a transaction.
According to statistics from the Ministry of Industry and Information Technology	而根据 <b>工信部的统计</b>	<b>工信部</b> (gōng xìn bù) Ministry of Industry and Information Technology (abbr). <b>统计</b> (tǒng jì) statistics; to count; to add up.
There are about 1 billion mobile payment users in China	中国的 <b>移动支付</b> 用户大概有10亿人	<b>移动</b> (yí dòng) to move; movement; migration; mobile; portable. <b>用户</b> (yòng hù) user; consumer; subscriber; customer.
In 2019, a total of 1.22 trillion pens were made	2019年的时候一共刷了1.22万亿笔	
If every person is averaged every month	如果平均到每一个人每一月的话	
It happened to be 100 strokes	<b>刚好</b> 是刷满100笔	<b>刚好</b> (gāng hǎo) just; exactly; to happen to be.
Now we buy breakfast and take a taxi in our daily life	现在我们每天的生活中买 <b>早餐</b> <b>打车</b>	<b>早餐</b> (zǎo cān) breakfast. <b>打车</b> (dǎ chē) to take a taxi (in town); to hitch a lift.
Pay utility bills, pay phone bills	交 <b>水电费</b> 交电话费	<b>水电</b> (shuǐ diàn) hydroelectric power; plumbing and electricity.
Are you using online payment all the time?	是不是 <b>每时每刻</b> 都在使用着 <b>网络</b> 支付呢	<b>每时每刻</b> (měi shí měi kè) at all times; at every moment. <b>网络</b> (wǎng luò) network (computing, telecommunications, transport etc).
And this activity of adding chicken legs	而这个加鸡腿的活动	
From October 20th to November 30th	是从10月20号到11月30号	
So brushing 100 pens is actually not a problem at all	所以刷满100笔其实根本不是 <b>事儿</b>	<b>事儿</b> (shì r) one's employment; business; matter that needs to be settled; (northern dialect) (of a person) demanding; trying; troublesome; erhua variant of 事 (shì).
And the meaning of this activity is to say	而且这个活动的意思是说	
As long as you bind a China Merchants Bank credit card for payment	只要你绑定了招商银行信用卡进行支付	
No matter if you used WeChat or Alipay before	那无论前面你是使用了 <b>微信</b> <b>支付宝</b>	

Or whether you are shopping  
or taking a taxi to eat

或者无论你是购物 还是打车吃饭

As long as (single pen) brush  
up to 18 yuan, you can get cash  
back

只要(单笔)刷满18元 你都可以笔  
笔返现

For local tyrants

对于土豪来讲

You only need to split a large  
consumption into several small  
consumptions

你只要把一个大的消费拆成几个  
小笔的消费

For ordinary people, lunch  
costs less than 18 yuan

而对于普通人午餐费用18元都不  
到的

A hard year

辛苦了一年

May wish to add two poached  
eggs to every meal for yourself  
this month

不妨在这个月给自己每一餐加两  
个荷包蛋

Add another chicken leg

再加一个鸡腿

Maybe this chicken drumstick  
can still be waived

兴许这个鸡腿还是可以免单的

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updated information the first  
time

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返(fǎn) to return (to).

土豪(tǔ háo) local tyrant; local strong man; (slang)  
nouveau riche.

拆(chāi) to tear open; to tear down; to tear apart; to  
open. 几个(jǐ ge) a few; several; how many.

普通人(pǔ tōng rén) ordinary person; private citizen;  
people; the person in the street. 午餐(wǔ cān) lunch;  
luncheon. 不到(bù dào) not to arrive; not reaching;  
insufficient; less than.

餐(cān) meal; to eat; classifier for meals. 荷包蛋(hé  
bāo dàn) poached egg; egg fried on both sides.

兴许(xìng xǔ) perhaps.

视频(shì pín) video.

帐号(zhàng hào) account number.

铃铛(líng dang) little bell. 第一时间(dì yī shí jiān) in  
the first moments (of sth happening); immediately  
(after an event); first thing. 更新(gēng xīn) to replace  
the old with new; to renew; to renovate; to upgrade; to  
update; to regenerate.