

Determine whether each conjecture is true or false. Provide a counterexample for any false conjecture.

- 1) Given: $m\angle A = m\angle B$

1) TRUE **FALSE**

Conjecture: $\angle A$ and $\angle B$ are vertical angles.

Counterexample (if FALSE): $\angle A$ & $\angle B$ can be a linear pair, both 90°

- 2) Given: $AM = MB$

2) TRUE **FALSE**

Conjecture: M is the midpoint of $\overline{AB}$



Counterexample (if FALSE): _____

Use the following conditional statement for questions 3 – 5.

Right angles are congruent.

- 3) Write the statement in If-then form: If 2 angles are right, then they are congruent.

- 4) Write the hypothesis and conclusion.

Hypothesis: 2 angles are right (p) ($p \rightarrow q$)

Conclusion: they are congruent (q)

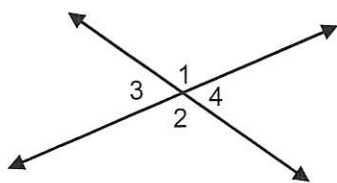
- 5) Write the converse of question 3: If 2 angles are congruent, then they are right. ($q \rightarrow p$)

- 6) Write the inverse of question 3: If 2 angles are not right, then they are not congruent. ($\sim p \rightarrow \sim q$)

- 7) Write the contrapositive of question 3: If 2 angles are not congruent, then they are not right. ($\sim q \rightarrow \sim p$)

- 8) Is the converse of question 3 TRUE? If not, please provide a counterexample: No. 2 angles can both be 60° , thus congruent, but not right.

Use the following picture for questions 9 -12.



$$\begin{array}{r}
 6x - 5 = 5x + 23 \\
 \underline{-5x + 5} \quad \underline{-5x + 5} \\
 x = 28
 \end{array}$$

- 9) If $m\angle 1 = 6x - 5$ and $m\angle 2 = 5x + 23$, find the value of x .

9) $x = 28$

- 10) Based on #9, find the $m\angle 1$ and $m\angle 2$.

10) $m\angle 1 =$ 163
 $m\angle 2 =$ 163

- 11) If $m\angle 1 = 4y - 7$ and $m\angle 3 = 2y + 7$, find the value of y .

$$\begin{array}{l}
 4y - 7 + 2y + 7 = 180 \\
 6y = 180 \\
 y = 30
 \end{array}$$

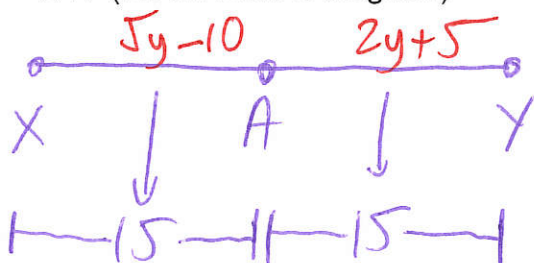
11) $y = 30$

- 12) Based on #11, find the $m\angle 3$ and $m\angle 4$.

$$\angle 3 = 2y + 7 = 2(30) + 7 = 67$$

12) $m\angle 3 =$ 67
 $m\angle 4 =$ 67

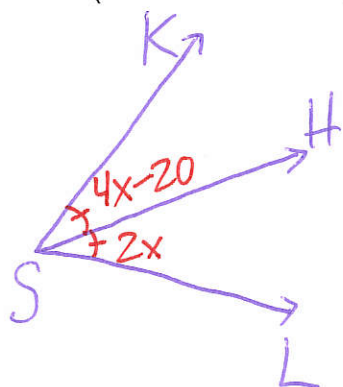
- 13) If A is the midpoint of XY , $XA = 5y - 10$ and $AY = 2y + 5$, find XY . (HINT: Draw a diagram)



$$\begin{array}{r}
 5y - 10 = 2y + 5 \\
 \underline{-2y + 10} \quad \underline{-2y + 10} \\
 3y = 15 \\
 y = 5
 \end{array}$$

13) 30

- 14) Given that $\overline{SH}$ bisects $\angle KSL$, $m\angle KSH = 4x - 20$, and $m\angle LSH = 2x$. Find the measure of $\angle KSH$. (HINT: Draw a diagram)



$$\begin{array}{r}
 4x - 20 = 2x \\
 \underline{-4x} \quad \underline{-4x} \\
 -20 = -2x \\
 x = 10
 \end{array}$$

$$\begin{array}{l}
 \angle KSH = 4x - 20 \\
 = 4(10) - 20 \\
 = 20
 \end{array}$$

14) 20

Write whether each statement is TRUE or FALSE.

15) Right angles are congruent.

15) T F

16) If two angles are adjacent angles, then they are complementary.

16) T F

17) Two angles that are supplementary are congruent.

17) T F

Fill in the blank with the correct word(s).

18) A ? is an educated guess based on known information.

18) Conjecture

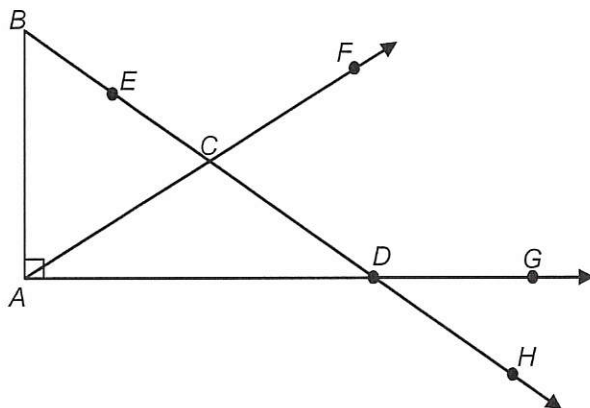
19) A pair of angles that have a common side and common vertex, but do not have any common interior points are called ?.

19) adjacent

20) The statement immediately following the word "then" in an If-then statement is called the ?.

20) conclusion

Use the diagram below to answer questions 21 – 25.



21) Name a pair of complementary angles.

21) $\angle BAC, \angle CAD$

22) Name a pair of vertical angles.

22) $\angle ECA, \angle FCD$

23) Name a linear pair.

23) $\angle CDA, \angle CDG$

24) Name the vertex of $\angle DCA$.

24) C

25) Name the sides of $\angle GDH$.

25) $\vec{DG}, \vec{DH}$

Consider the following statement for the problems below:

If someone drinks and drives, then s/he is at risk of causing an accident.

- 26) Create (2) additional statements that together with the statement above, exemplify the *Law of Detachment*.

(1) Sam drank and drove.

(2) She is at risk of causing an accident.

- 27) Create (2) additional statements that together with the statement above, exemplify the *Law of Syllogism*.

(1) If someone is at risk of causing an accident, then
someone may be hurt.

(2) If someone drinks and drives, then someone
may be hurt