

# Biomechanics in Orthodontics



Science of  
Mechanic



Biological  
System

MODERN SMILE INSTITUTE



# **BIOMECHANICS**

**MECHANICS—IS THE DISCIPLINE THAT DESCRIBES THE EFFECT OF FORCES ON BODIES.**

**BIOMECHANICS—STUDY OF MECHANICS AS IT AFFECTS THE BIOLOGIC SYSTEMS.**

**BIOMECHANICS— APPLICATION OF MECHANICS TO THE BIOLOGY OF TOOTH MOVEMENT.**



# The Basic Principle of Physical science

MECHANIC



# Rule of Mass

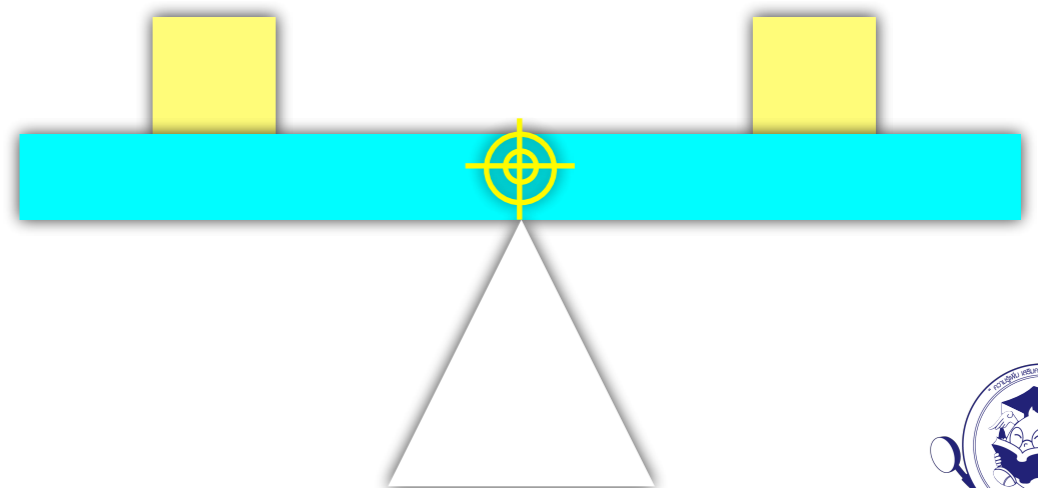
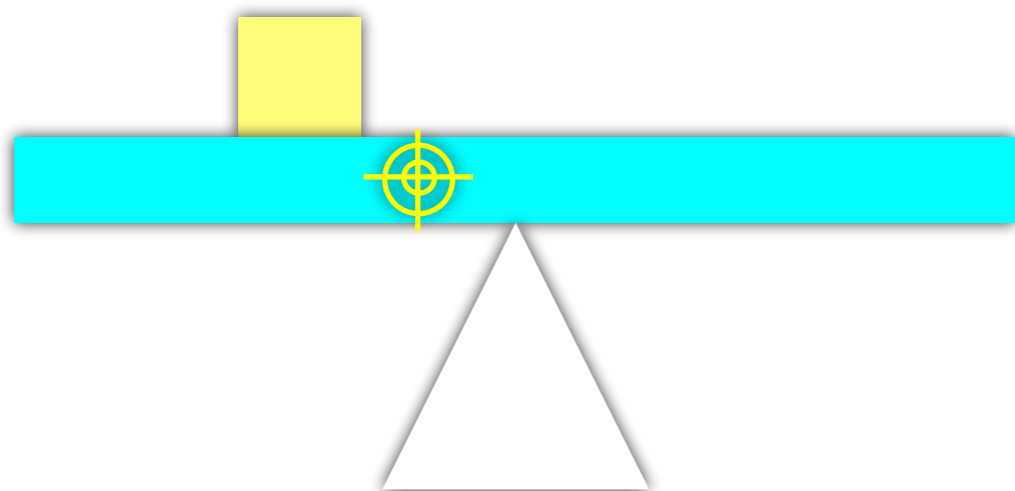
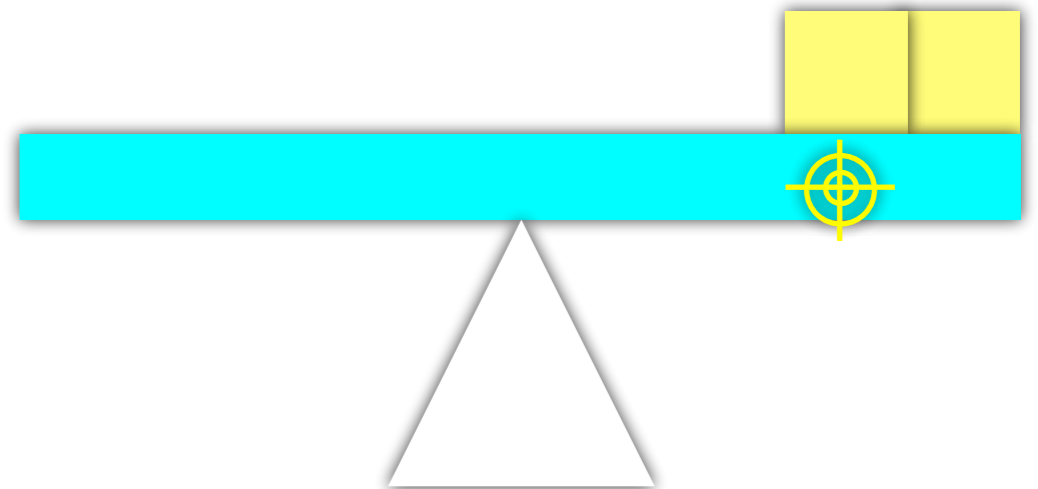
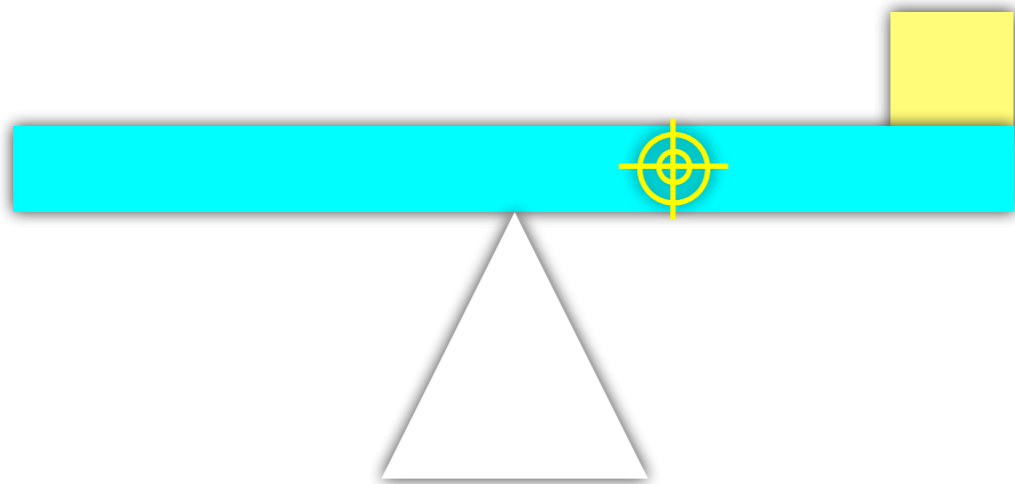
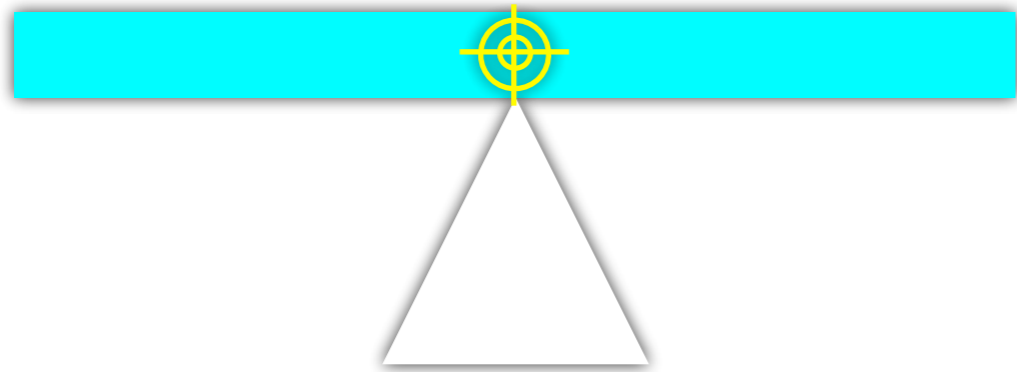
- Center of Mass (Free body) exists in all free object
- Center of Gravity (Free body)
- Center of Resistance (Restrained body)

The point that the force applied pass through any object to move linearly without any rotation or tilted

Balance



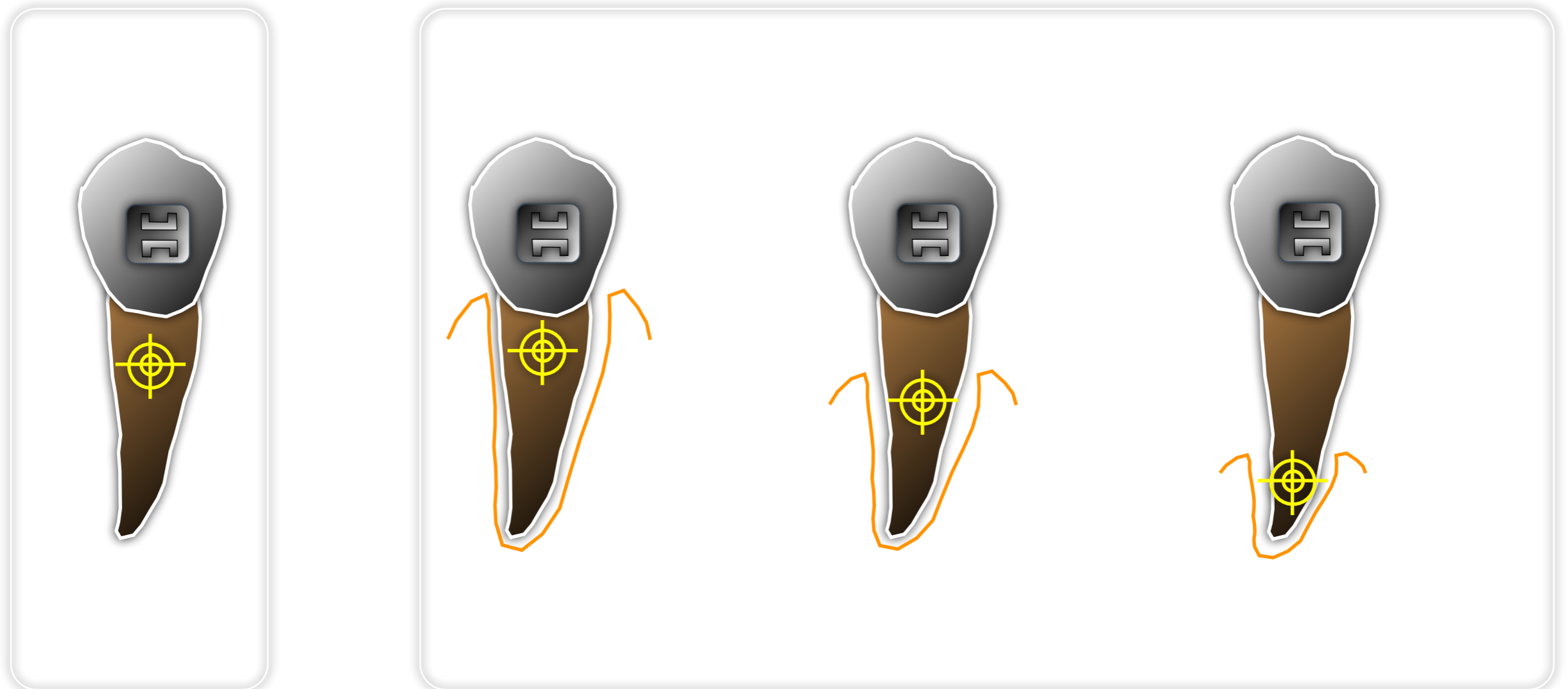
# Determination of Center of MASS



# Determination of Center of Resistance

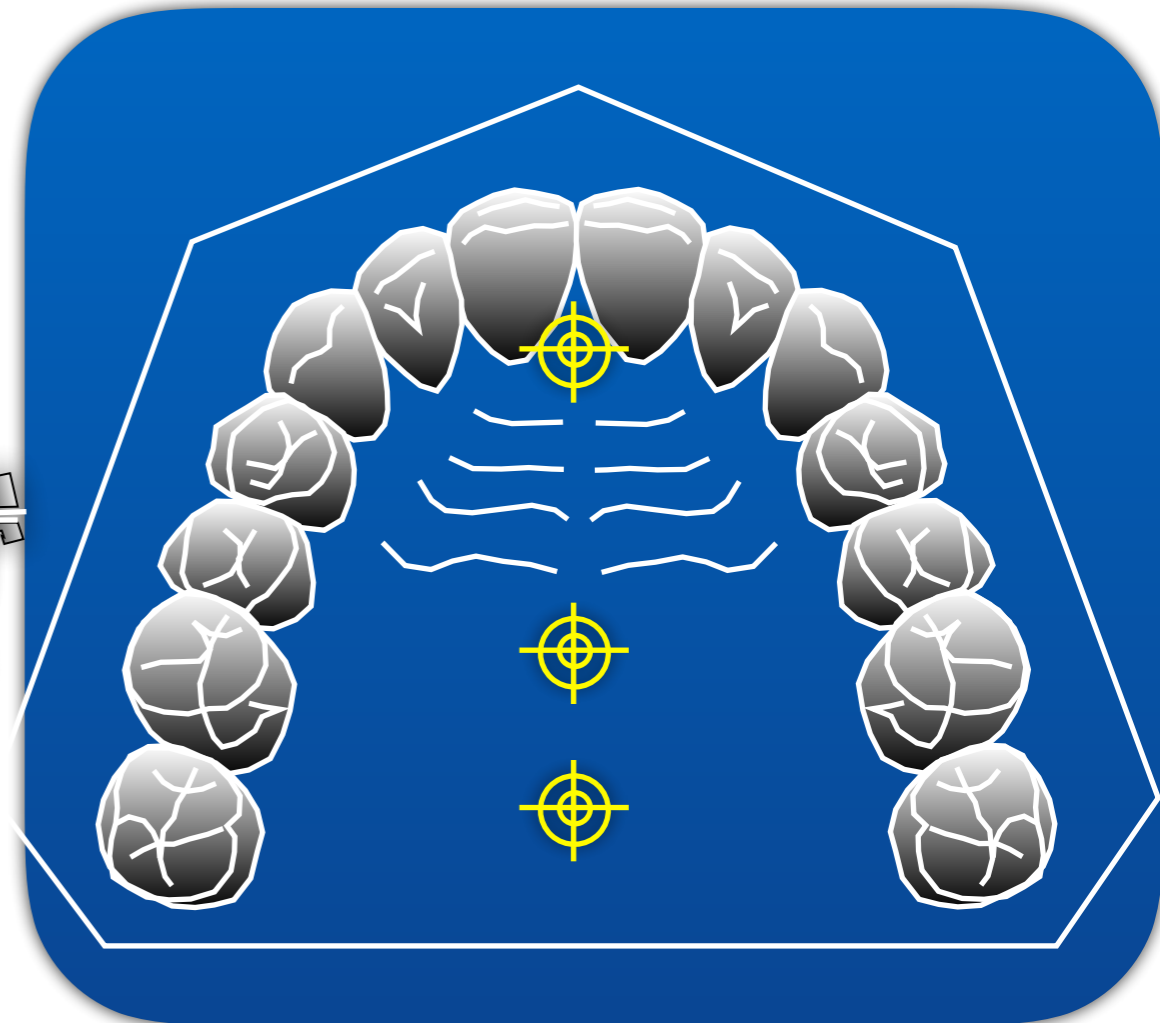
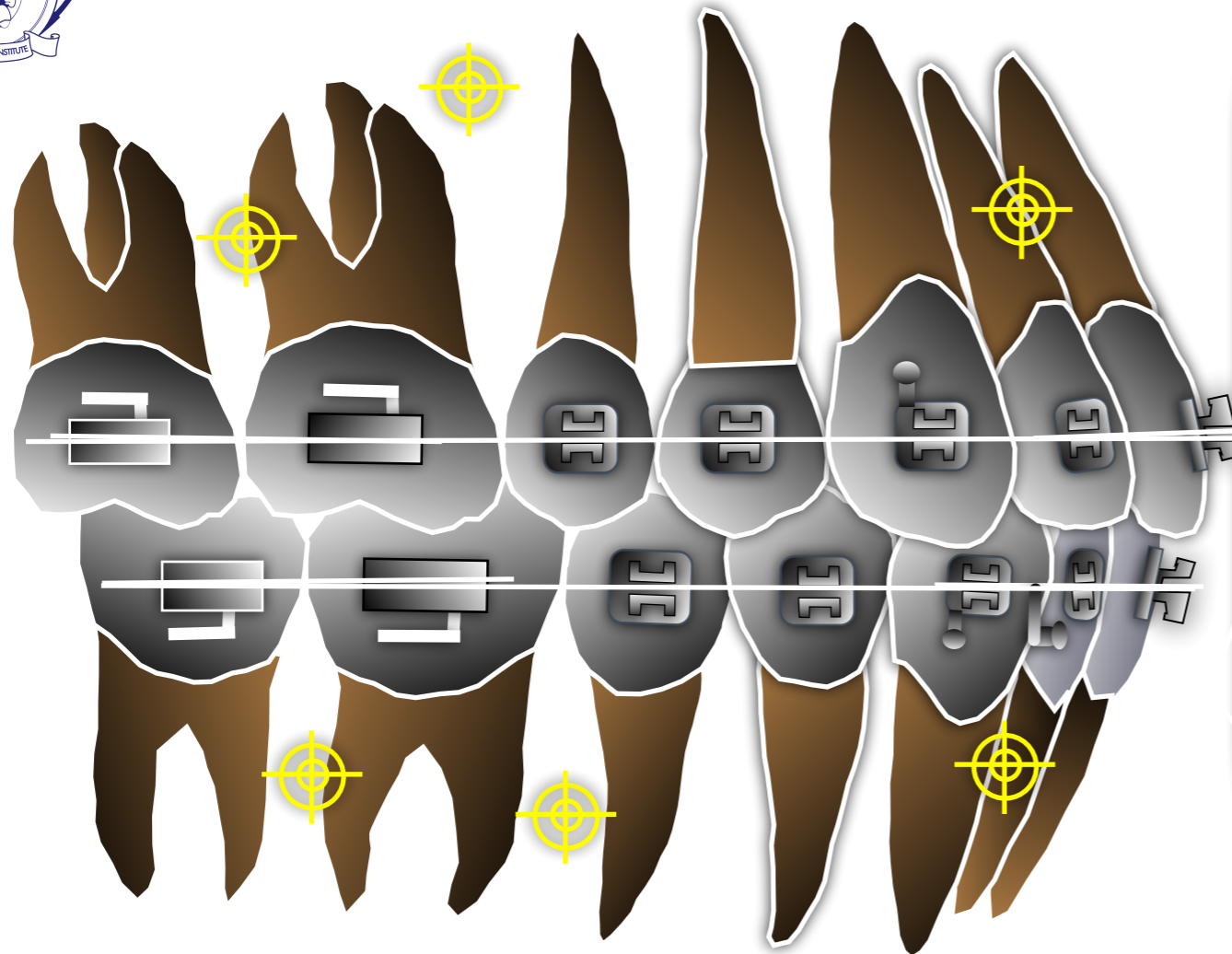


- Center of Mass (Free body) will never change
- Center of Resistance (Restrained body) can be changed according to the environment and not coincide with the CM

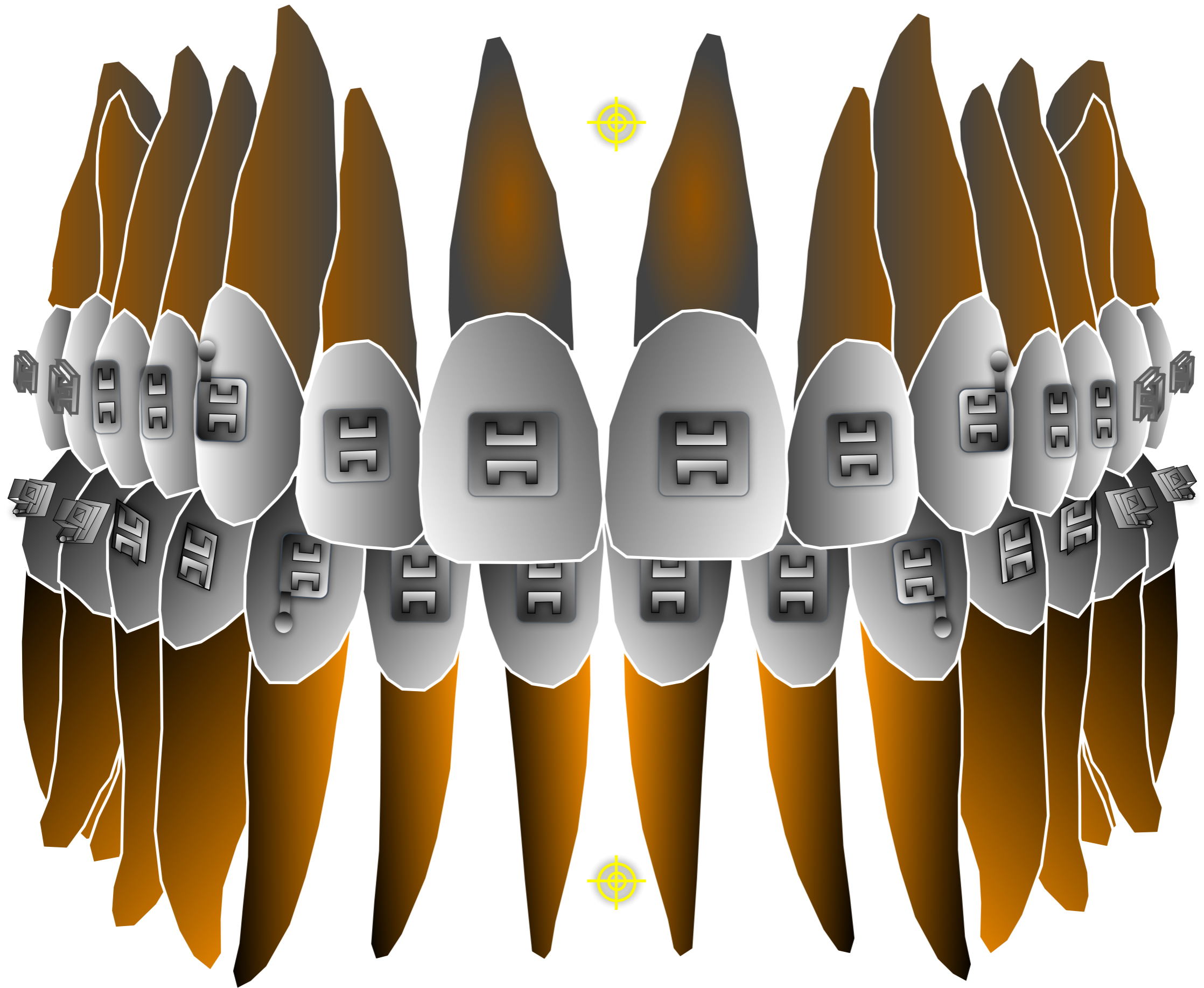




# Location of Center of Resistance in Orthodontics



- CR point is based on the estimation or calculate from the experiment therefore, the force system should be monitored according to clinical observation

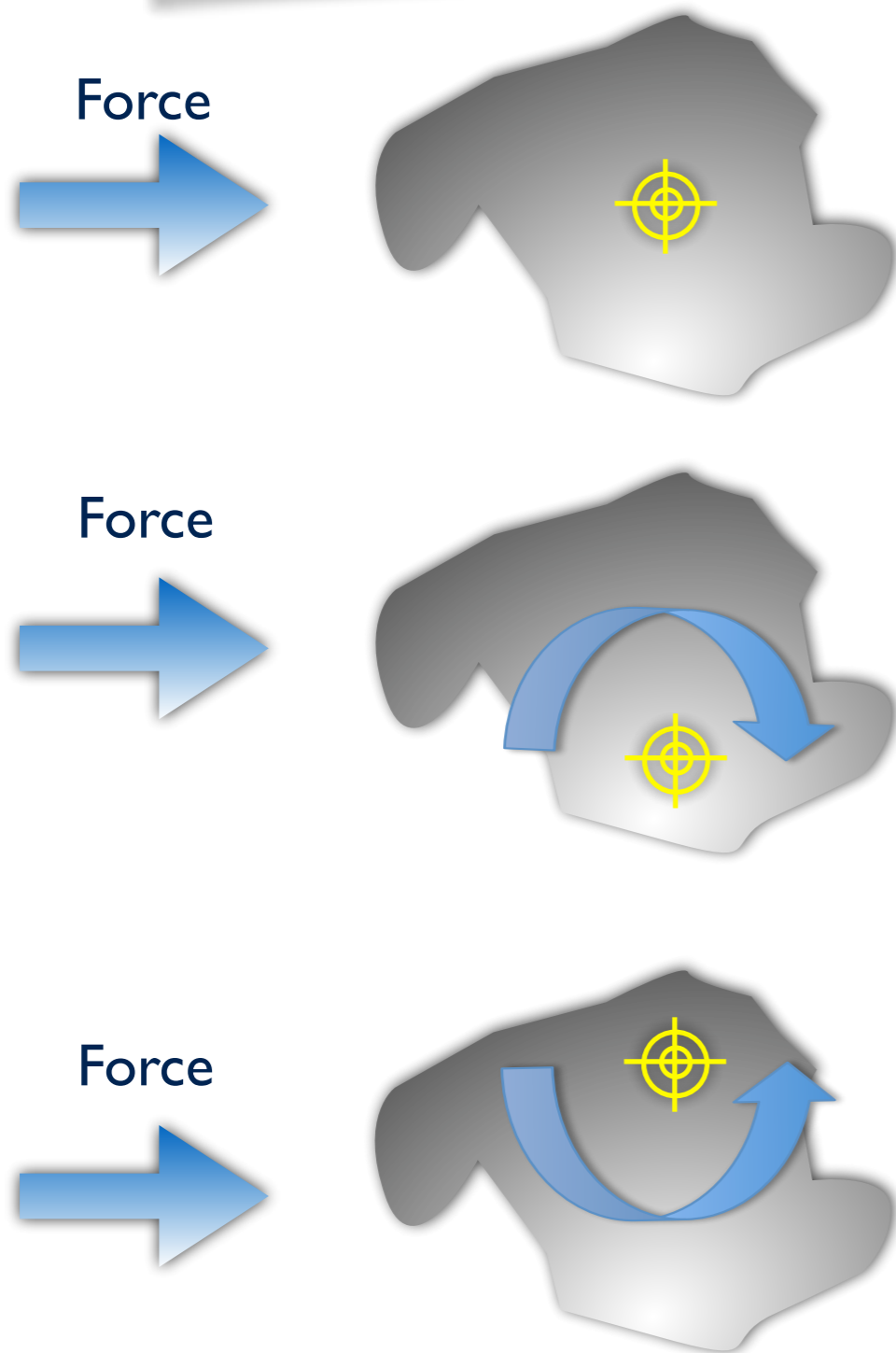




## Clinical implication for Location of CR

- CR will be about 33% - 40% from the marginal bone depending on the authors
- Practically, localization of CR is based on the estimation therefore, the force system should be monitored according to clinical observation
- CR position varies with root length, root morphology, numbers of root, numbers of teeth and alveolar crest height

# Mechanical Concepts in Orthodontics



The relationship of the **line of force** acting on the object to the **center of resistance (CR)** determines the type of movement expressed

# The basic concept of force

The force is a vector comprised of

1 Magnitude of force  
(Scalar)

3 Point of  
Application

10 Gm.

2 Direction  
(Line of force)

Note: 2 does not affect 3 (The law of transmissibility)



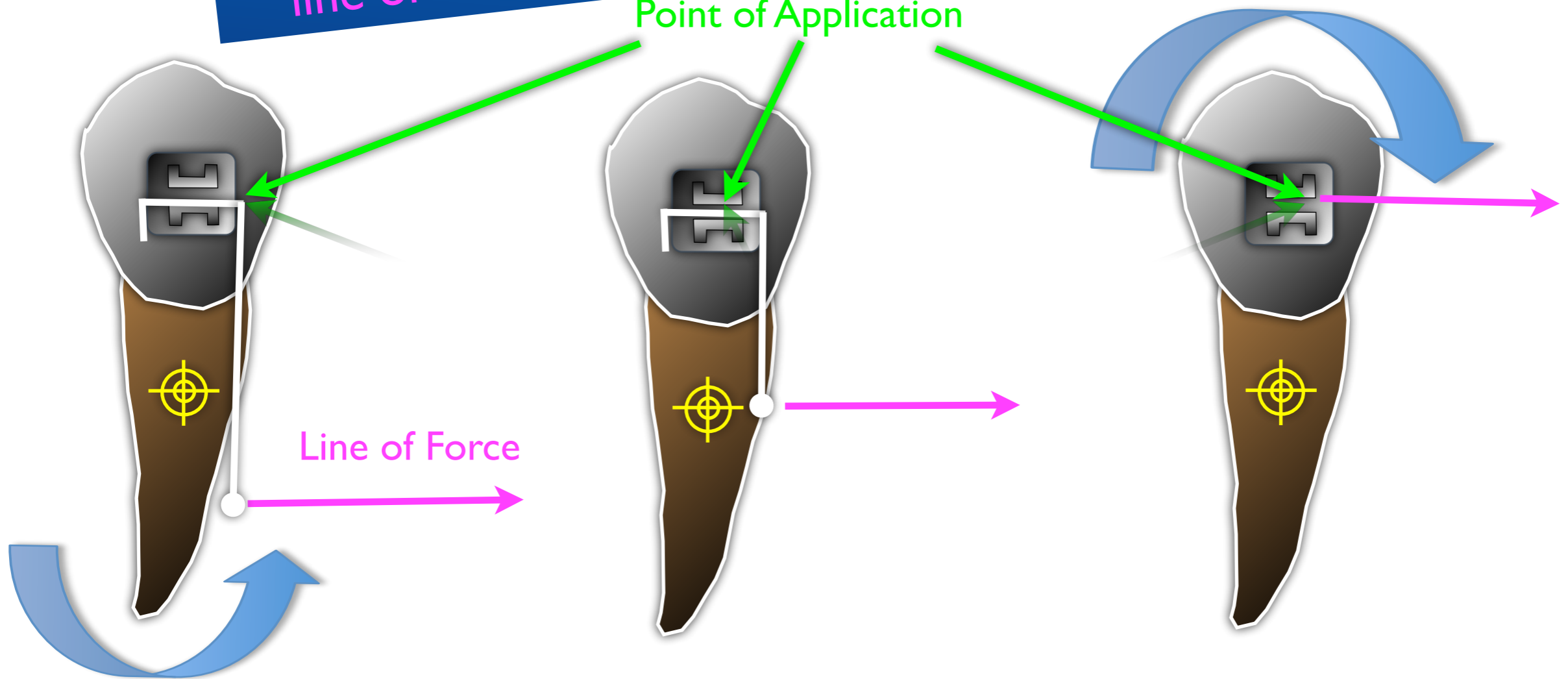
# Point of Application & Direction (line of force)

Type of Tooth movement affected by  
line of force to CR not point of application



Point of Application

Line of Force



Root MM.

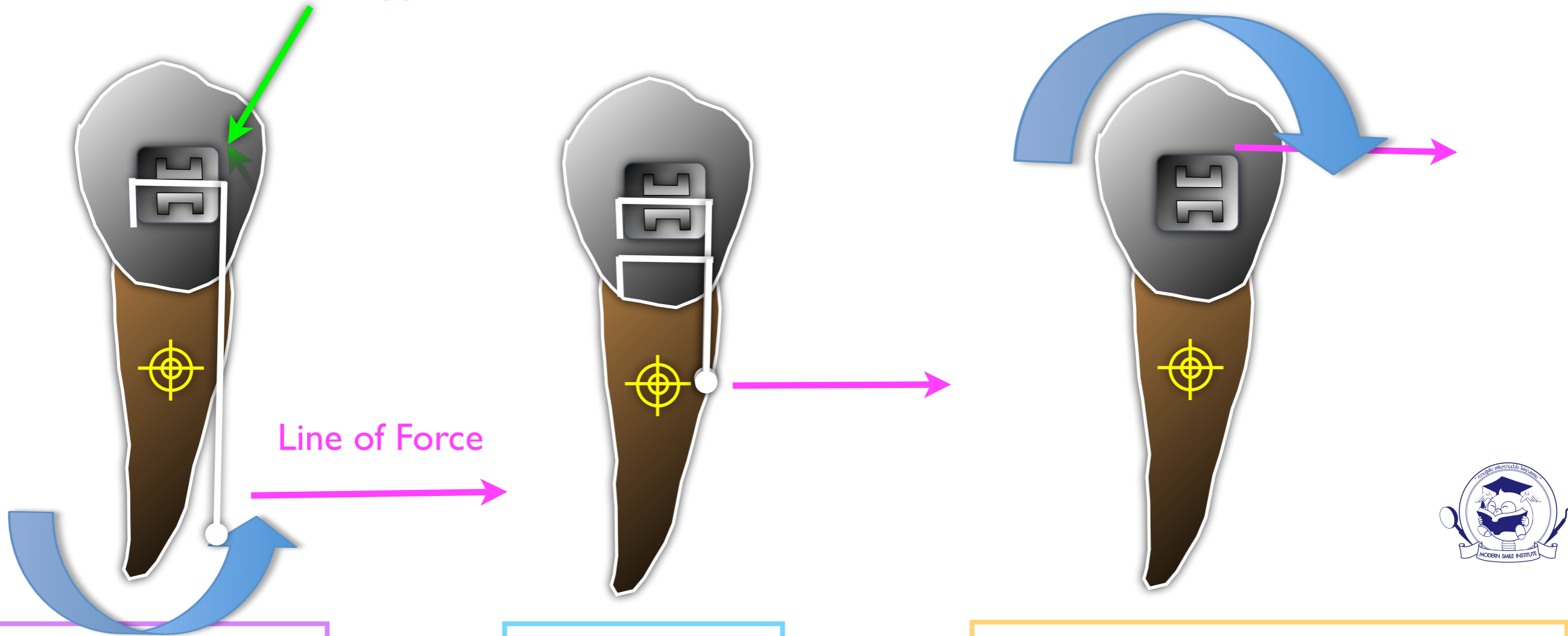
Translation

Crown tipping

# Point of Application & Direction (line of force)

Type of Tooth movement controllable by **handling line of force** not **point of application** (BKT position)

Point of Application



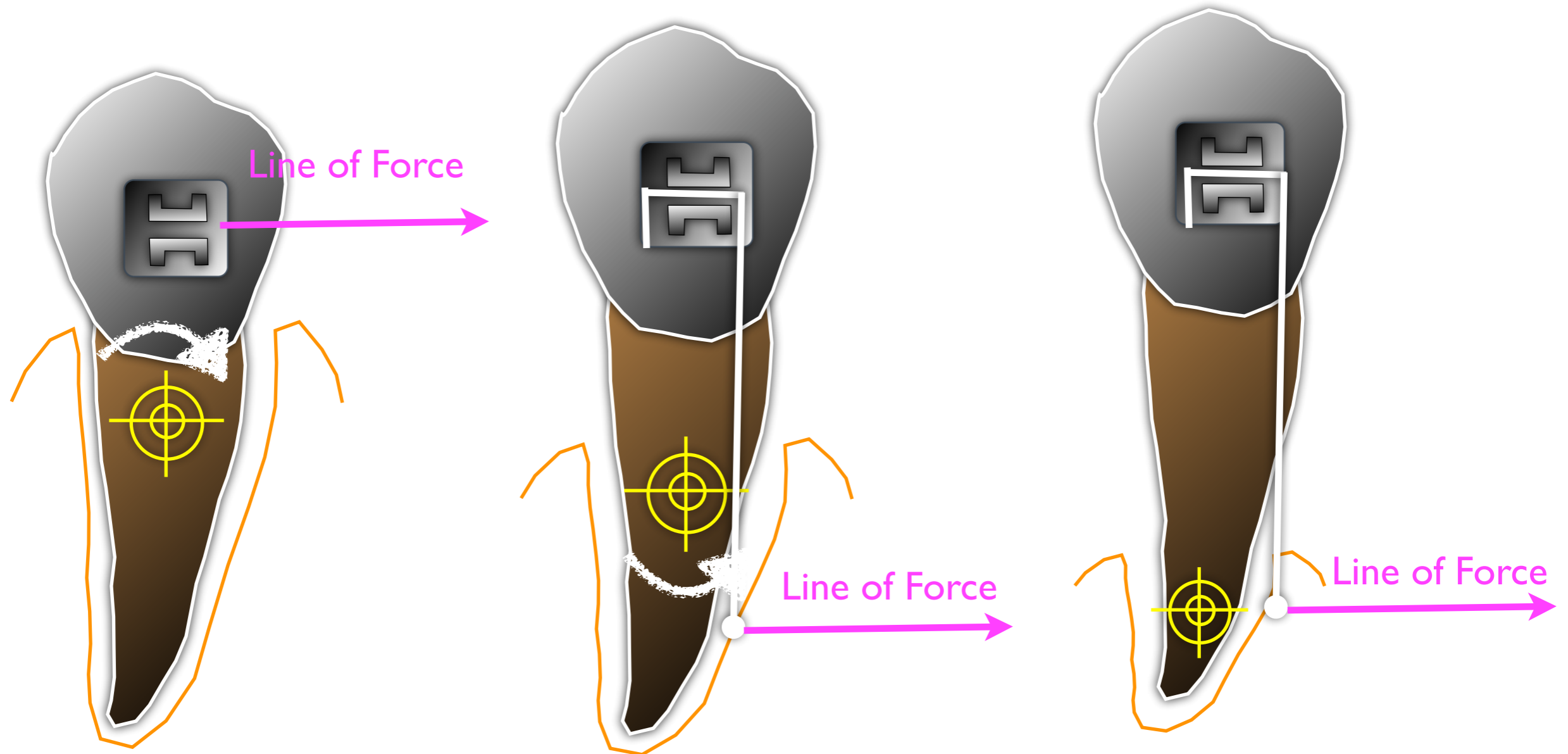
Less root MM.

Translation

Crown tipping increased



# Clinical implication for periodontal cases



Crown tipping

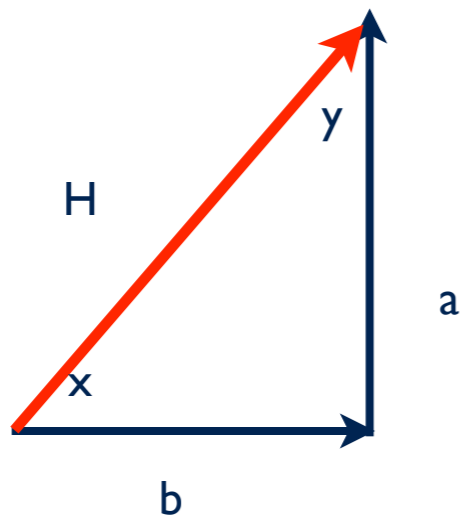
Root MM.

Translation



# Handling of Force

## Vector Composition



$$\begin{aligned}\sin x &= a/H \\ \cos x &= b/H \\ \tan x &= a/b\end{aligned}$$

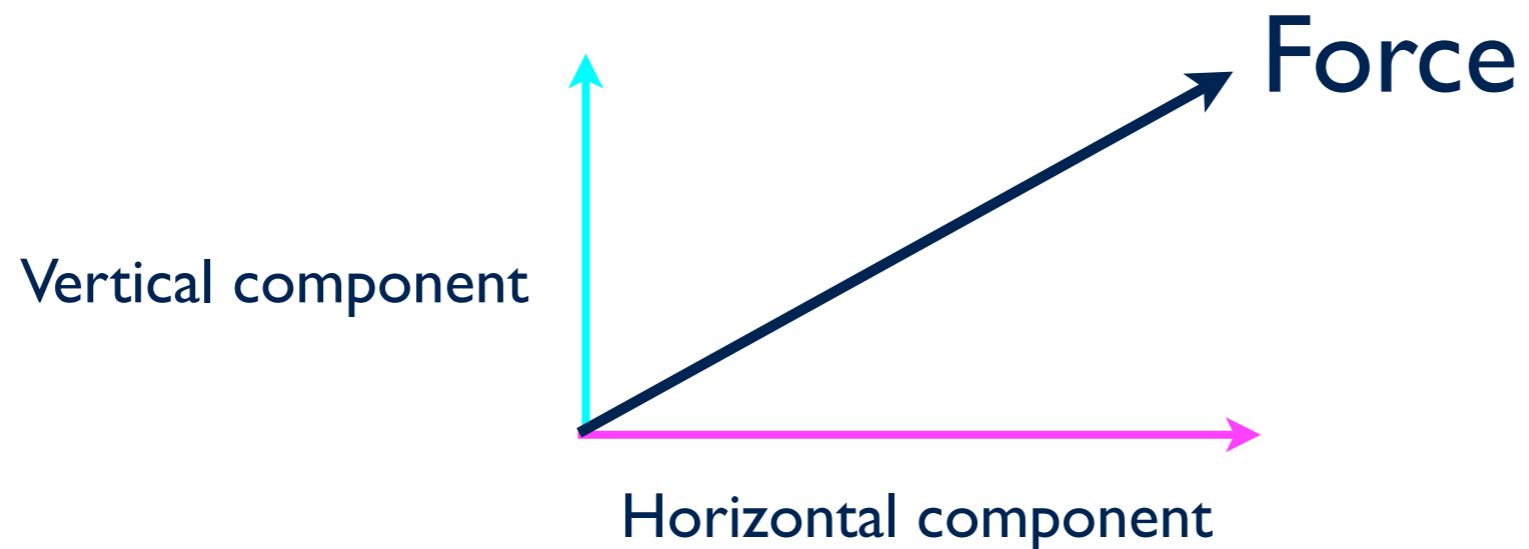
$$\begin{aligned}\sin y &= b/H \\ \cos y &= a/H \\ \tan y &= b/a\end{aligned}$$

$$H^2 = a^2 + b^2$$

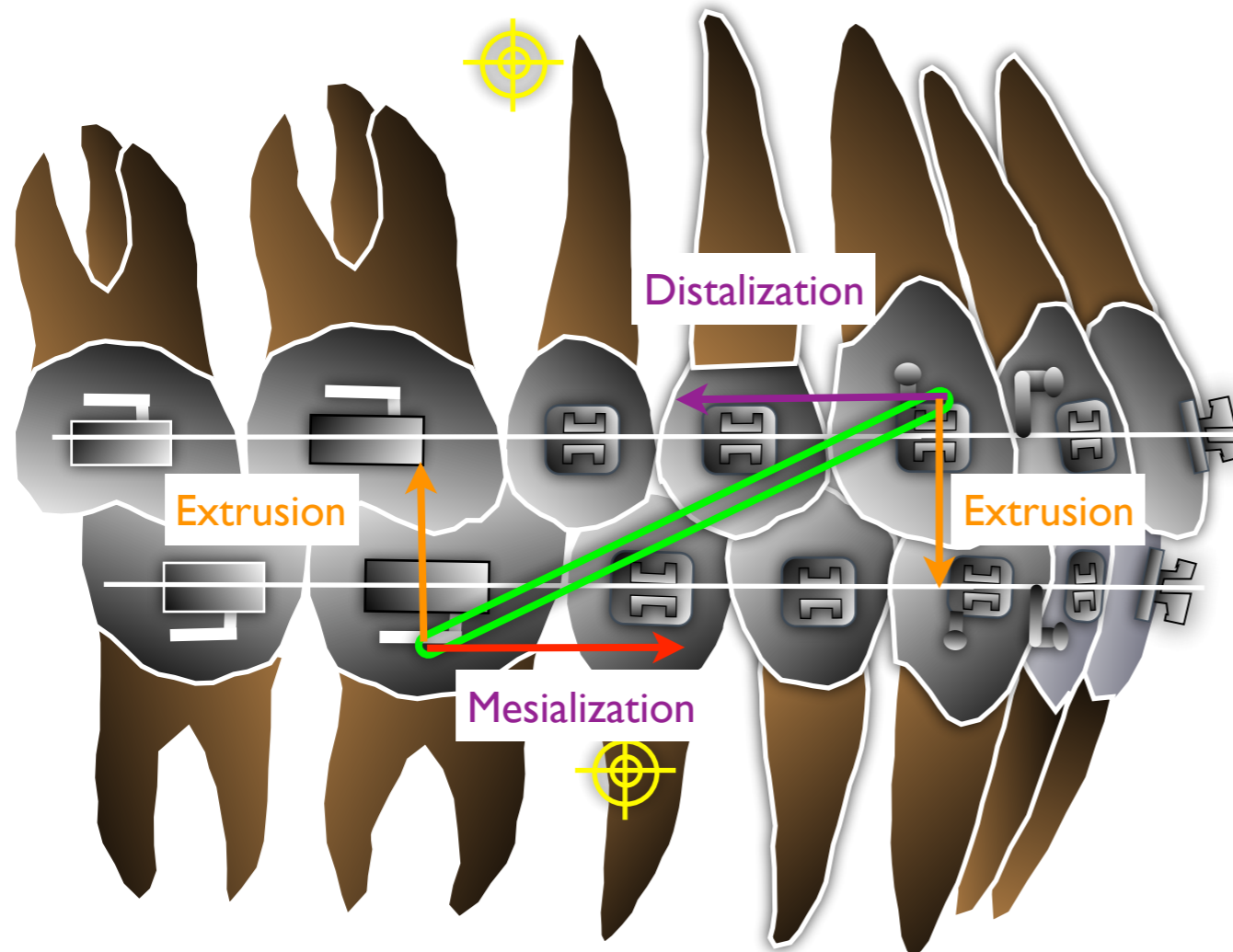


# Vector Decomposition

is a method to decomposed a force into component along the X,Y,Z axes

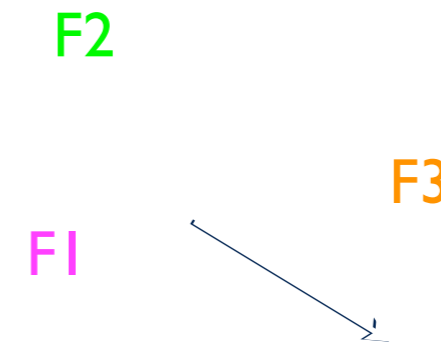
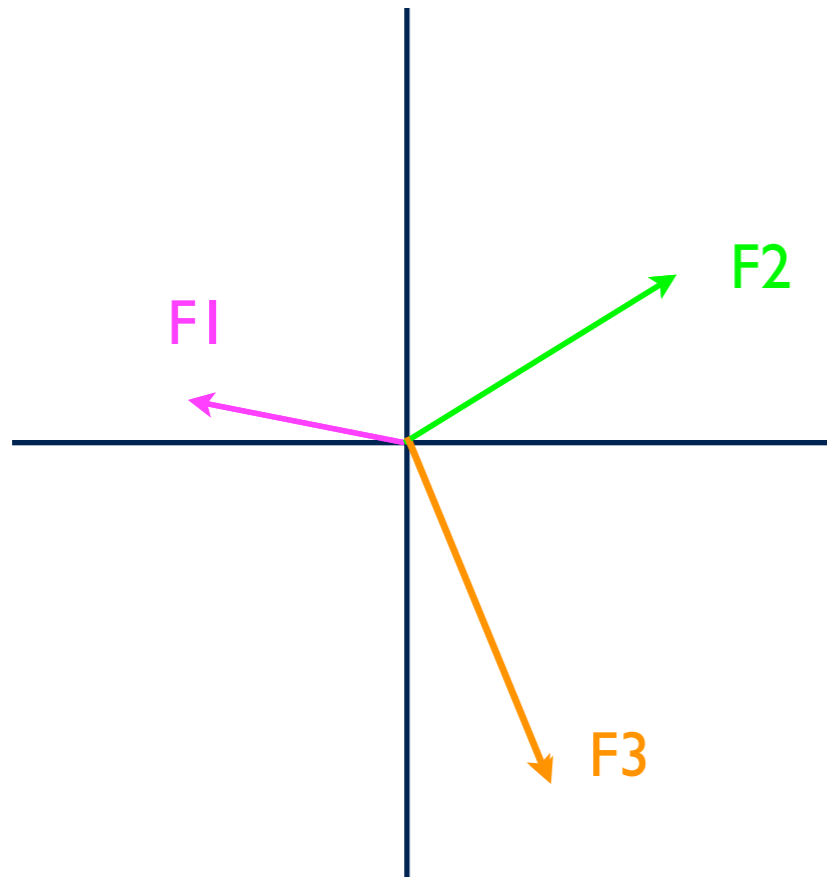


# Handling force in orthodontic



Clinically, the determination of the horizontal, vertical, and transverse component of a force can help the understanding of the direction of tooth movement

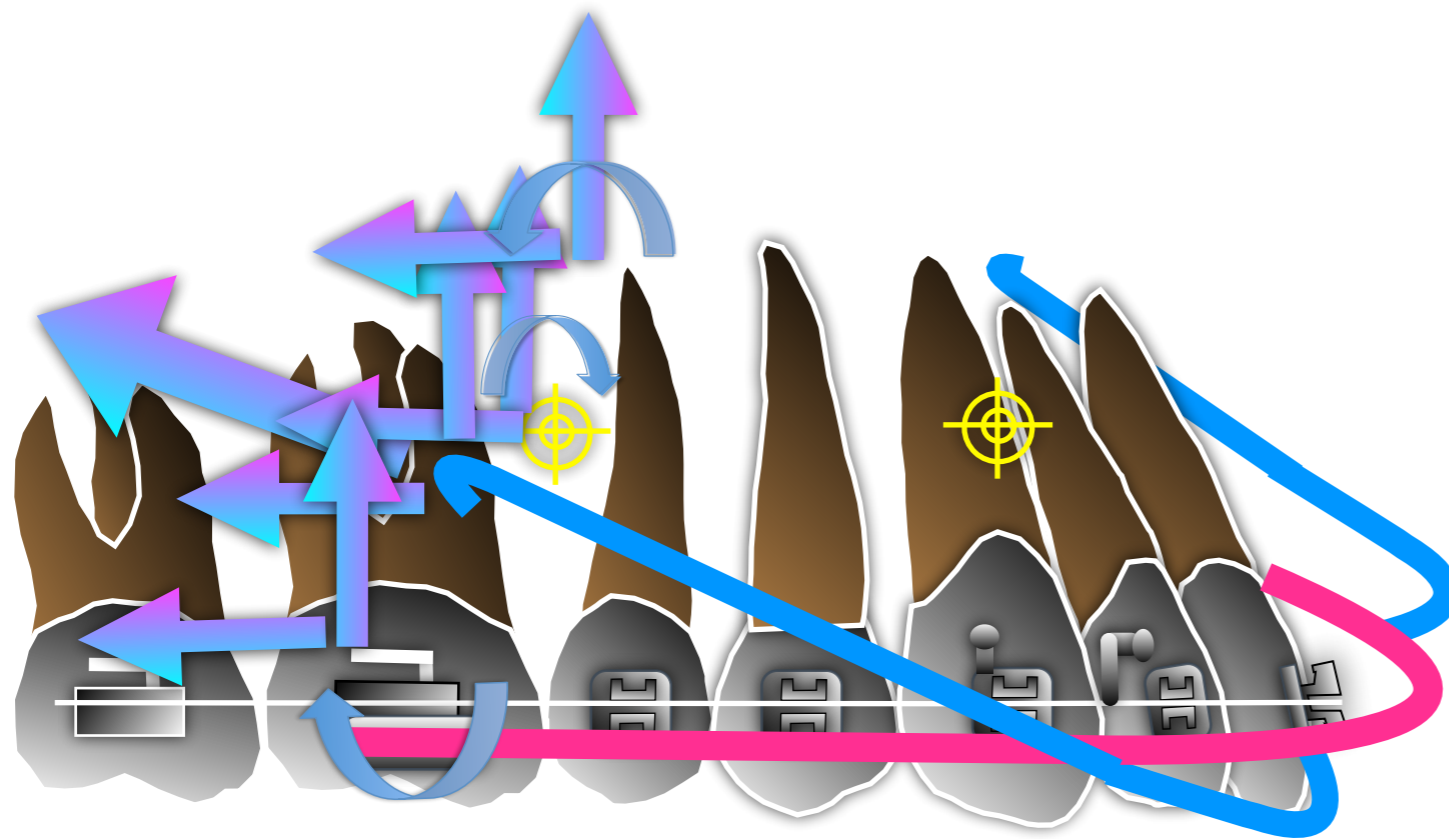
# Determination of Resultant Force



Resultant is not coincide with any force  
(Magnitude, Point of application, Direction)

- Magnitude of force (Scalar) = the length of the line
- Point of Application = Center
- Direction (line of force)





line of force  
composed and decomposed vectors

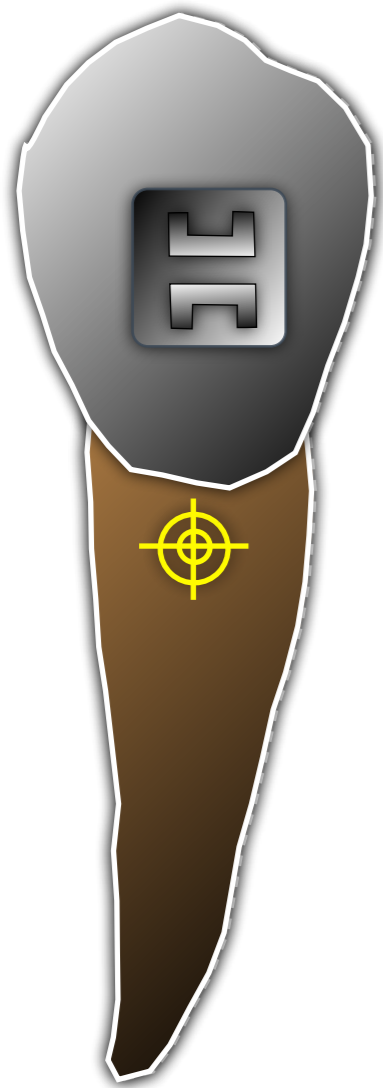
## Type of Tooth Movement in Term of **mechanic**

- Translation : Force passing through CR produces all points of the tooth move an equal distance in the same direction.
- Pure Rotation : Movement of all points around the CR as being a center of circle ( Couple)
- Combination : Not pure rotation and pure translation

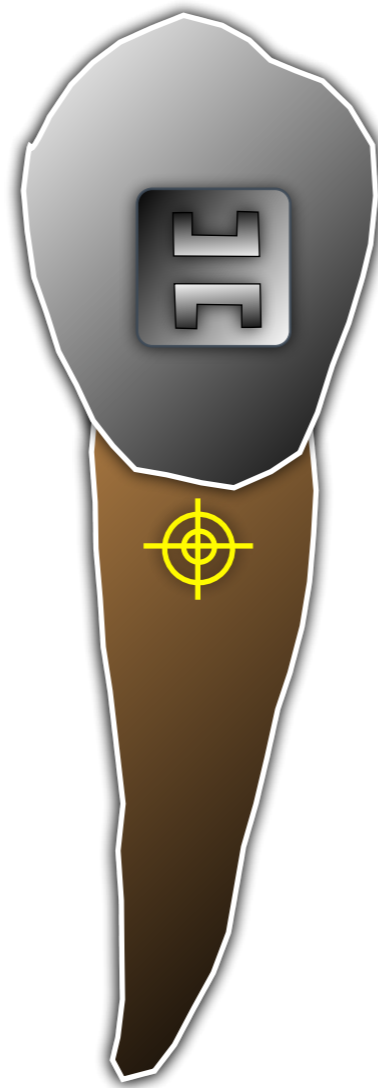




# Type of Tooth Movement in Biomechanic Term



Translation

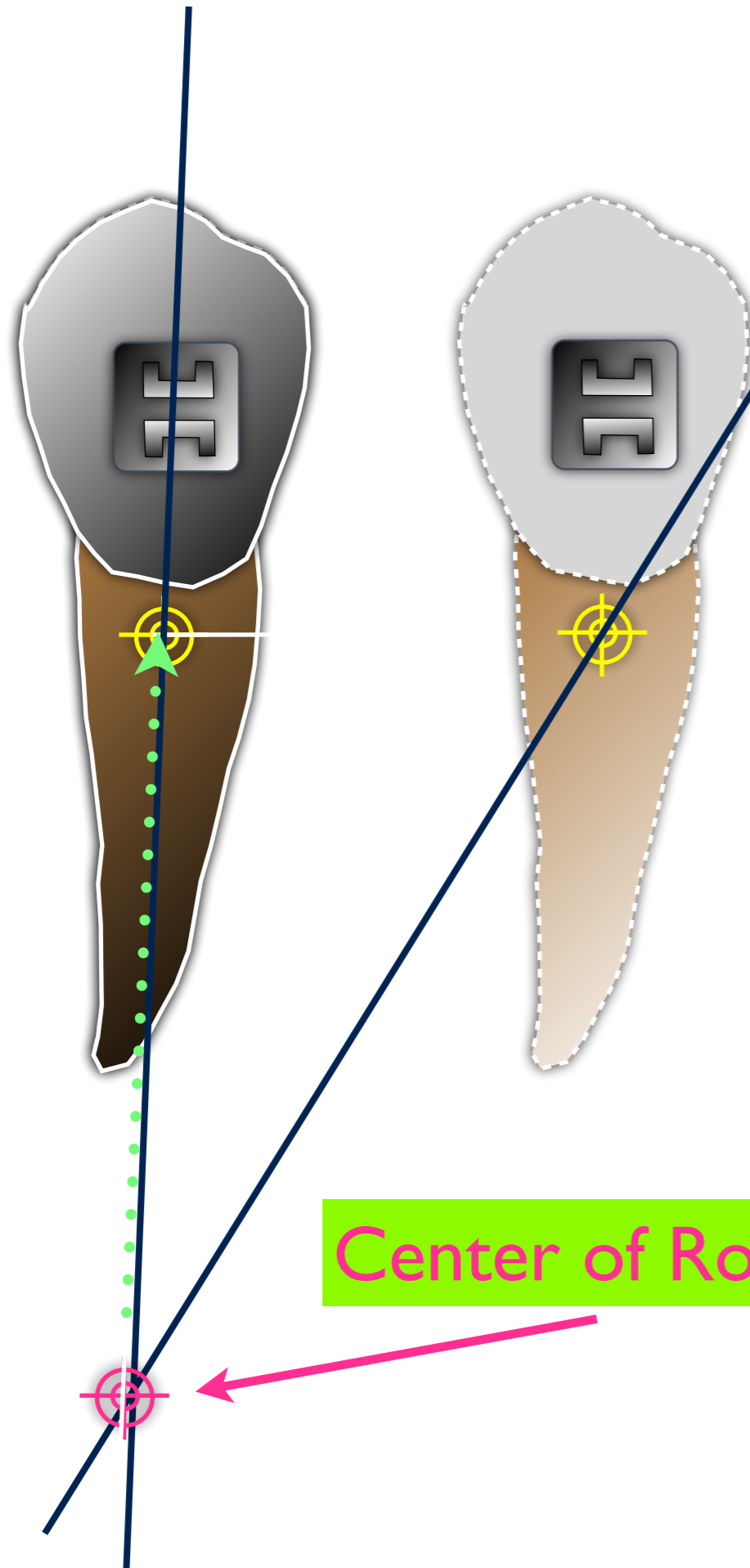


Pure Rotation



Combination

# Center of Rotation

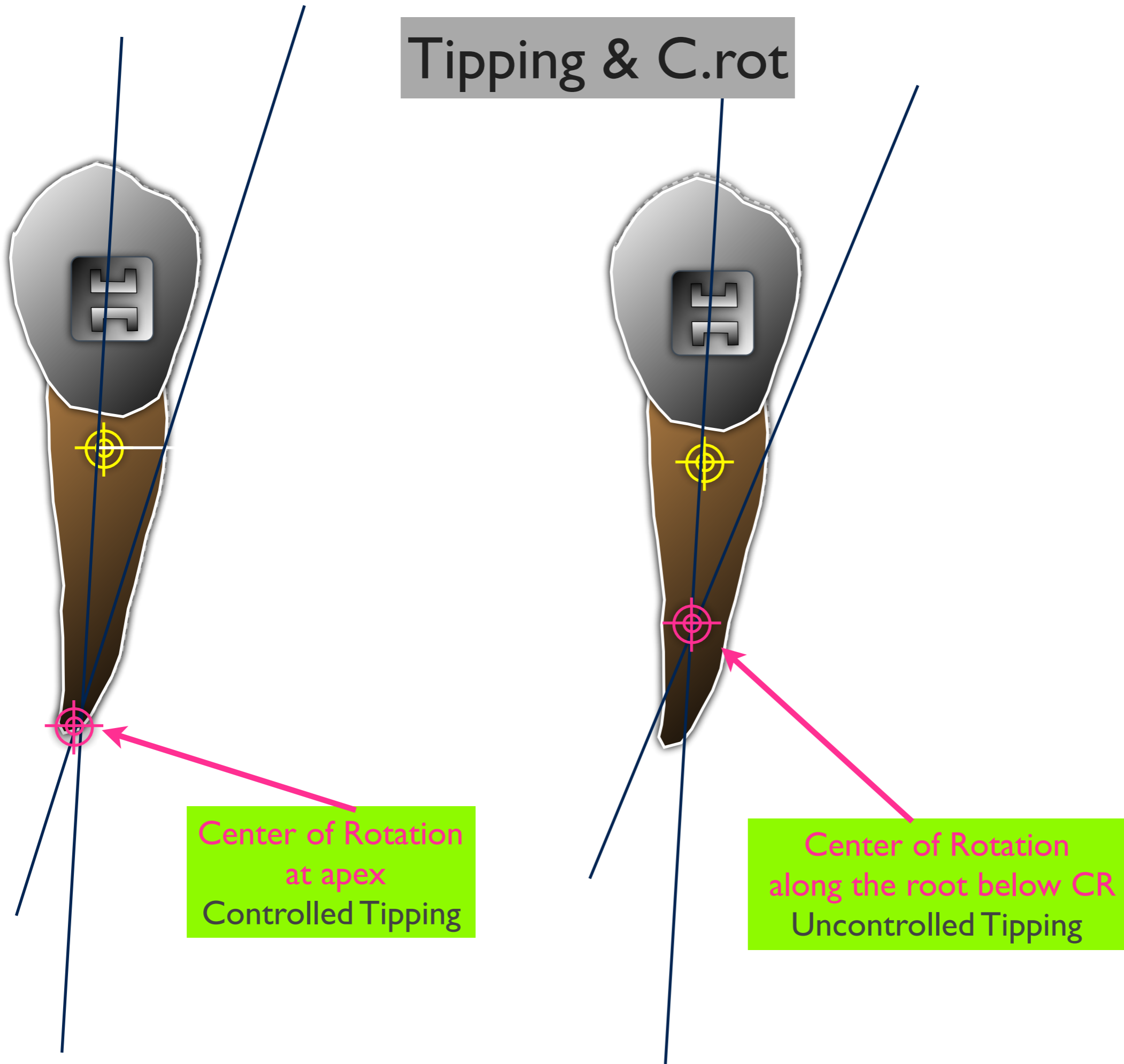


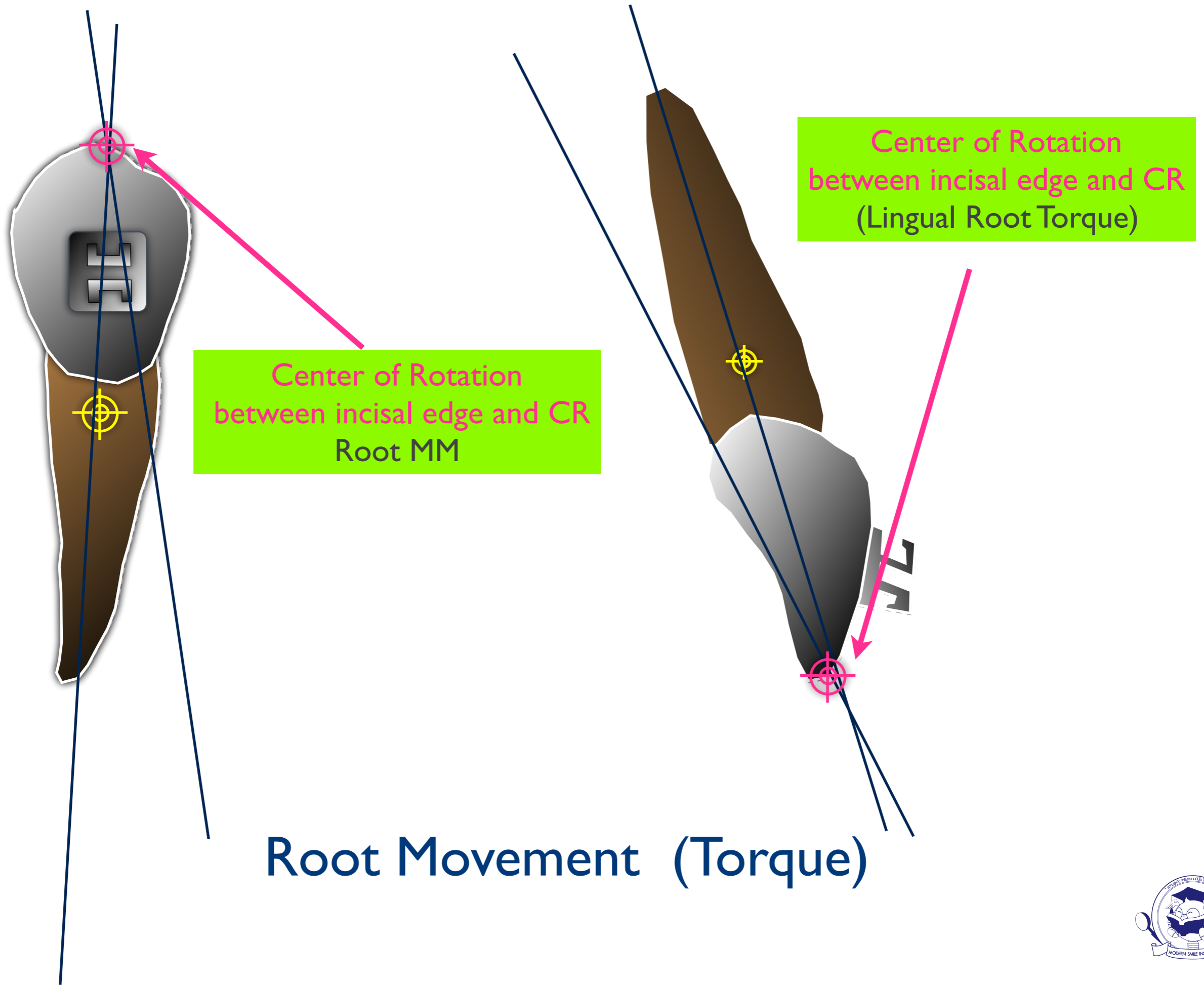
Combination of pure rotation and translation usually occurs in orthodontic clinic, therefore, there must be the exact point to determine type of tooth movement which is the center of rotation

Movement of points of the tooth along the arc of a circle. The center of the circle is the center of Rotation

Center of Rotation

# Tipping & C.rot



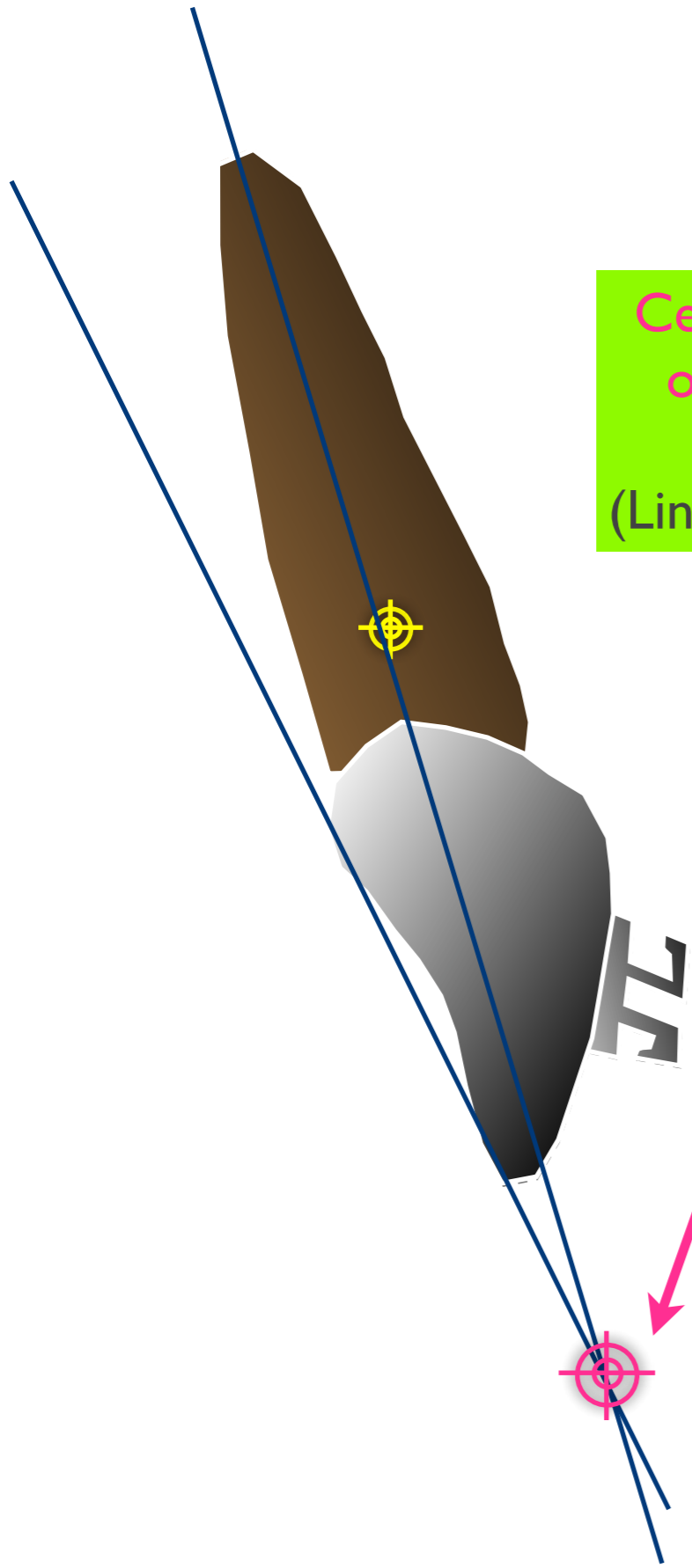


Center of Rotation  
between incisal edge and CR  
Root MM

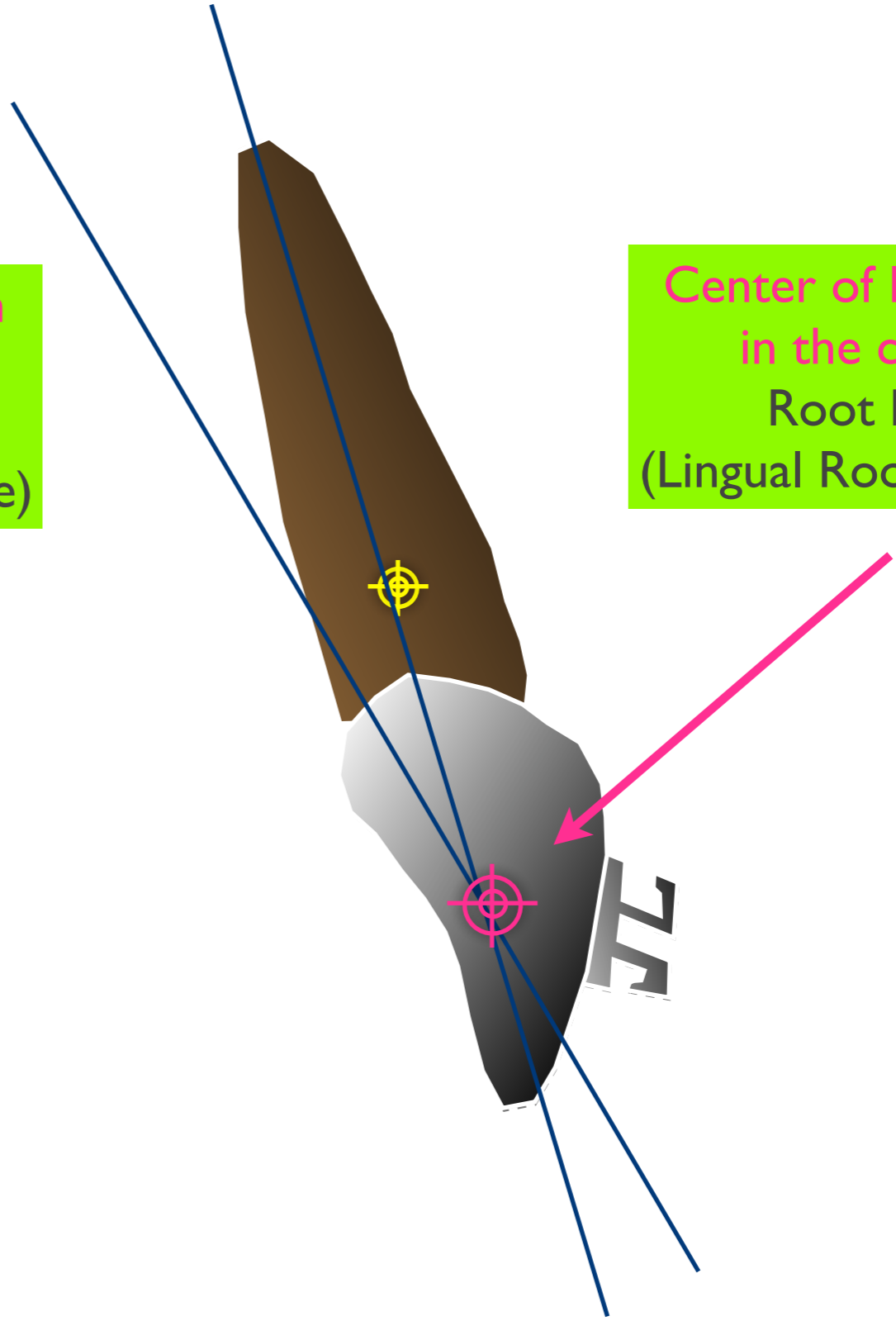
Center of Rotation  
between incisal edge and CR  
(Lingual Root Torque)

# Root Movement (Torque)

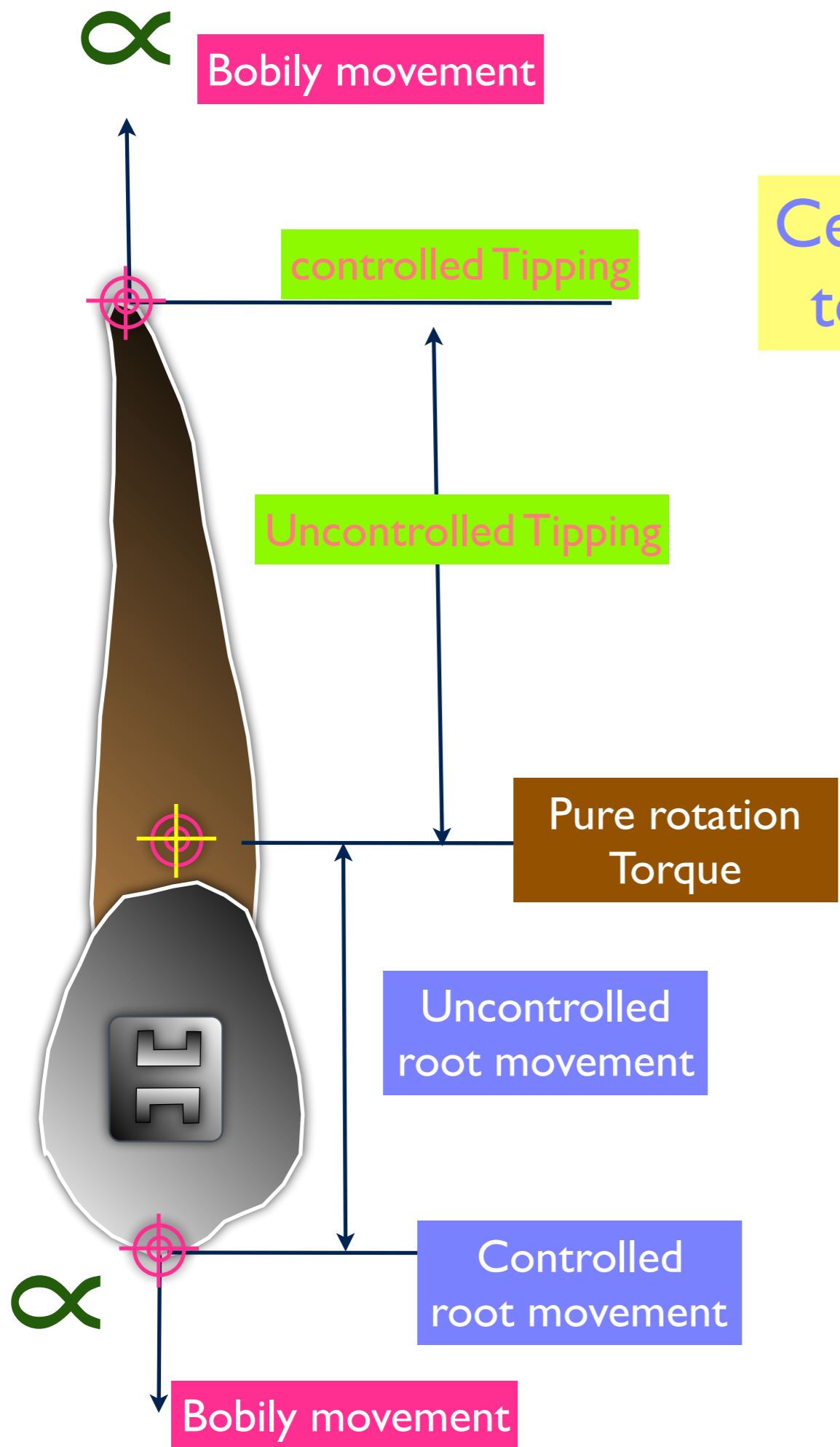
Center of Rotation  
out of the crown  
Root MM  
(Lingual Root Torque)



Center of Rotation  
in the crown  
Root MM  
(Lingual Root Torque)



# Center of Rotation (C.rot) and type of tooth MM. in Term of Orthodontics





# Clinical implication for C.rot

- determined from its initial and final position
- can be at any position on or off a tooth
- can be used to describe type of tooth movement

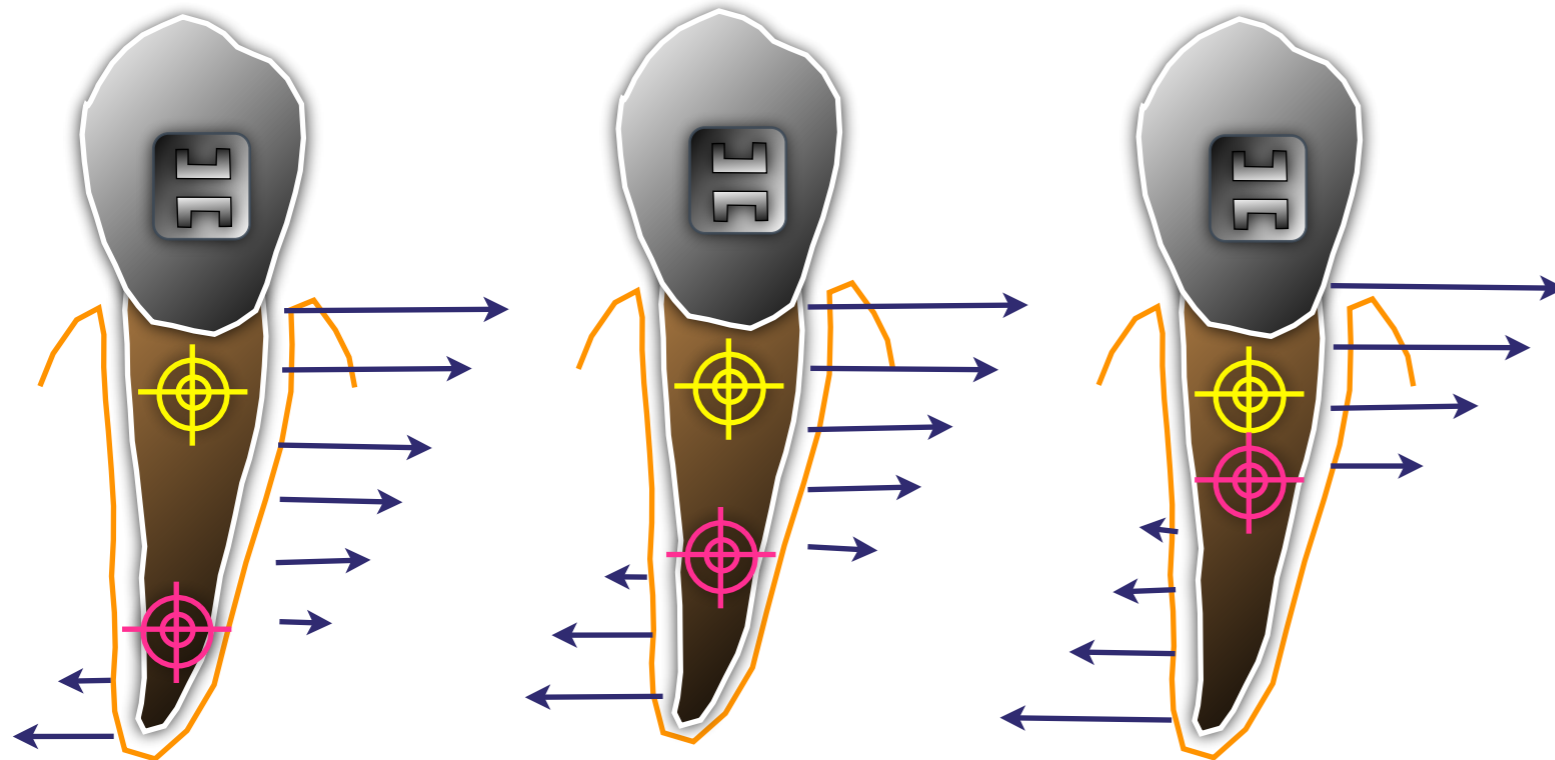


# Types of object movement (position of C.rot) in Orthodontic term Vs Biomechanics term

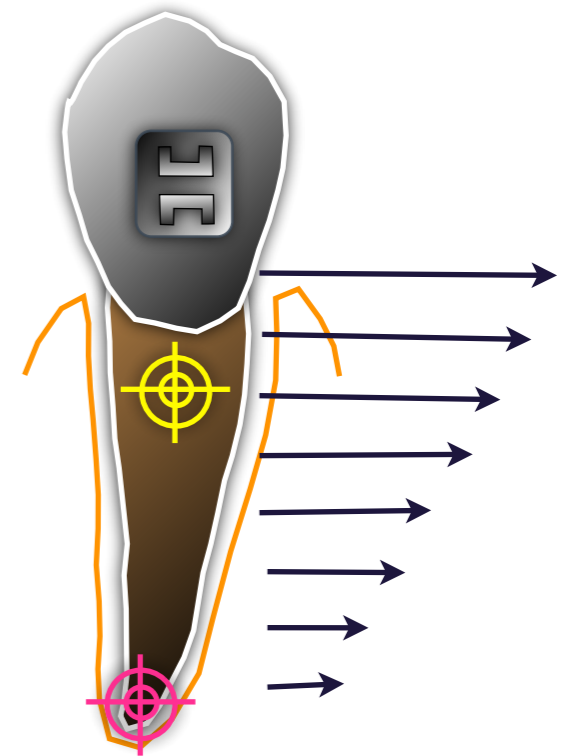
Position of C.rot	Biomechanic	Orthodontic
Infinity	Translation	Bodily MM
Apex	Tipping	controlled Tipping
Apical to CR	Combination	Uncontrolled Tipping
CR	Pure Rotation, Couple	1st, 2nd, 3rd order bend (Toe in-out, tipping,artistic bend,Tip back, Torque)
CR - incisal edge	Root MM	Lingual / Buccal Root Torque
Incisal edge	Root MM	Lingual / Buccal Root Torque

# Tipping

Crown MM. is greater than root MM.

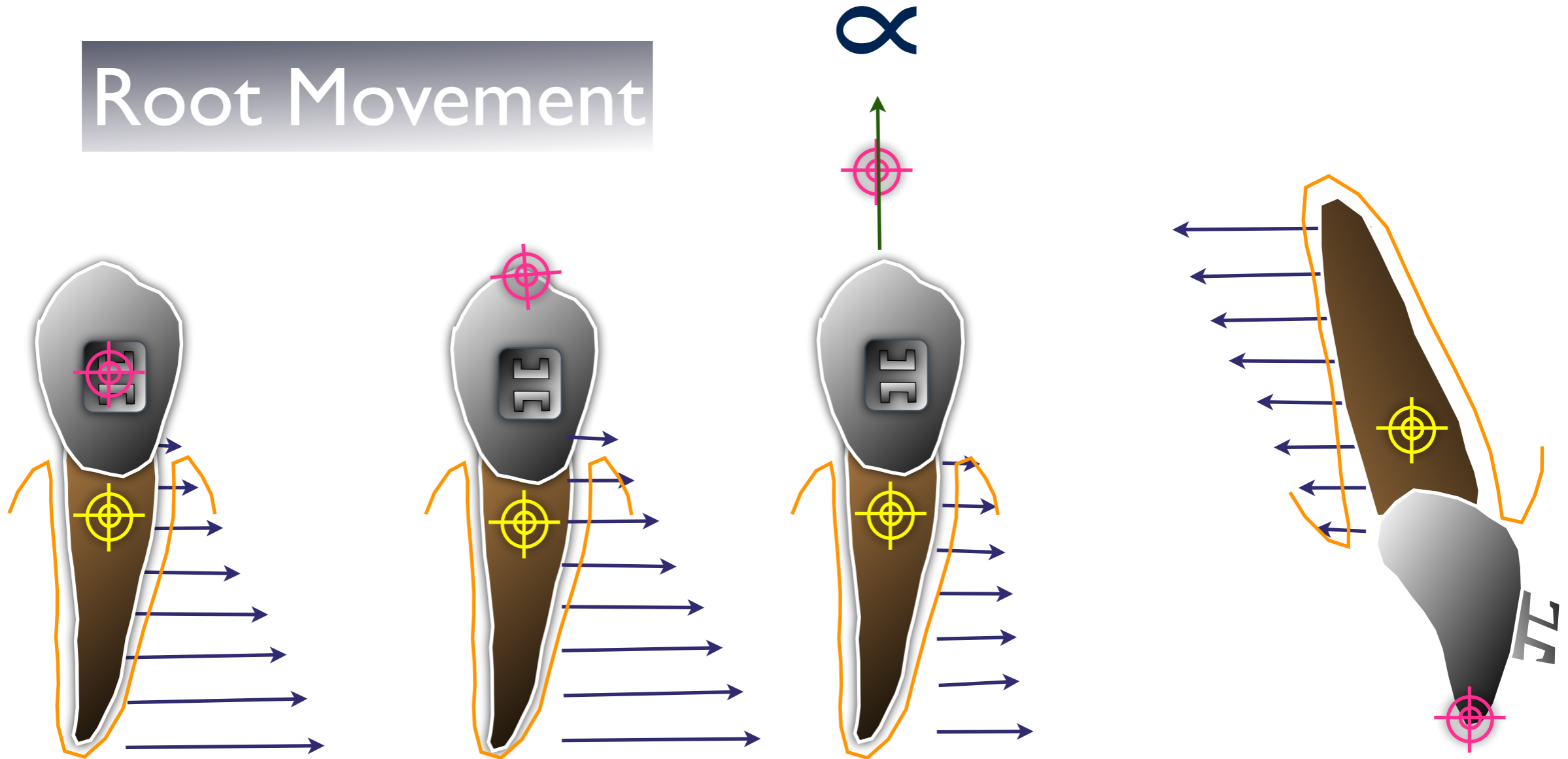


**Uncontrolled Tipping**



**Controlled Tipping**

# Root Movement

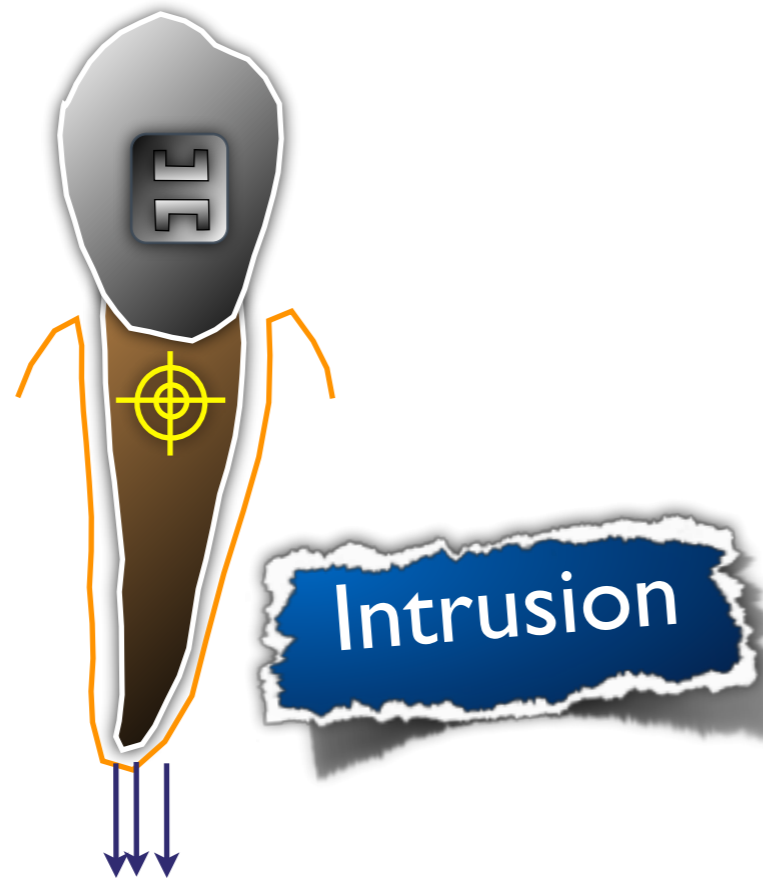


Root MM. is greater than crown MM.

Root movement must be manipulated carefully if inevitable to avoid root resorption



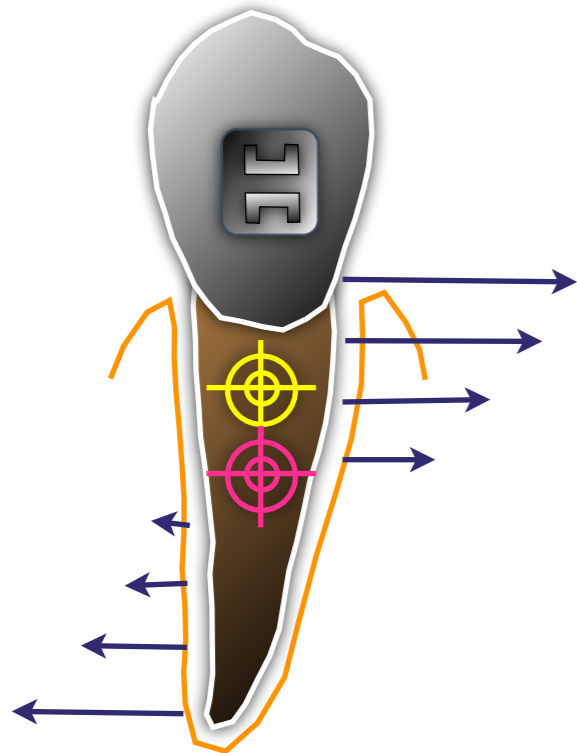
# Tooth movement in vertical plane



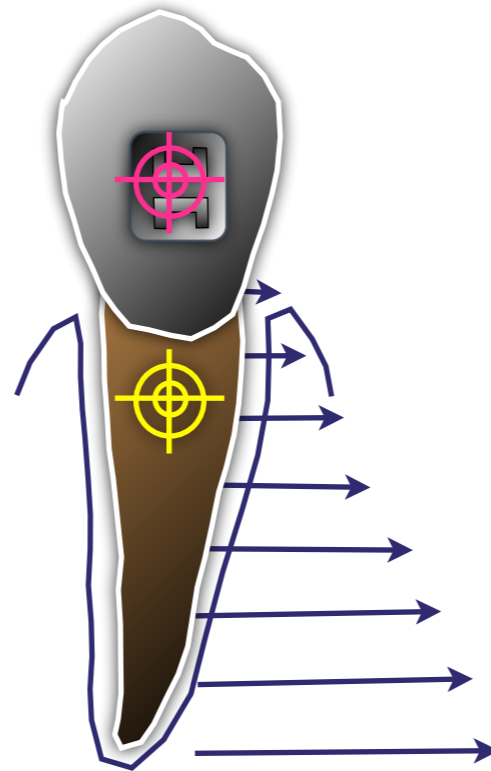
must be manipulated carefully if inevitable to avoid root resorption

is the easiest type of tooth movement to occur

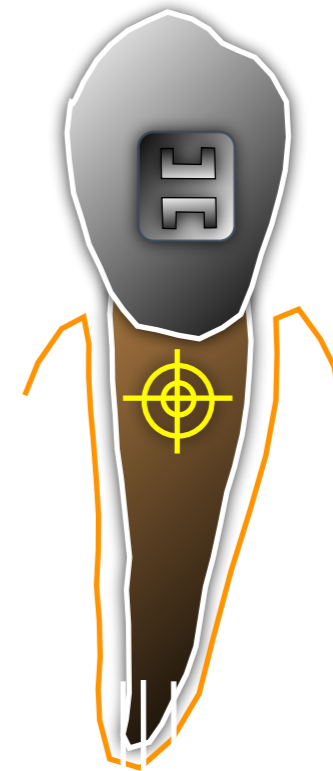
# Why is the type of tooth movement so important ?



Uncontrolled Tipping



Root Movement



Intrusion

-Root resorption  
-Root pinching out  
cortical bone



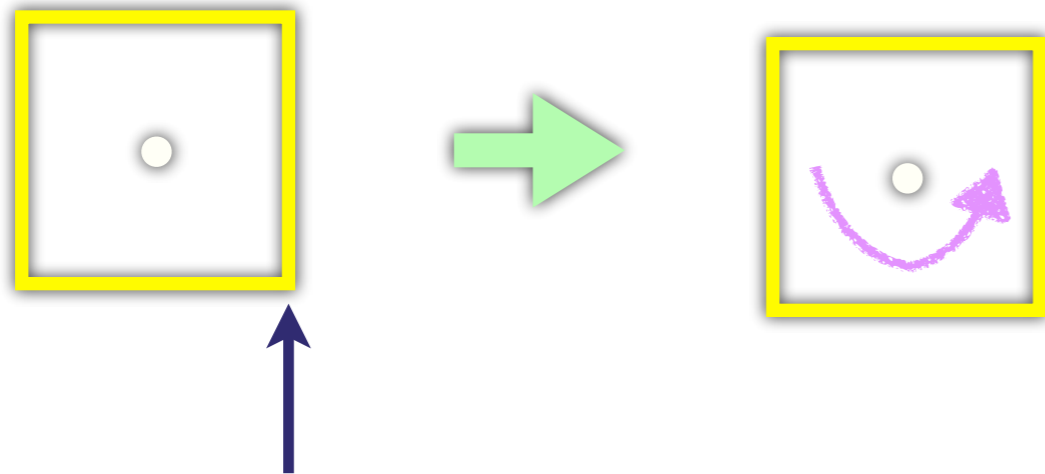
Very  $\mu\text{mm}$   
Light Force

# Moment of Force Vs Moment of Couple

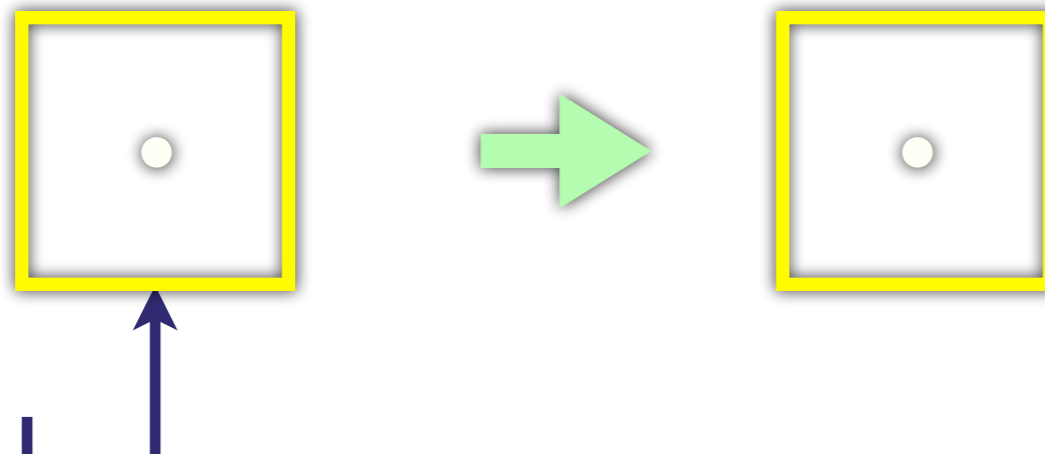
- Moment of force ( $M_f$ ): Magnitude of single force not parallel through CR  $\times$  perpendicular distance from the line of action to CR. ( C.rot is at anywhere)
- Couple force : Consists of 2 forces of equal magnitude with parallel but non-collinear lines of action and opposite senses
- Moment of couple ( $M_c$ ): Magnitude of one of the forces  $\times$  the perpendicular distance between them ( $C_{rot} = CR$ )



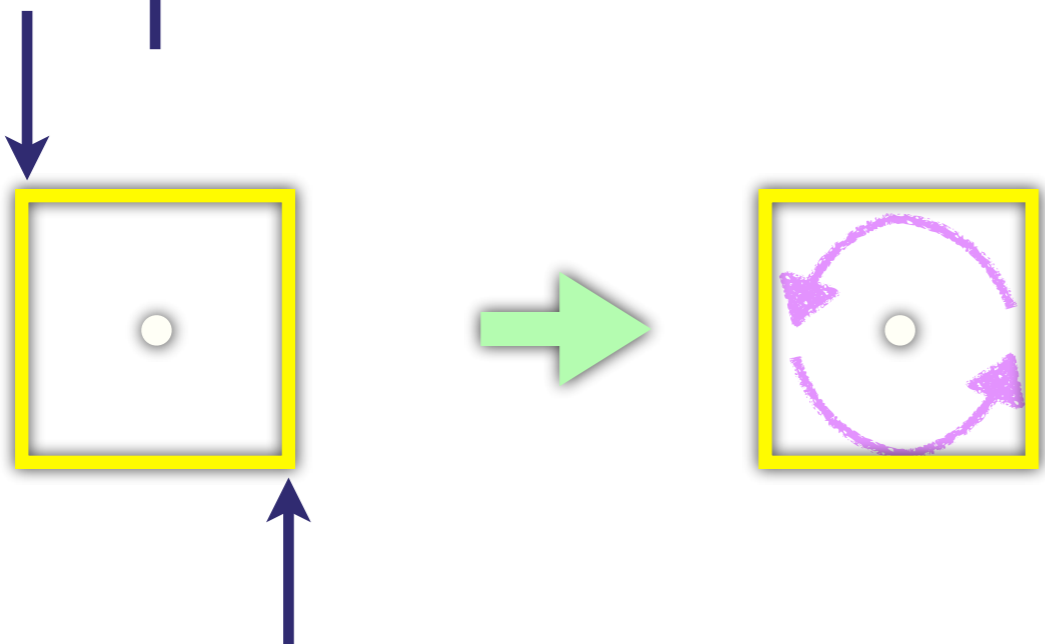
# Moment of Force Vs Moment of Couple



- Moment of force ( $M_f$ ): Magnitude of single force not parallel through CR X perpendicular distance from the line of action to CR. ( C.rot is at anywhere)



- No Moment of force or Couple

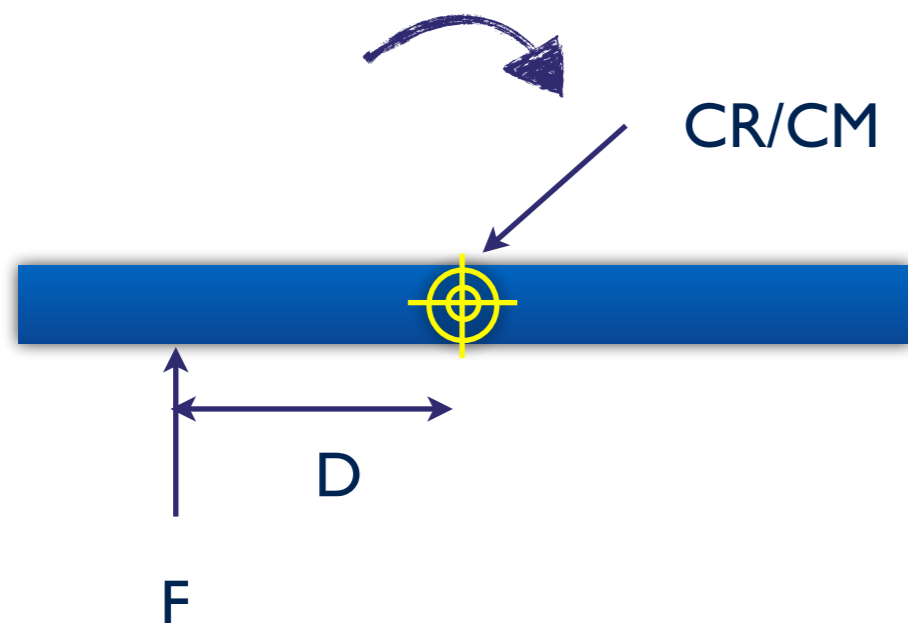
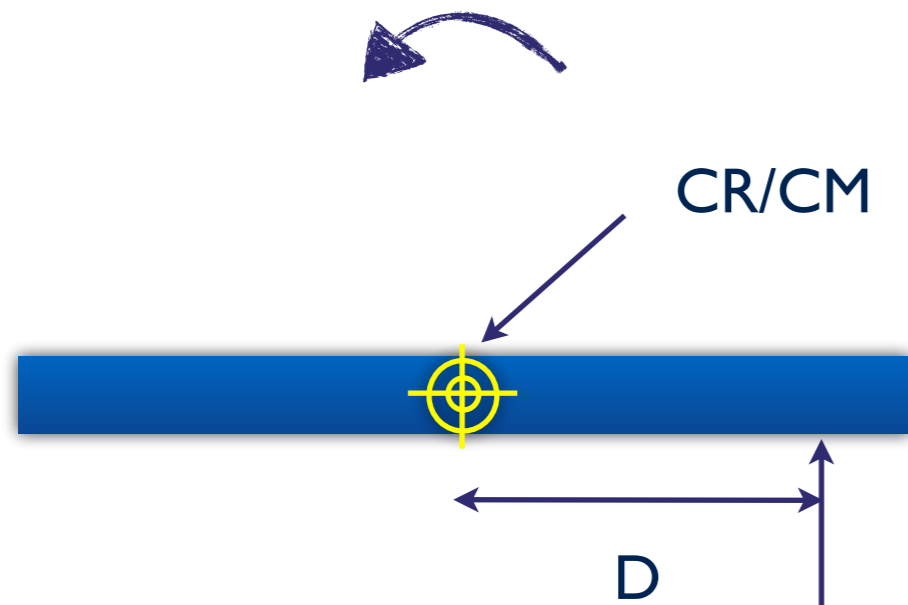


- Couple : Consists of 2 forces of equal magnitude with parallel but non-collinear lines of action and opposite senses



# Moment of force ( $M_f$ )

Magnitude of single force not parallel through CR(CM) X perpendicular distance from the line of action to CR. ( C.rot is at anywhere)



Type of Moment	Moment	Sense	Center of rotation
Moment of Force	Force X Distance ( Newtons - millimeter)	<b>Translation &amp; Counter clockwise</b> rotation	Next to CR at the left side

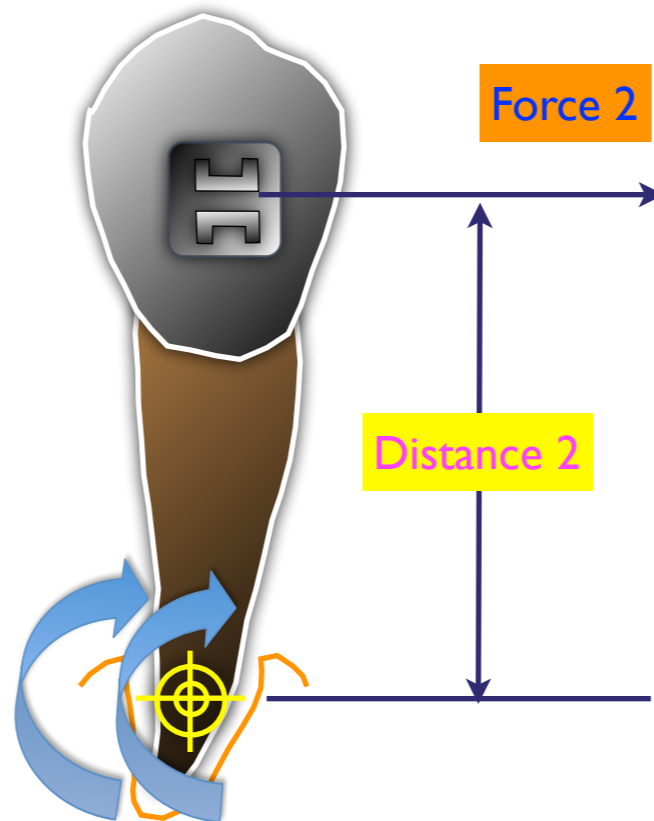
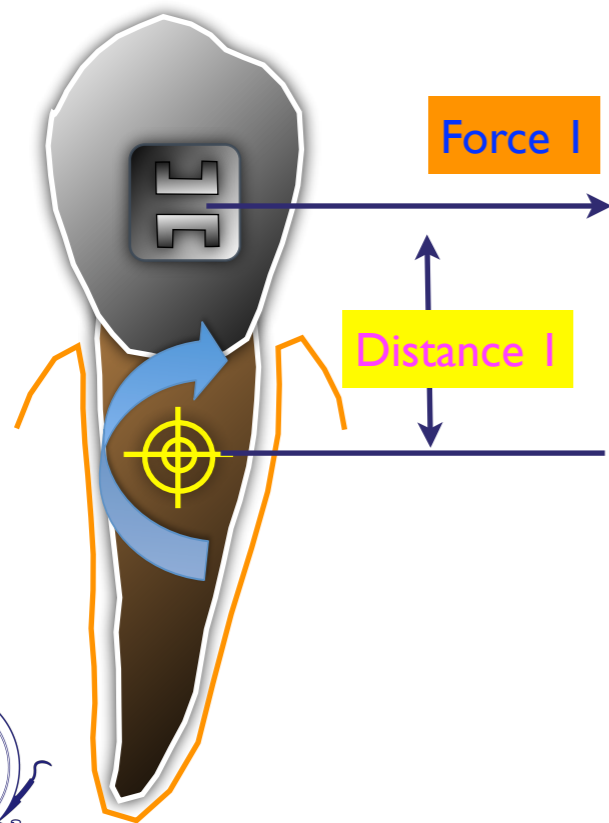
Type of Moment	Moment	Sense	Center of rotation
Moment of Force	Force X Distance ( Newtons - millimeter)	<b>Translation &amp; Clockwise</b> rotation	Next to CR at the right side

# Clinical implication of Moment of force ( $M_f$ )

$$M.f = \text{Force} \times \text{Distance} \quad (\text{Newtons} - \text{millimeter})$$

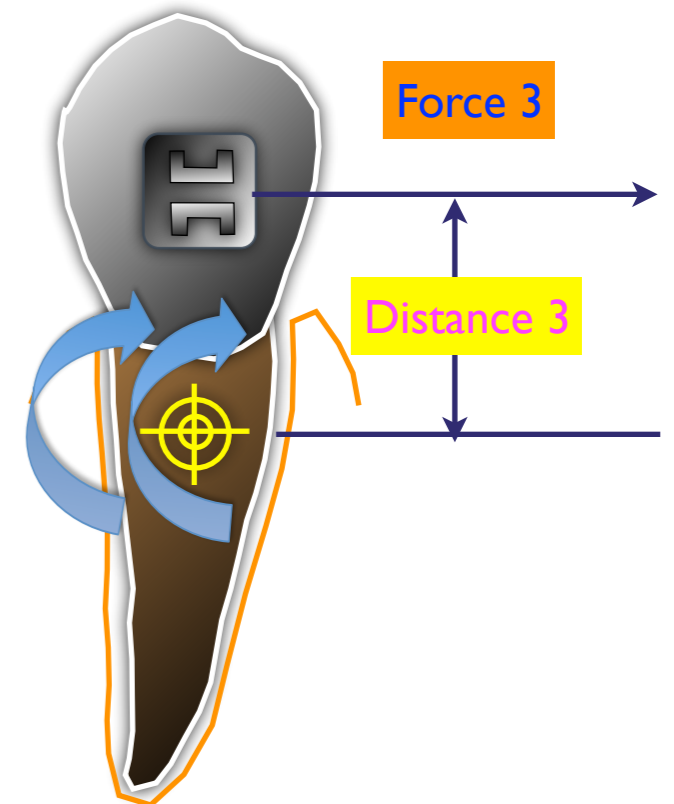
$$F_1 = F_2$$

$$M.f_1 < M.f_2$$



$$F_3 > F_1, D_1 = D_3$$

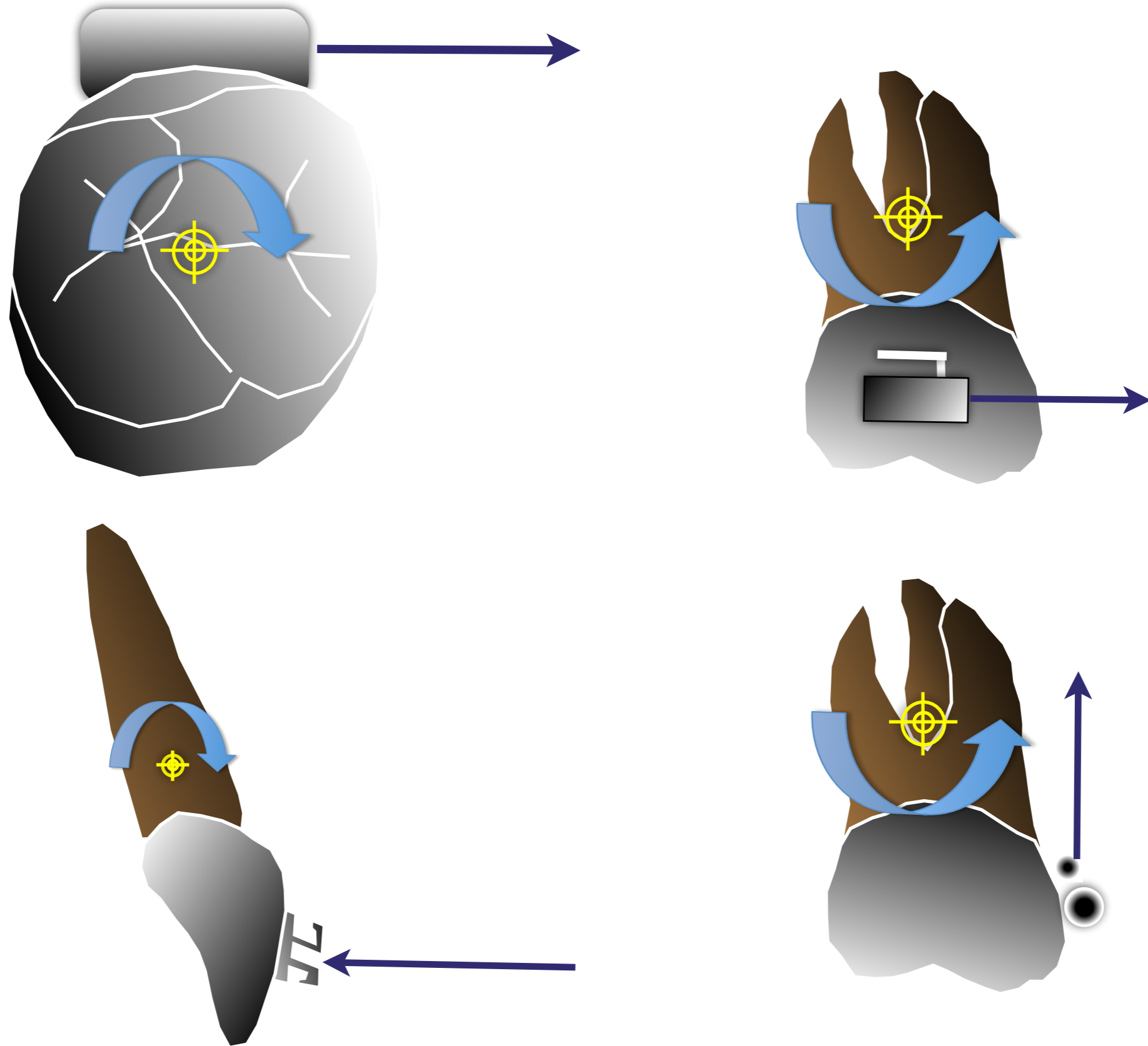
$$M.f_1 < M.f_3$$



Pay very much attention in patient with alveolar bone loss

The more the force, the more the moment of force

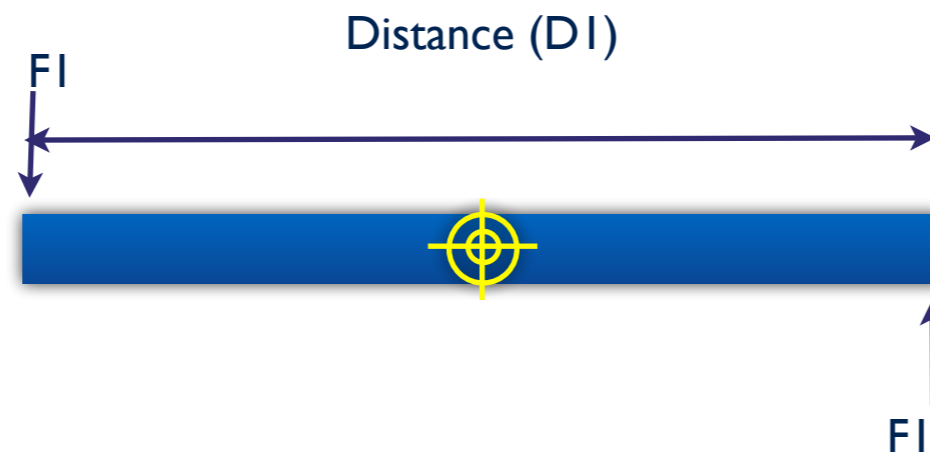
# Moment of force commonly occurred in orthodontic clinic



# Moment of Couple

Two parallel forces of equal magnitude acting in opposite directions and separated by a distance.  
(No translation)

Moment of Couple = Force X Distance (Newtons-mm.)

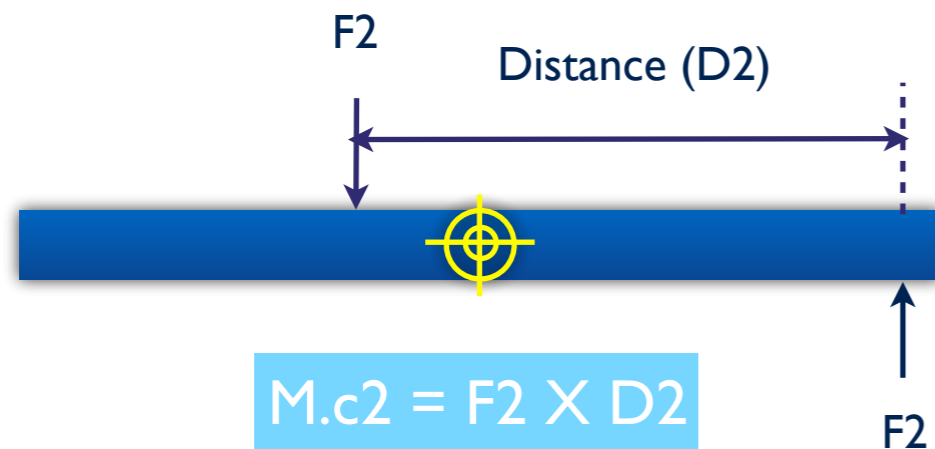


Center of Rotation = The center of resistance = Pure rotation

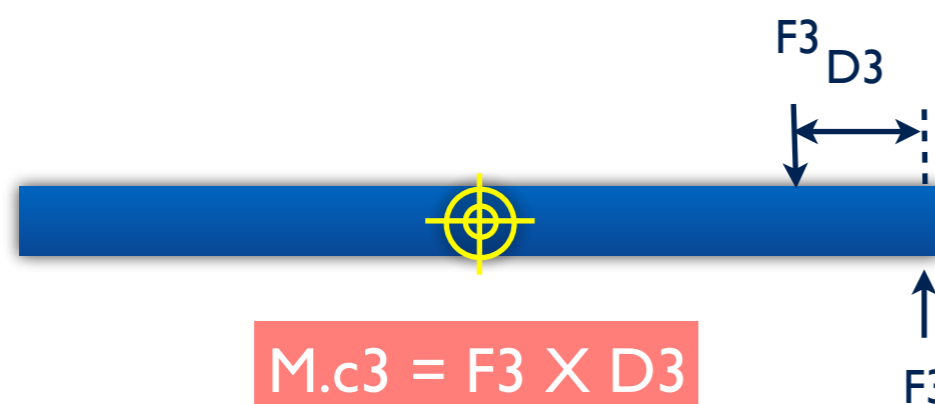
# Moment of Couple



$$M.c1 = F1 \times D1$$



$$M.c2 = F2 \times D2$$



$$M.c3 = F3 \times D3$$

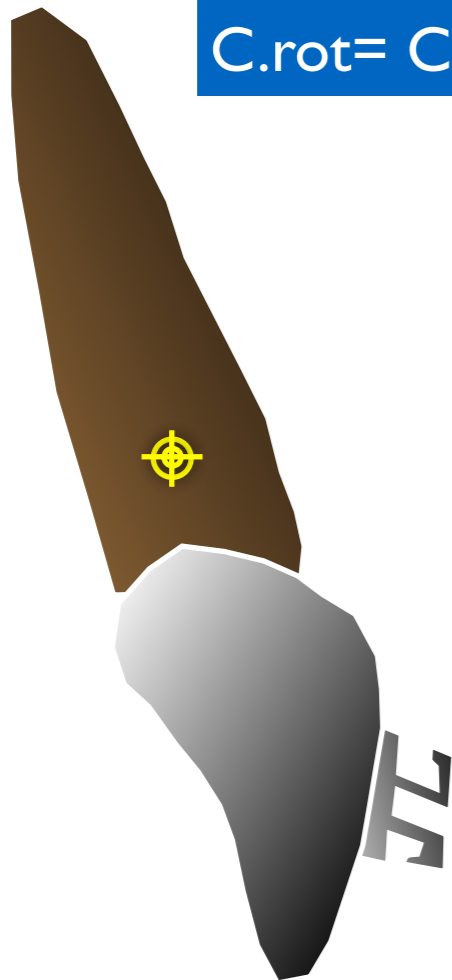
Center of Rotation  
= CR  
= CM

What does it mean?

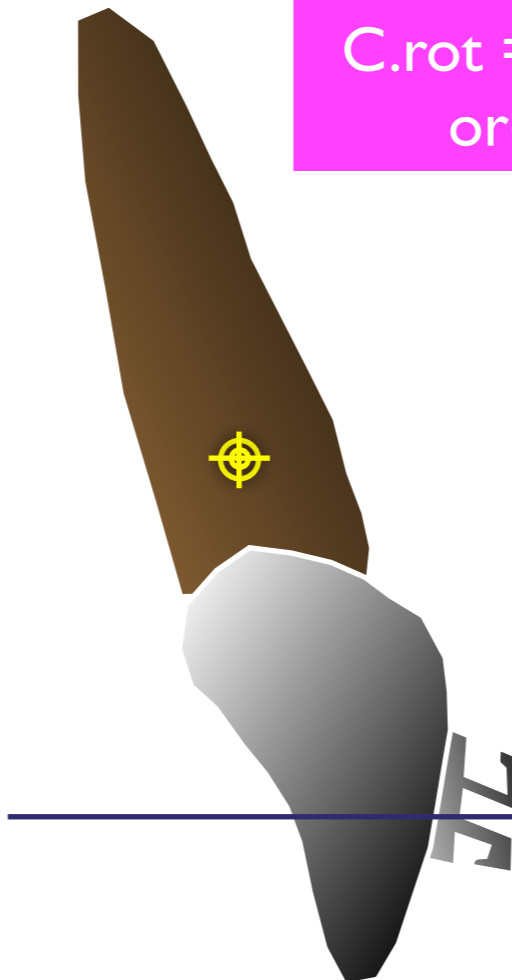
Producing rotation at CR  
regardless of the location of  
forces applied.

# What does we learn from the concept of **Moment of Couple** in **Orthodontics** ?

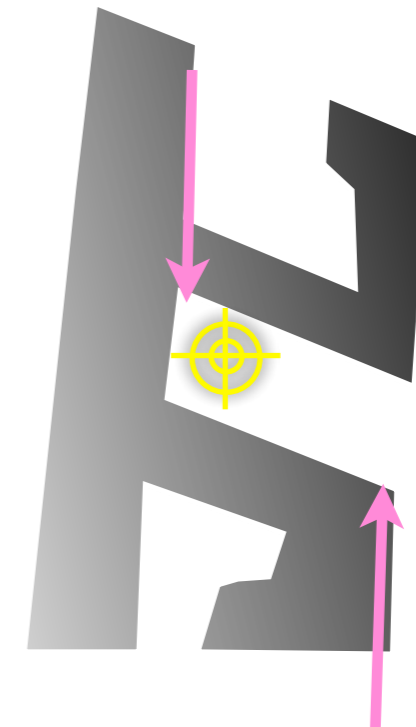
C.rot= CR



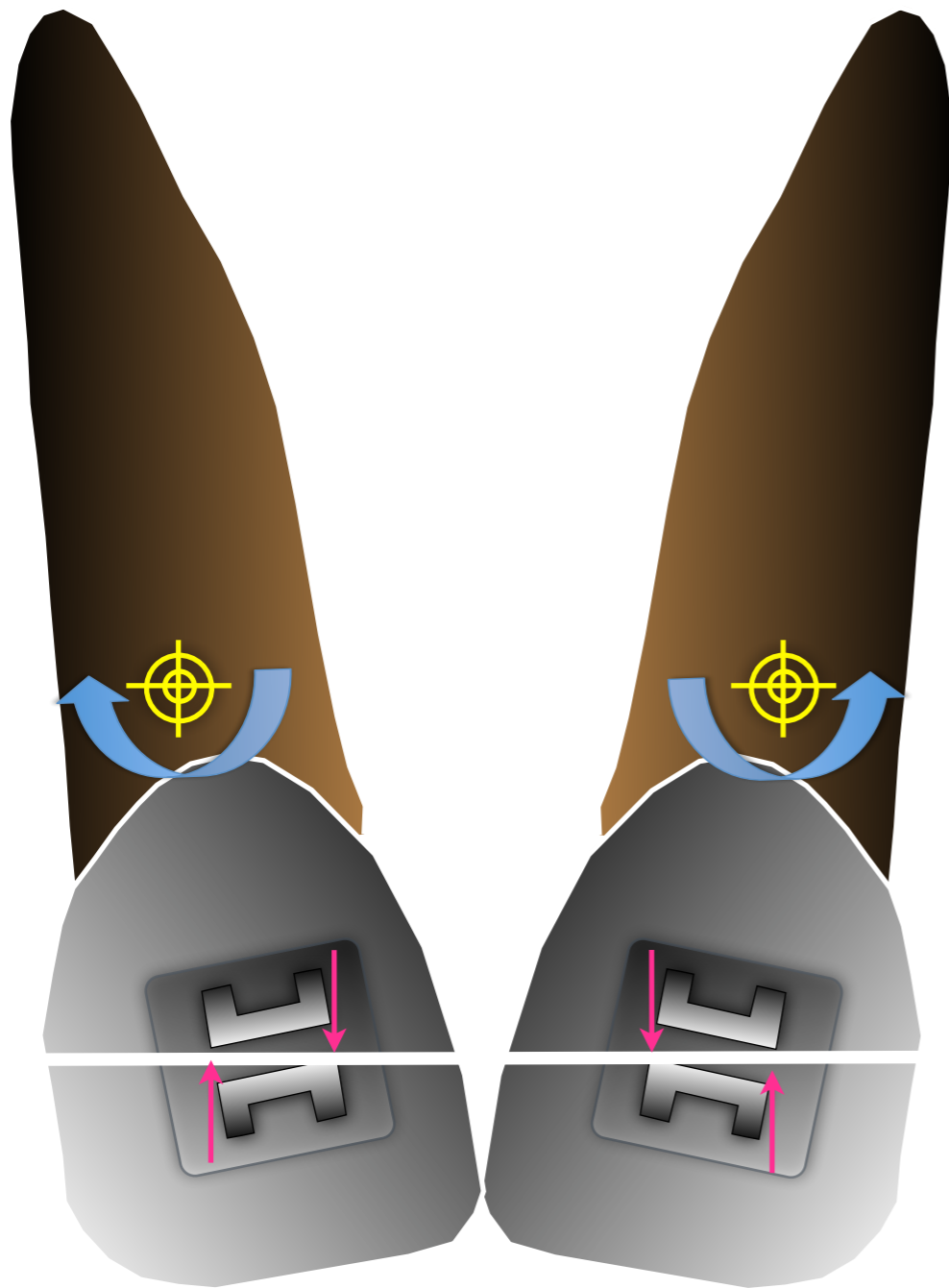
C.rot = Incisal edge  
or=Bracket



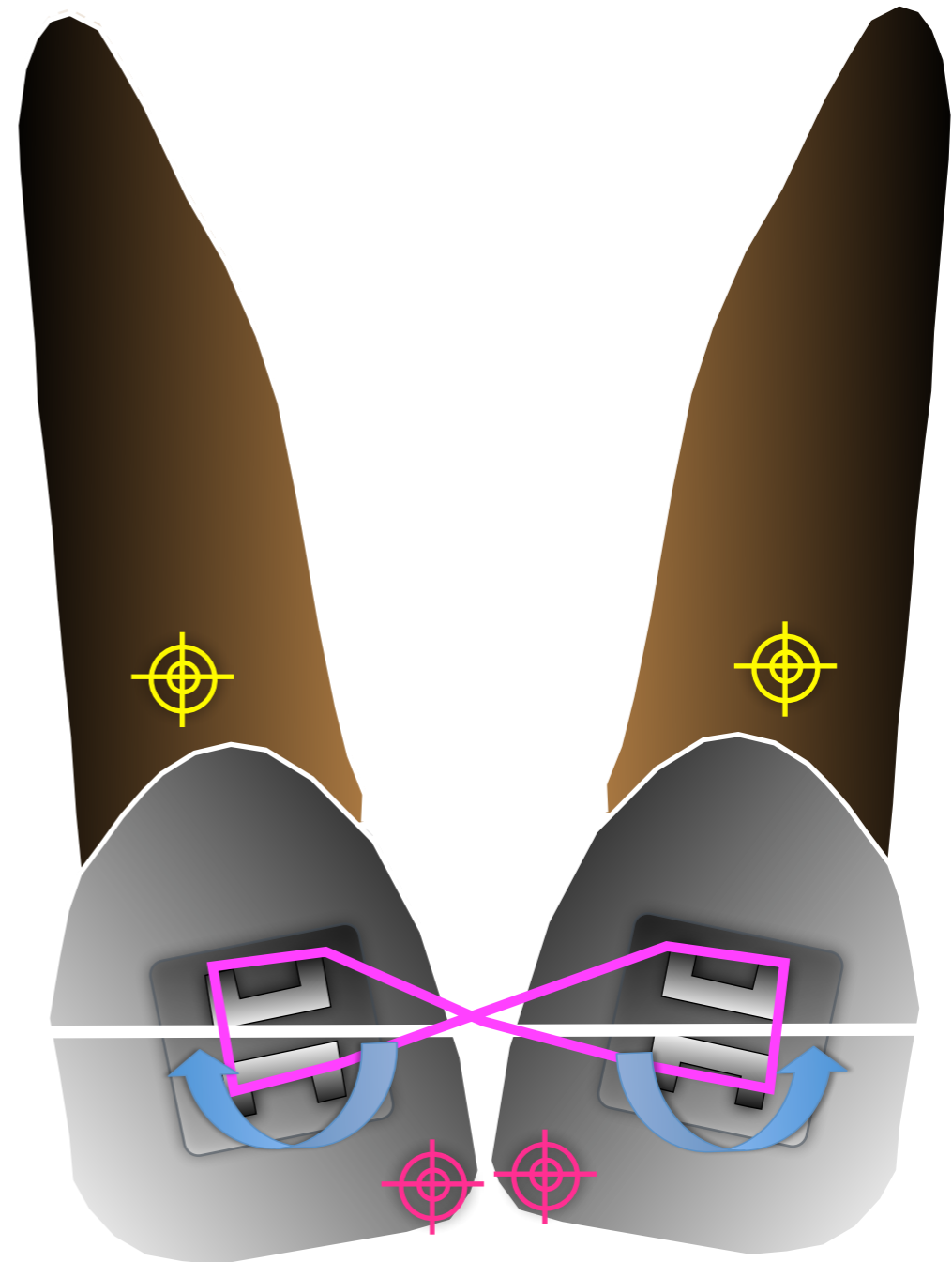
C.rot = C of BKT



The I/I will be proclined when 16 x22 NiTi has been used without enmasse or cinch back in the leveling stage



C.rot = CR

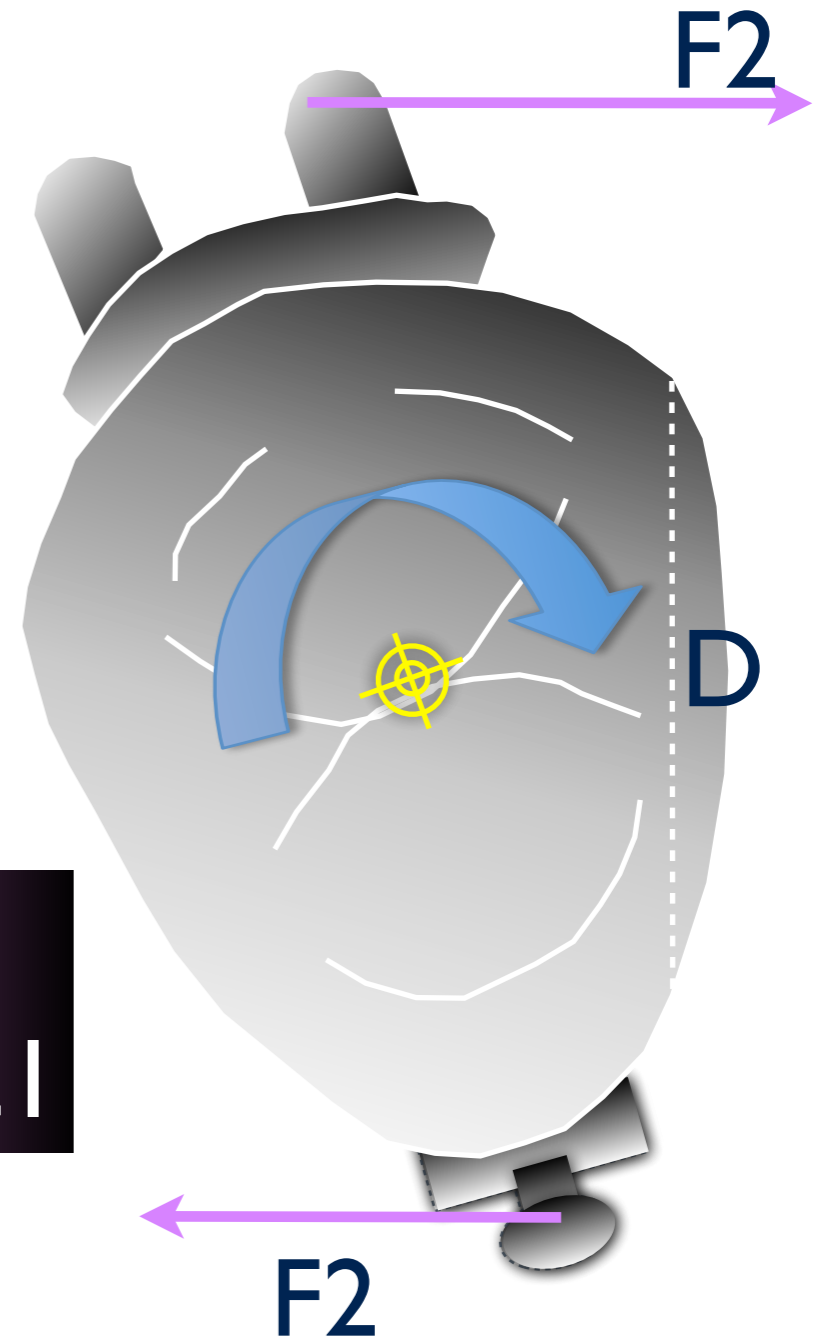
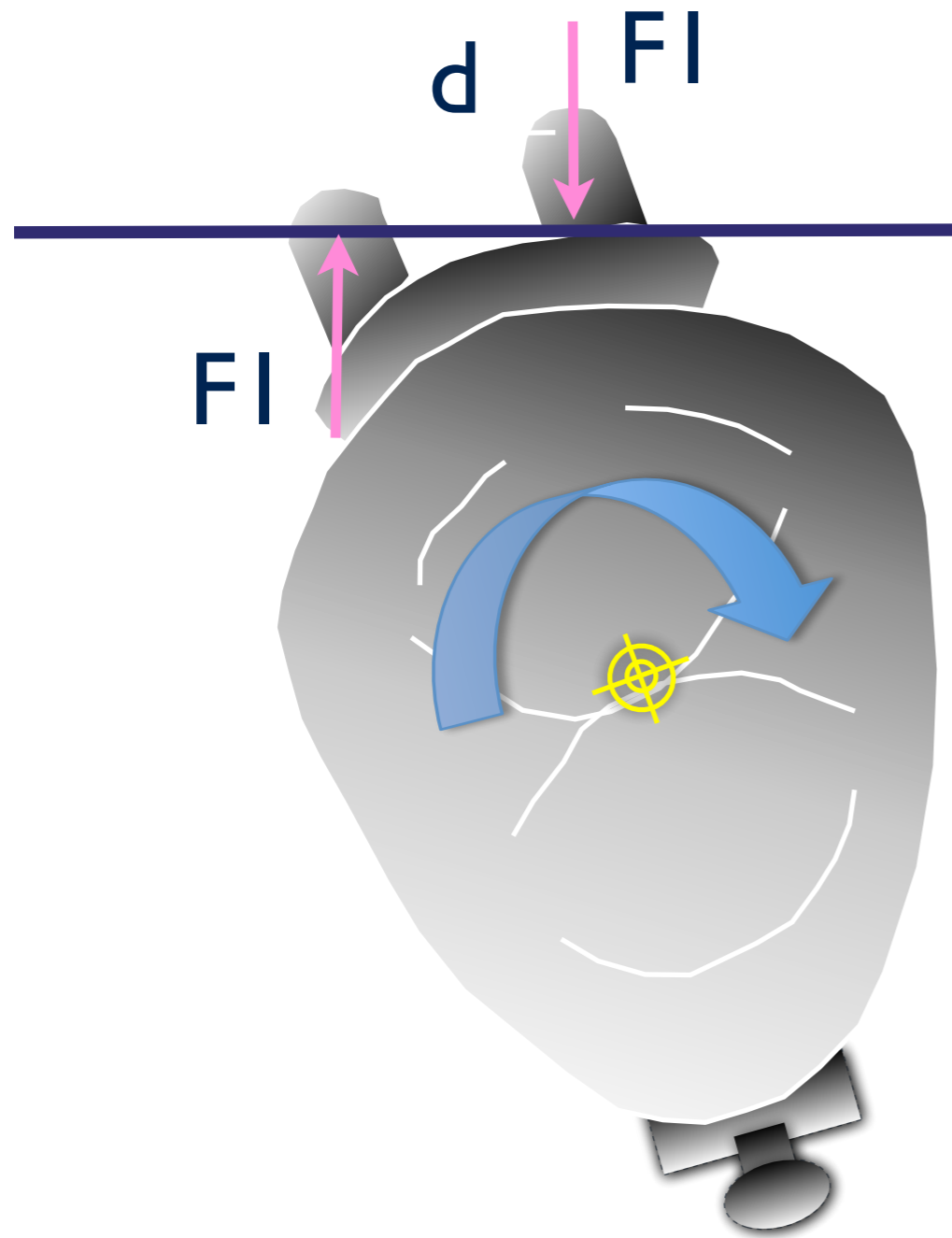


C.rot = incisal edge



$$M.c1 = F1 \times d$$

$$M.c2 = F2 \times D$$

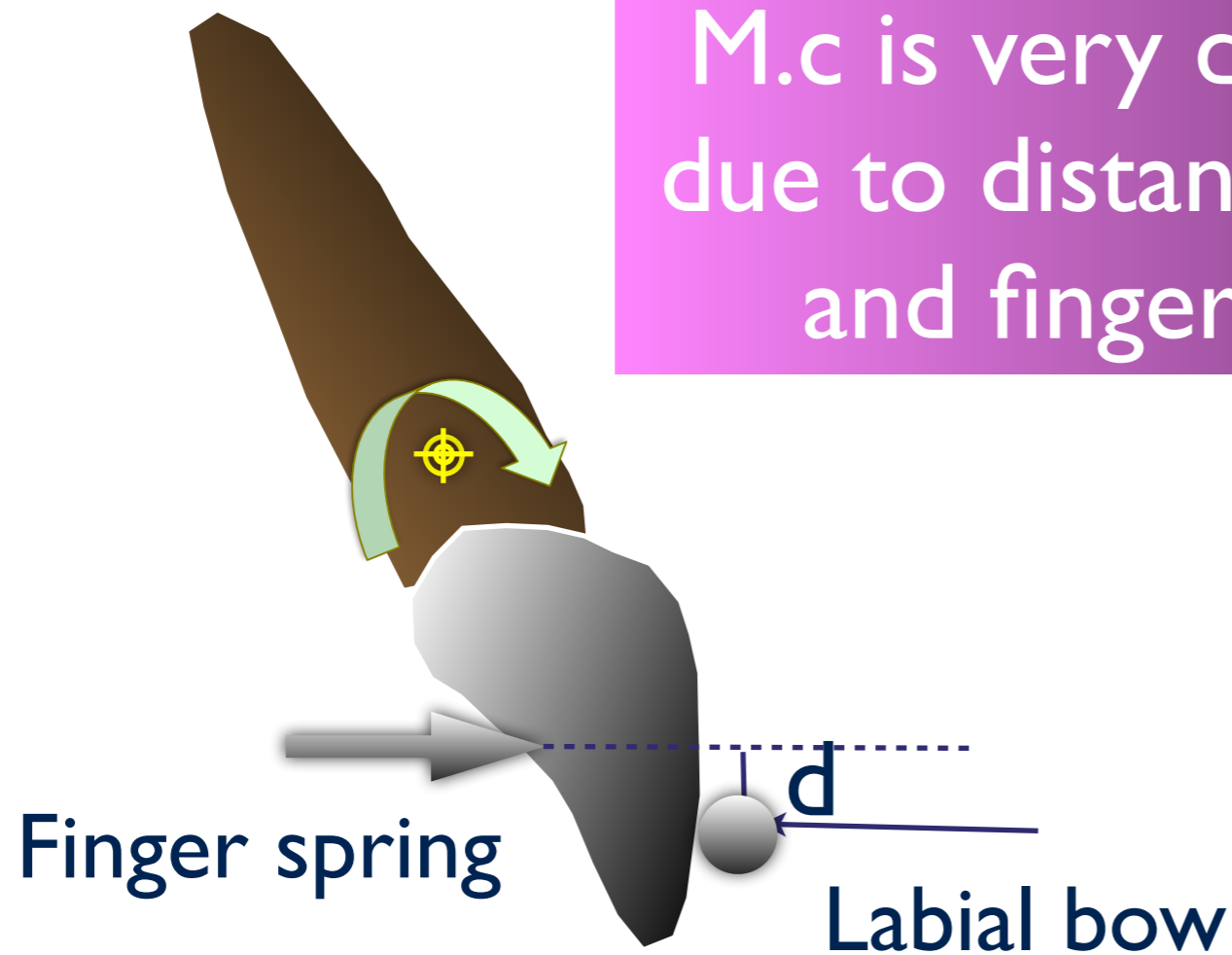


$$F1 = F2$$
$$M.c2 > M.c1$$

Less force (pain) but more effective

# Moment of couple in Removable Appliances

M.c is very difficult to initiate in RA. due to distance between labial spring and finger spring is very short.



# Force System and Center of Rotation

The method for predicting the type of tooth movement(Center of Rotation)

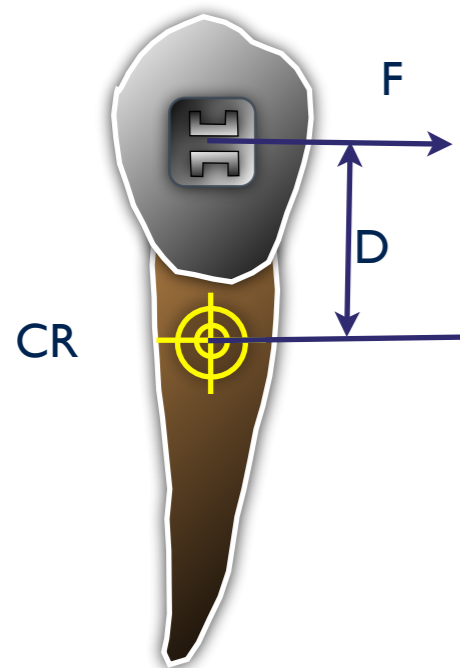
Resultant orthodontic  
single force  
(not through CR)



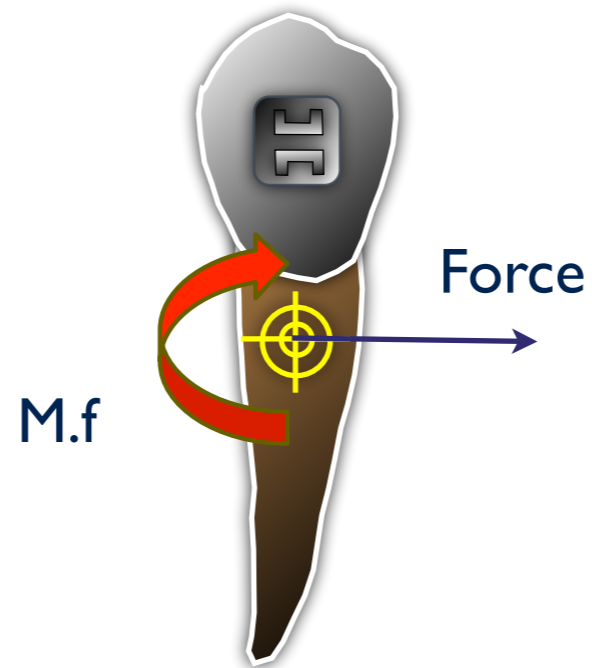
Single force at  
CR(Translation)  
+ M.c (Pure  
Rotation)



Type of tooth MM  
(Location of C.rot)



$$M.f = FD$$

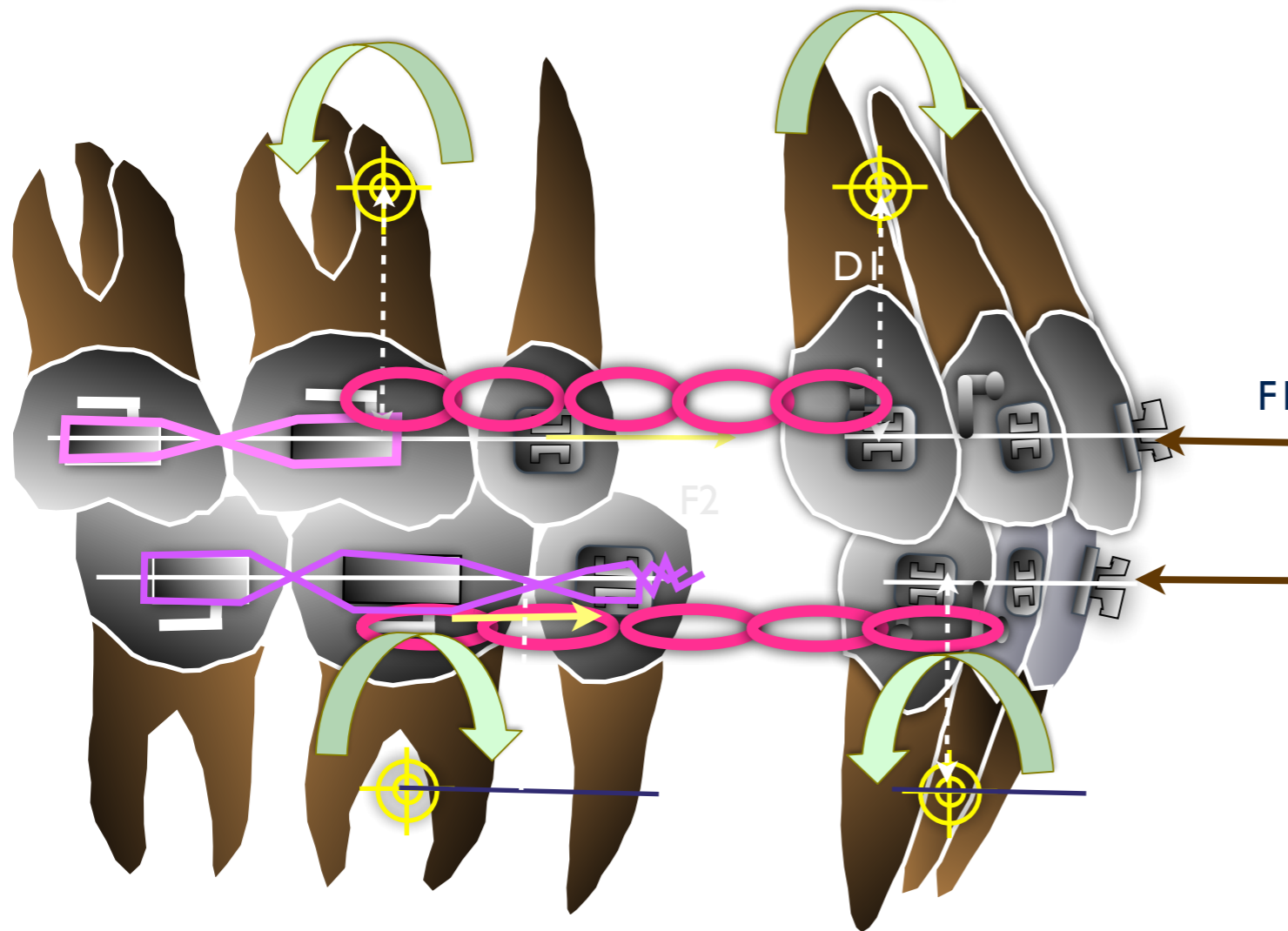


Force System



Type of tooth MM.

# Force System & clinical application

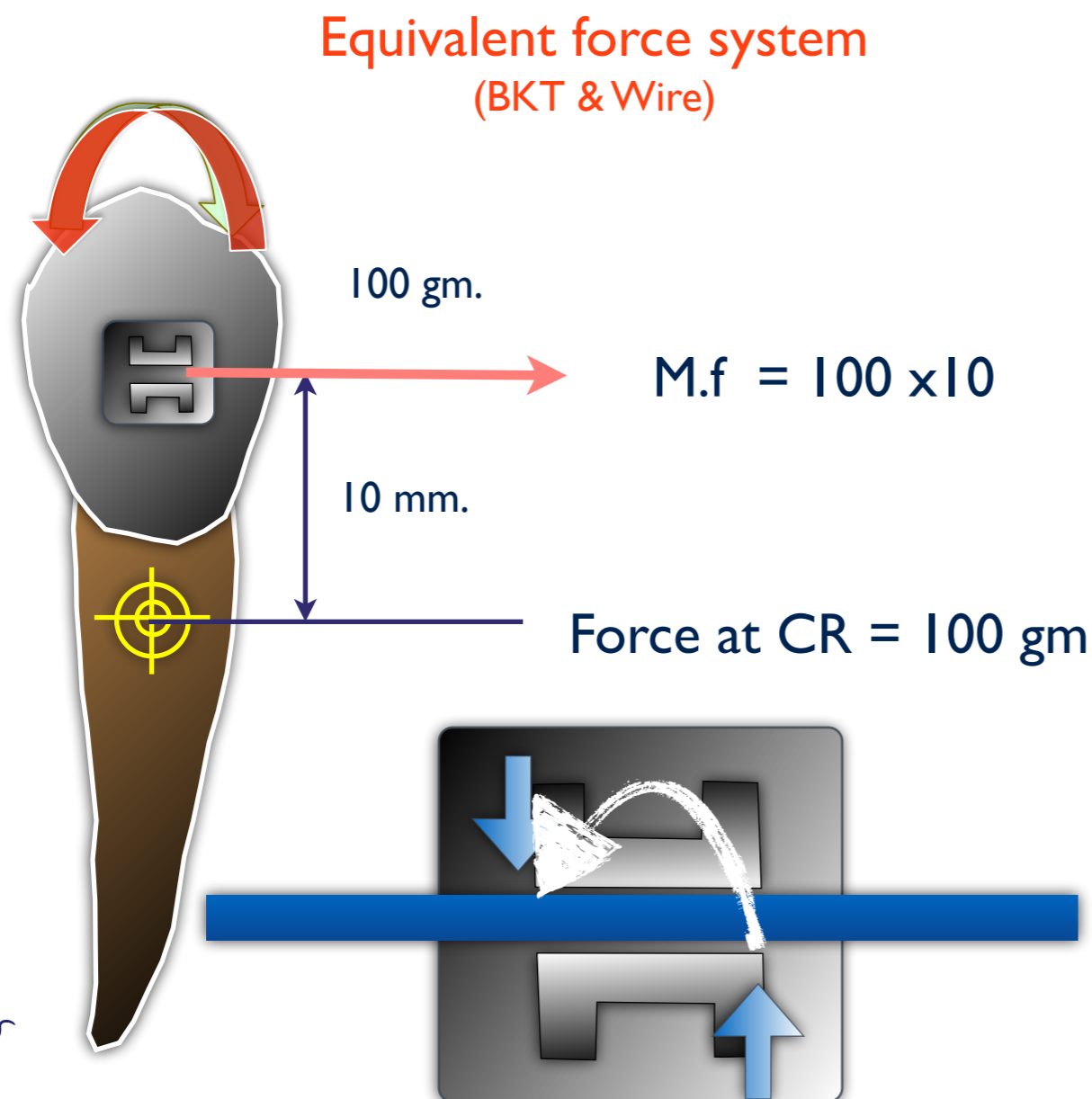


- Overbite increased
- I/I retrocination
- Mesial tipping of buccal segment (Anchorage loss)
- Bite opening around #3 - #5
- Usually this situation occurs in space closure by full strap power chain (จัดฟันแบบ Turbo)

# Force System & Equivalent Force System

(Action & Reaction)

- The method for predicting the type of tooth movement(Center of Rotation).
- Determining equivalent FS to control tooth MM



## Force System (Action)

$$M.f = 100 \times 10$$

$$= 1000 \text{ gm-mm}$$

= Clockwise crown tipping

$$\text{Force at CR} = 100 \text{ gm}$$

= Translation

## Equivalent force system (Reaction)

Counter clockwise moment

-M.c at CR

$$M_c > 1000 \text{ gm-mm} = \text{Root MM}$$

$$M_c < 1000 \text{ gm-mm} = \text{Crown}$$

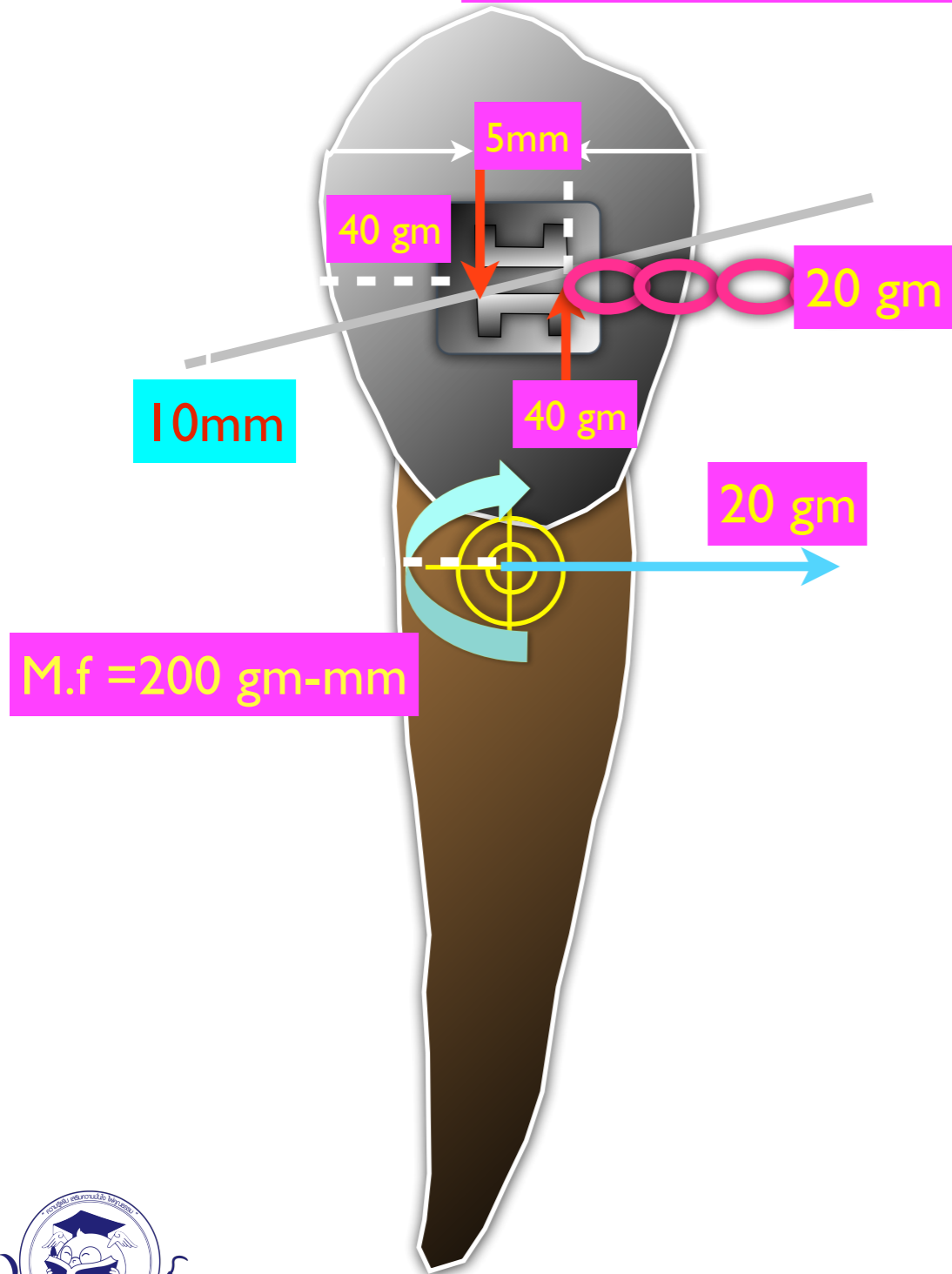
tipping

$$M_c = 1000 \text{ gm-mm} = \text{Translation}$$



# The amount of equivalent force

can determine the type of tooth MM.

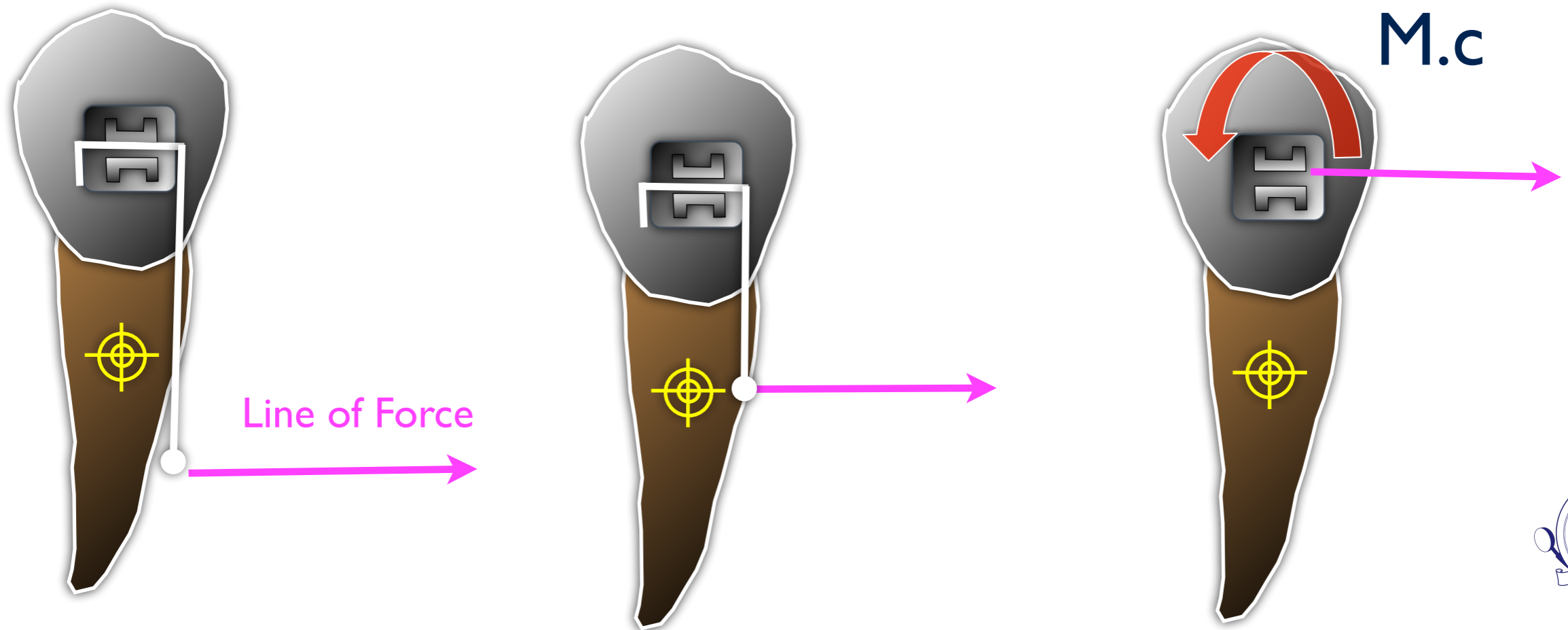


	Moment	Force	Result
Force system	$20 \times 10 = 200 \text{ gm-mm}$ Clockwise	at CR = 20 gm.	Crown tipping
Equivalent Force	$40 \times 5 = 200$ Anti-clockwise	None (couple)	Translation by 20 gm. at CR
	$M.c > \text{equi force}$ (Gable-bend,)		Root MM. or torque
	$M.c < \text{equi force}$ (V-bend)		Crown tipping





# How to control the orthodontic force to get a desirable tooth movement ?



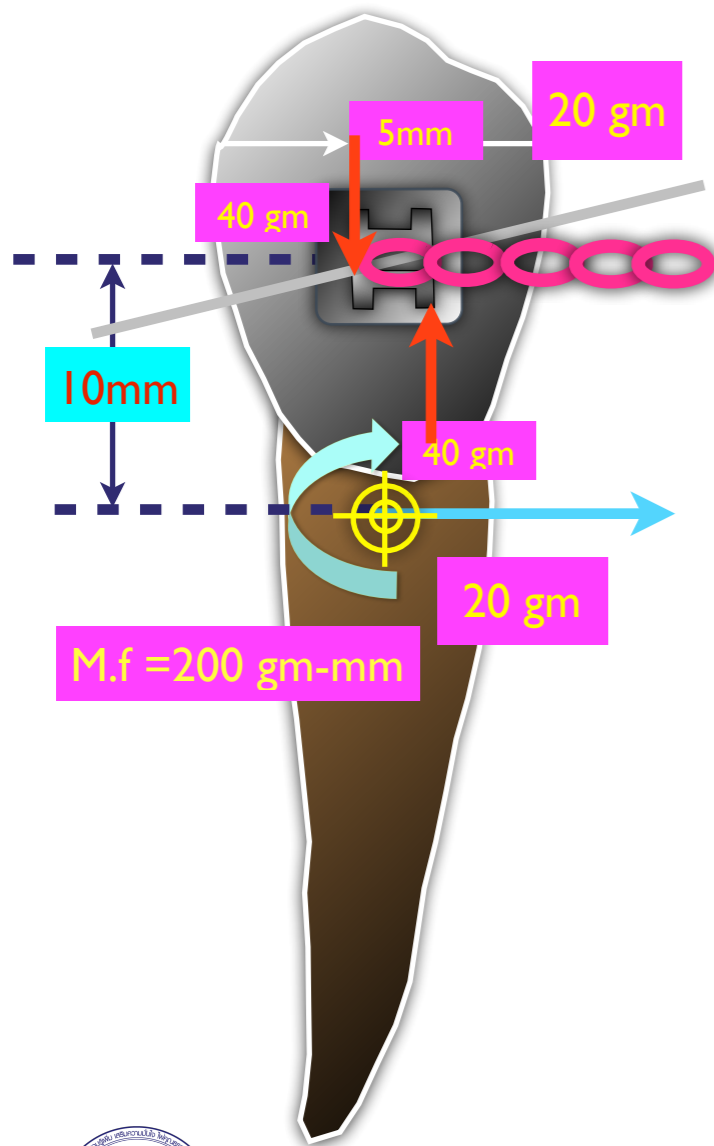
Controlling the line of force relative to CR according to the type of tooth MM needed

Regulating amount of M.c in the bracket produced relative to M.f when the force applied at bracket



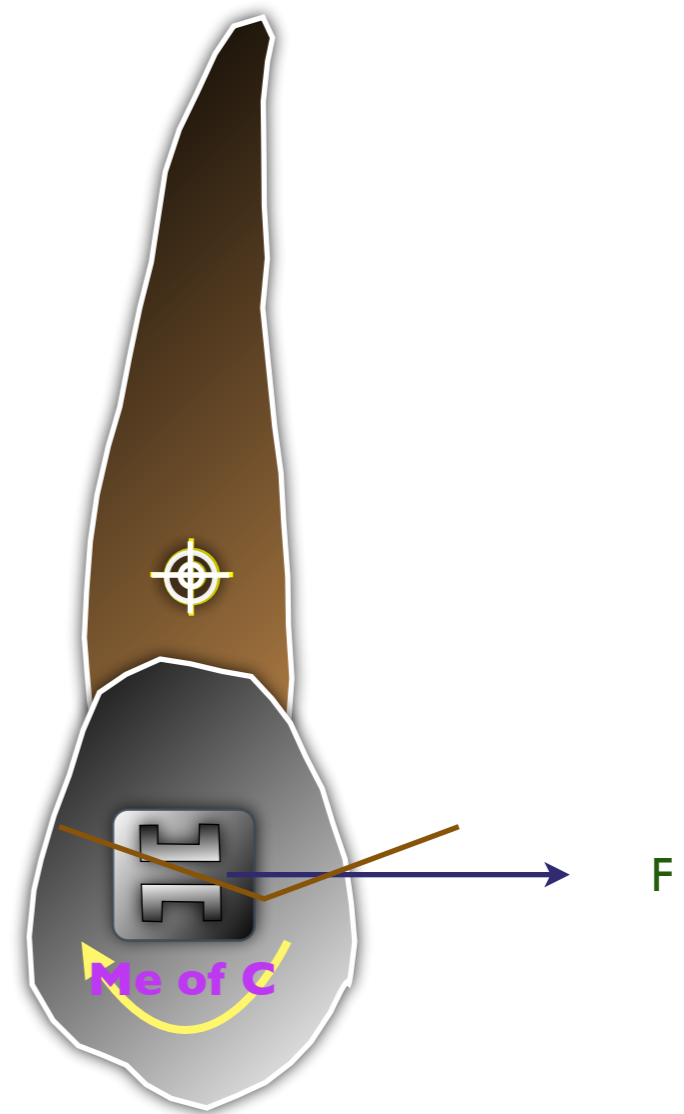
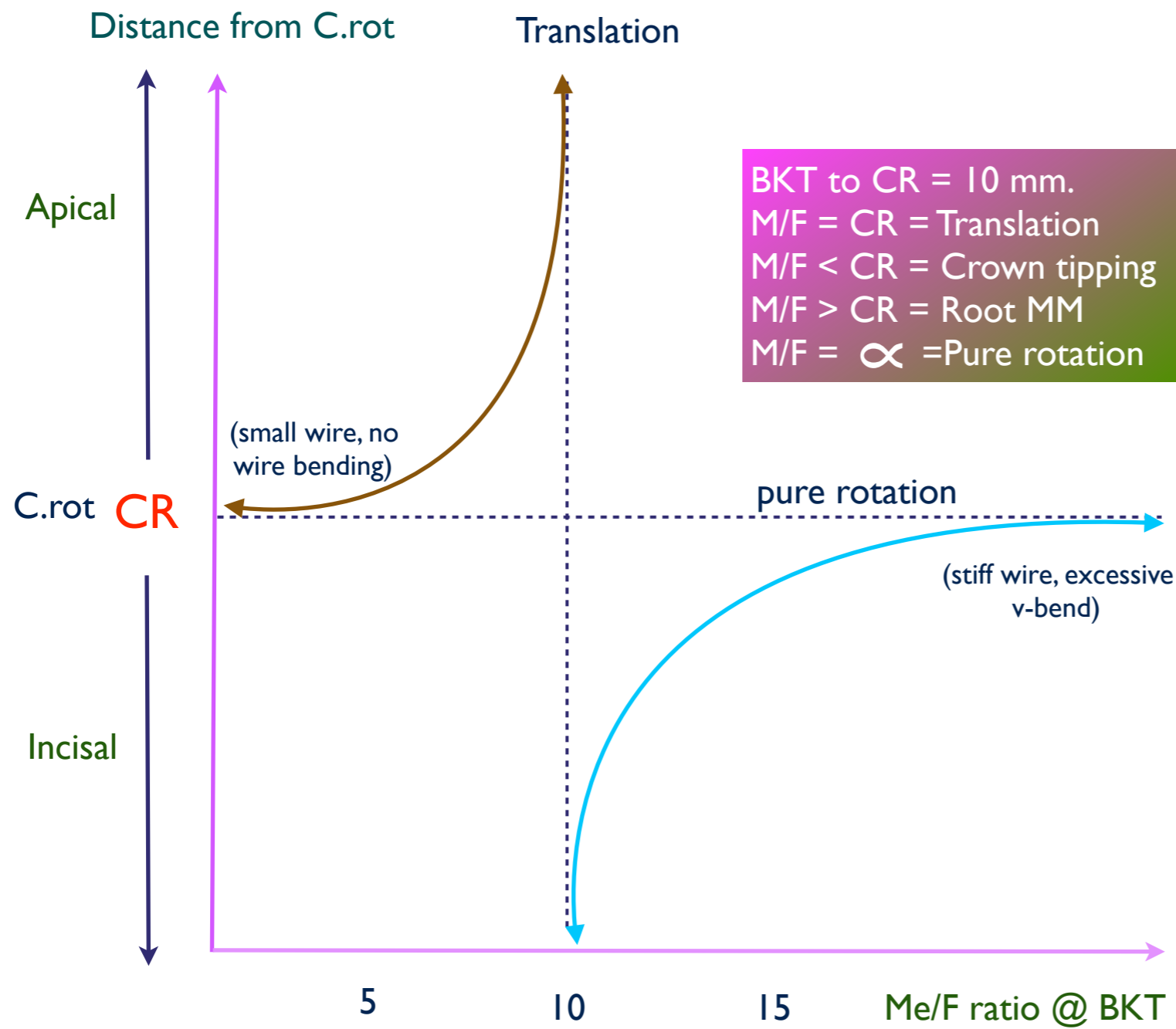


# FS & EFS & M/F ratio & Type of Tooth MM.



	Couple force (MOC)	Moment @ CR	Force	M.e/F Ratio	Relative to CR	Result
Force system	---	$20 \times 10 = 200 \text{ gm-mm}$ Clockwise	at CR = 20 gm.	---	LOF to CR = 10 mm.	Crown Tipping
Equivalent FS	40 gm	$40 \times 5 = 200$ Anti-clockwise	None (couple)	$200/20 = 10$	<b>M/F = CR (10mm)</b>	<b>Translation</b>
	< 40 gm. (small wire, no wire bending)	$F_c \times 5 < 200$		$< 200/20 < 10$	<b>M/F &lt; CR</b>	<b>Crown Tipping</b>
	> 40 gm. (stiff wire, v-bending)	$F_c \times 5 > 200$		$> 200/20 > 10$	<b>M/F &gt; CR</b>	<b>Root MM</b>
No force at BKT	Any	Any	F=0 gm.	$\infty$	$\infty$	Pure Rotation

# M/F ratio and C.rot



# $M_c/F$ ratio & C.rot for max incisor

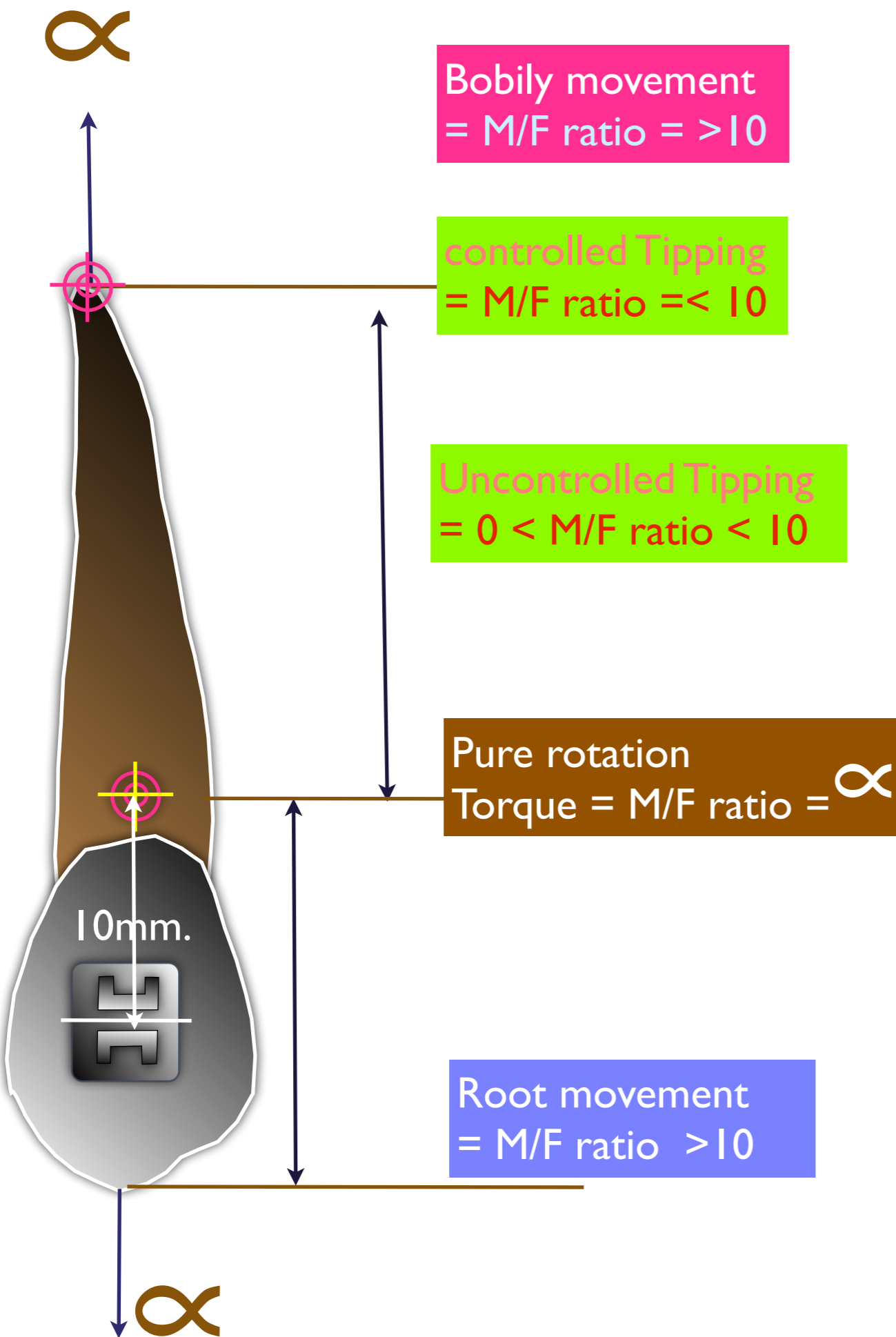
CR to Bracket = 10 mm.

$$M_f = F \times \text{Distance CR to BKT}$$

$$M.f/F = \text{Distance CR to BKT}$$

Type of tooth MM	M/F ratio	C.rot
Translation	10	Infinity
Controlled tipping	5	Apex
Uncontrolled tipping	0	CR - Apex
Root MM	12	CR - incisal edge
Pure rotation	$\infty$ (No Force)	CR

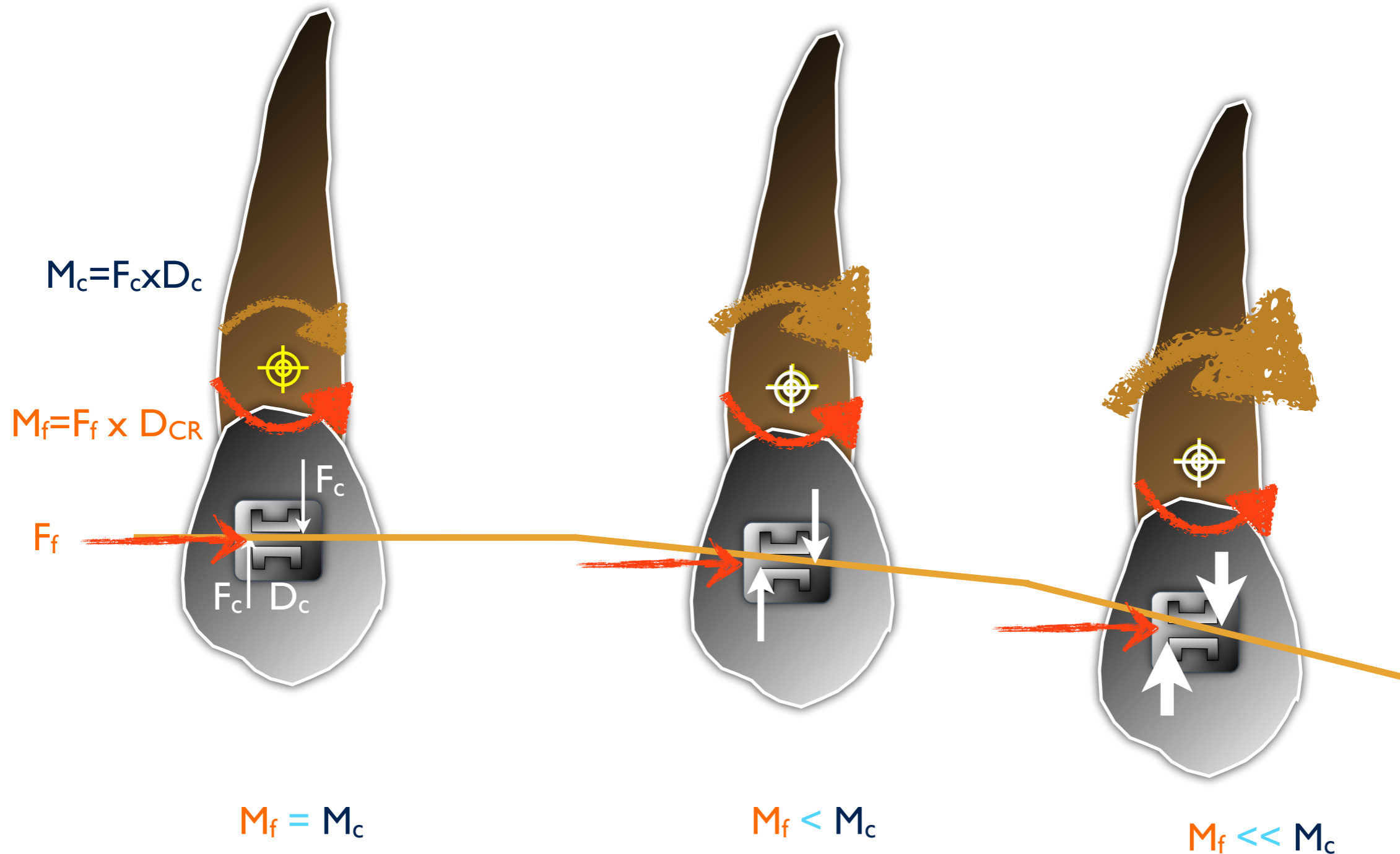




# Center of Rotation & Moment to Force Ratio

M/F ratio is used to describe type of tooth movement

# Clinical implicaton



# Static Equilibrium

## Newton's laws

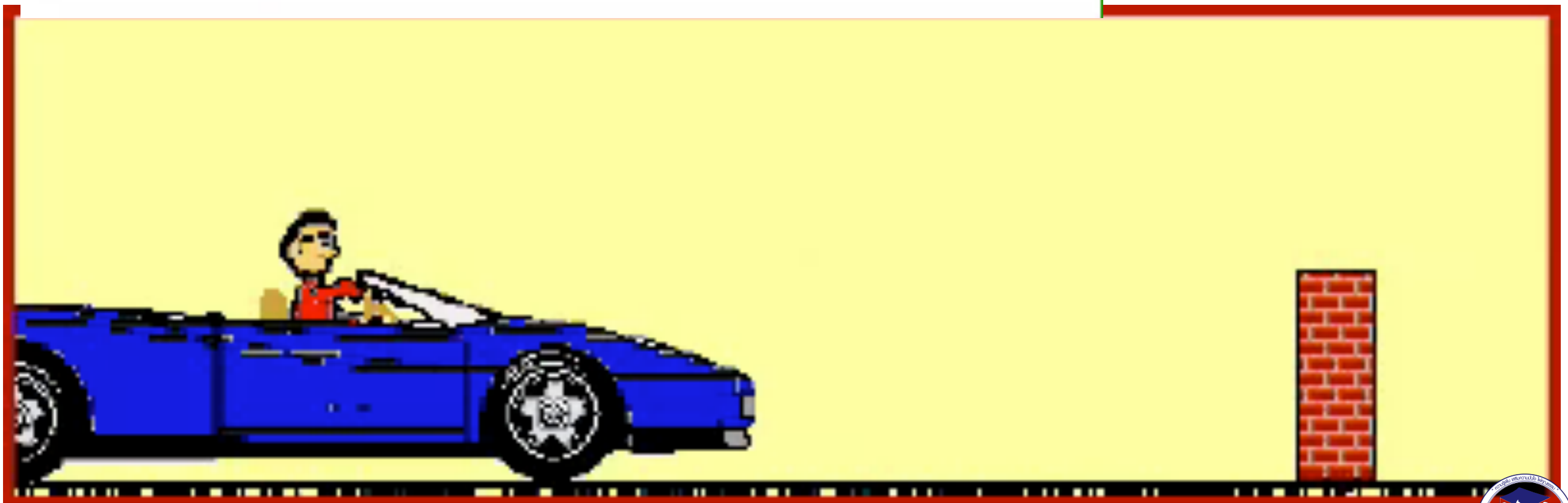
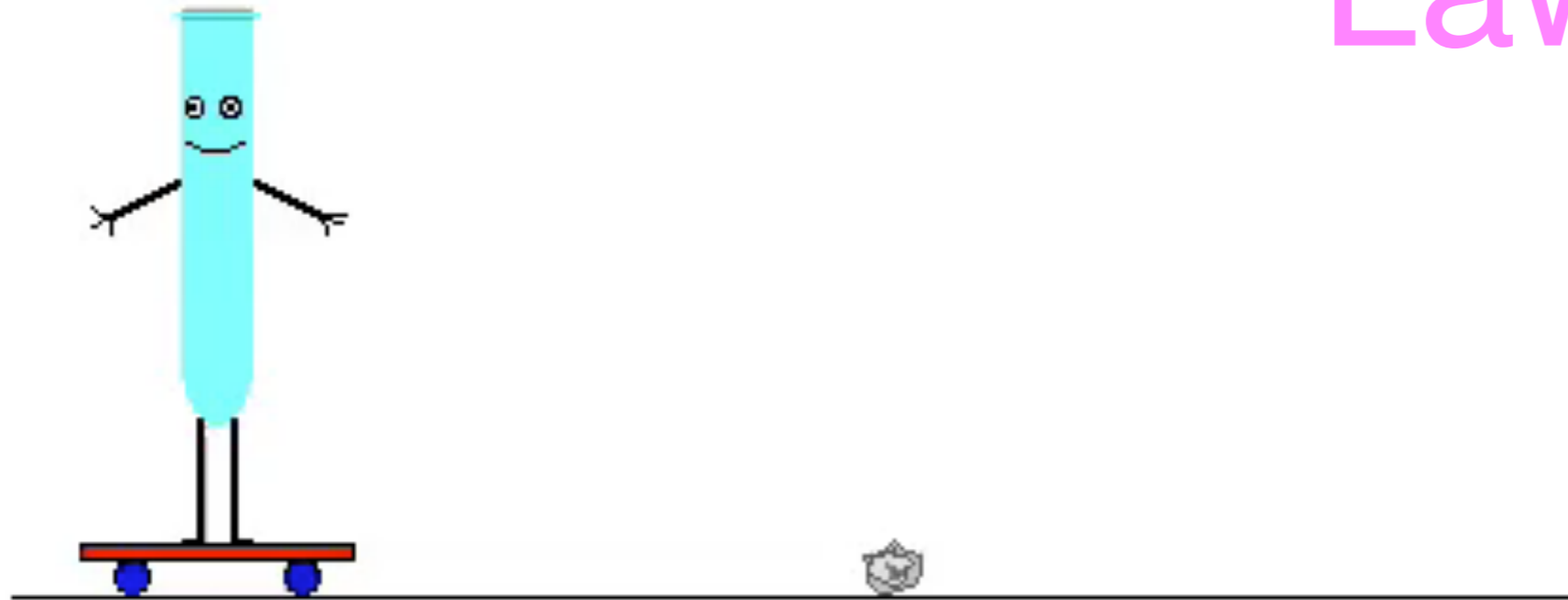
**Law of inertia** : Every body continues in its state of rest or uniform motion in a straight line unless it is compelled to change by the force impressed on it (seat belt) (Dynamic Equilibrium)

**Law of acceleration** : the change in motion is proportional to the impressed motive force and is made in the direction of the straight line in which the force is impressed ( $F=ma$ )

**Law of action and reaction** : To every action there is always an opposing and equal reaction (Rocket)( Static Equilibrium)



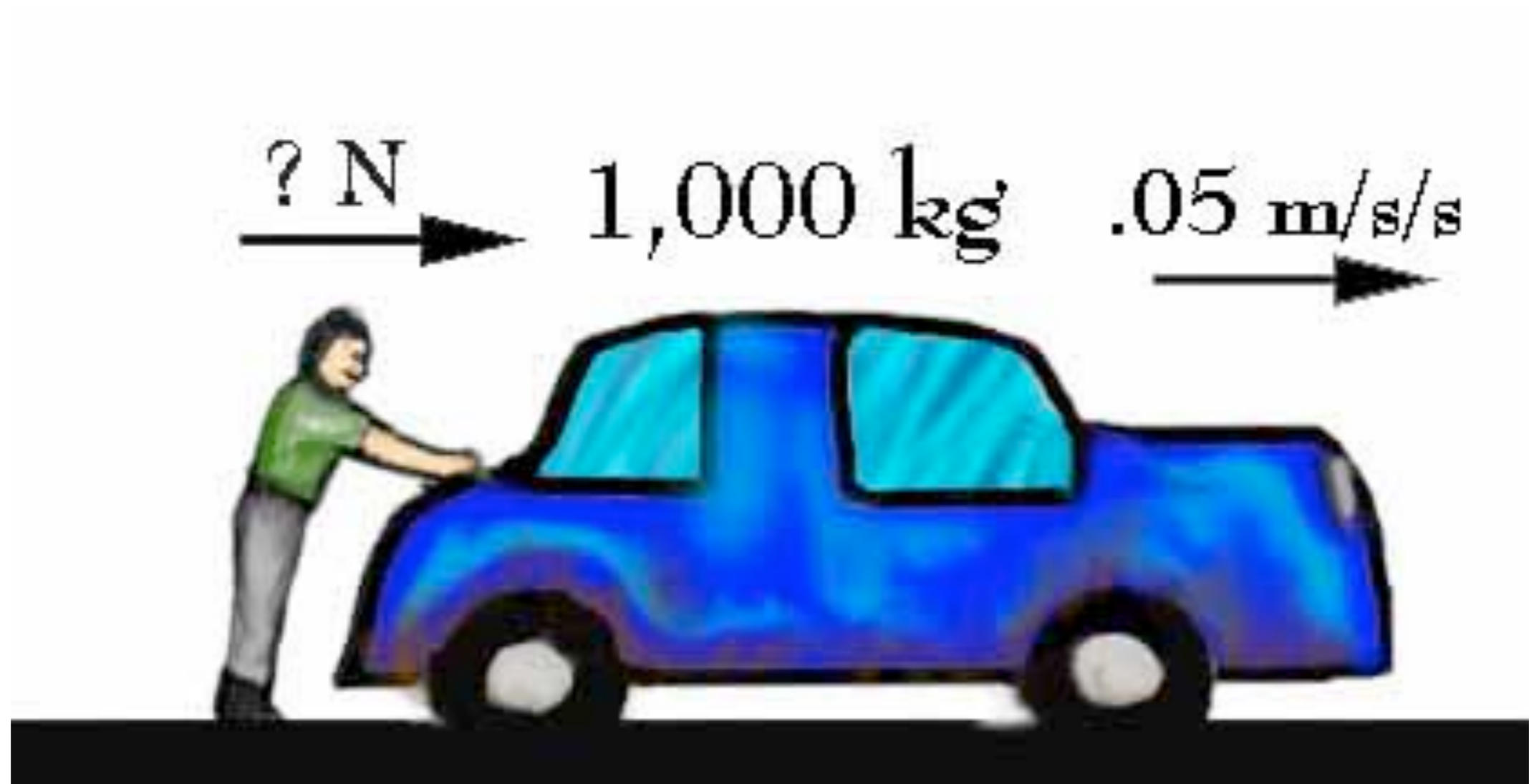
# Law of inertia





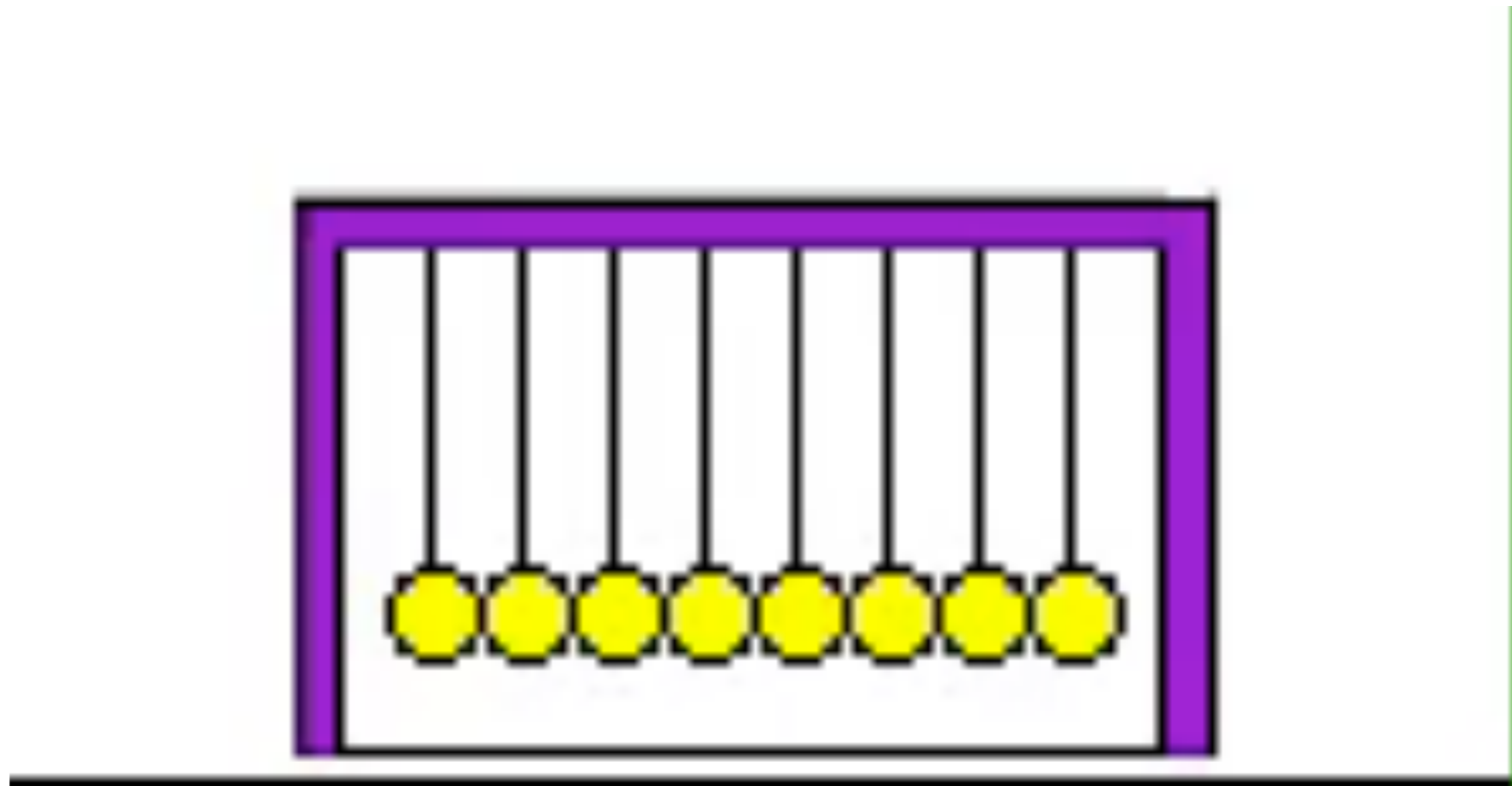
# Law of acceleration

Acceleration is produced when a force acts on a mass. The greater the mass (of the object being accelerated) the greater the amount of force needed (to accelerate the object).



# Law of action and reaction

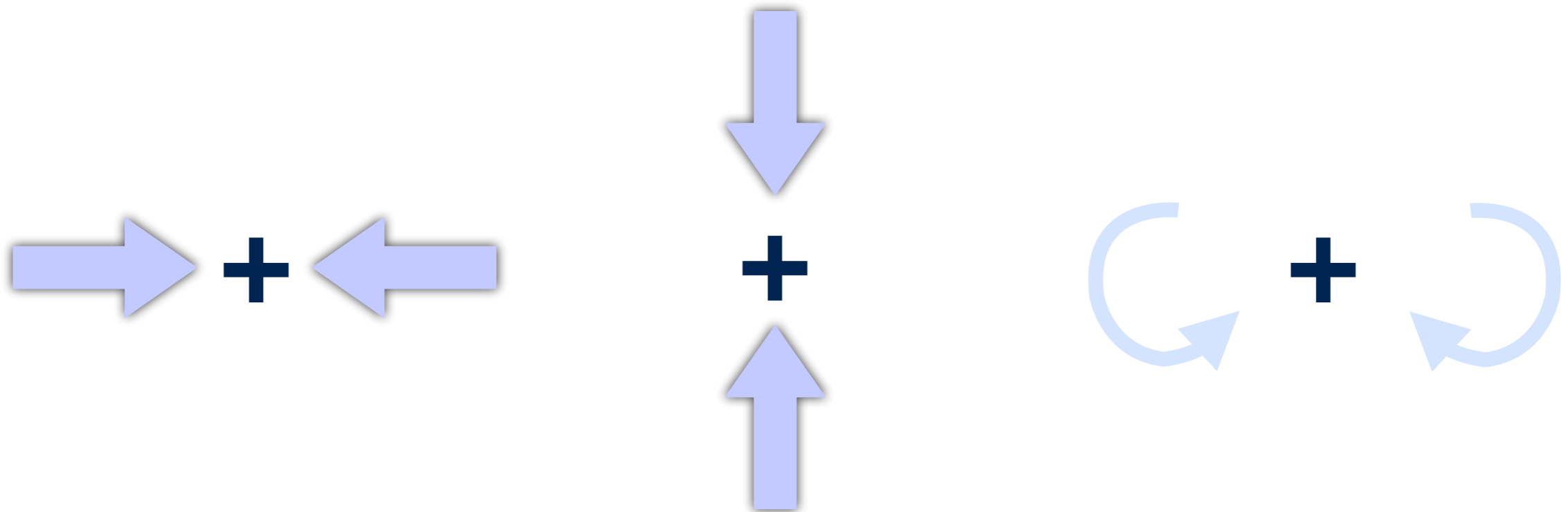
**For every action there is an equal and opposite re-action.**



# Static Equilibrium

STATIC EQUILIBRIUM IMPLIES –AT ANY POINT WITHIN A BODY, THE SUM OF FORCES AND MOMENTS ACTING ON A BODY IS ZERO.

THE ANALYSIS OF EQUILIBRIUM AS APPLIED TO ORTHODONTICS CAN BE STATED AS



# Static Equilibrium

**Is used to analyse the whole of every force system to predict tooth movement in the equilibrium**

can be stated in equation form

Horizontal forces =  $F_x=0$   
Vertical forces =  $F_y=0$   
Transverse forces =  $F_z=0$

Moments (X axis) =  $M_x=0$   
Moments (Y axis) =  $M_y=0$   
Moments (Z axis) =  $M_z=0$



# Static Equilibrium Situation

Many appliances and bends placed in clinical situations

Many situations –unequal forces and moments develop.

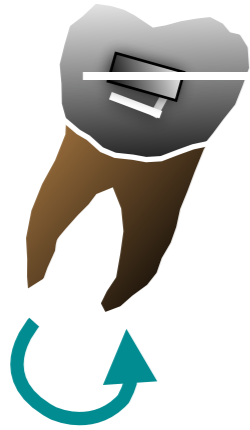
**“Additional forces”**-develop to obtain equilibrium

Determination of complete system in equilibrium-side effects.

The forces and moments that determine a appliances equilibrium –must exist.

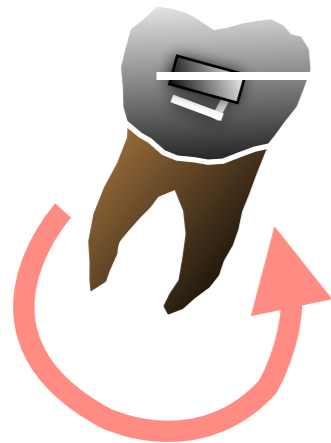


# Clinical situation of Static Equilibrium



*Equal forces and moments  
develop no moment*

**Moment acting around  
any point must = 0**



+



*unequal forces and  
moments develop*

**Forces produced to  
maintain static  
equilibrium**

*Additional forces*



*side effects*

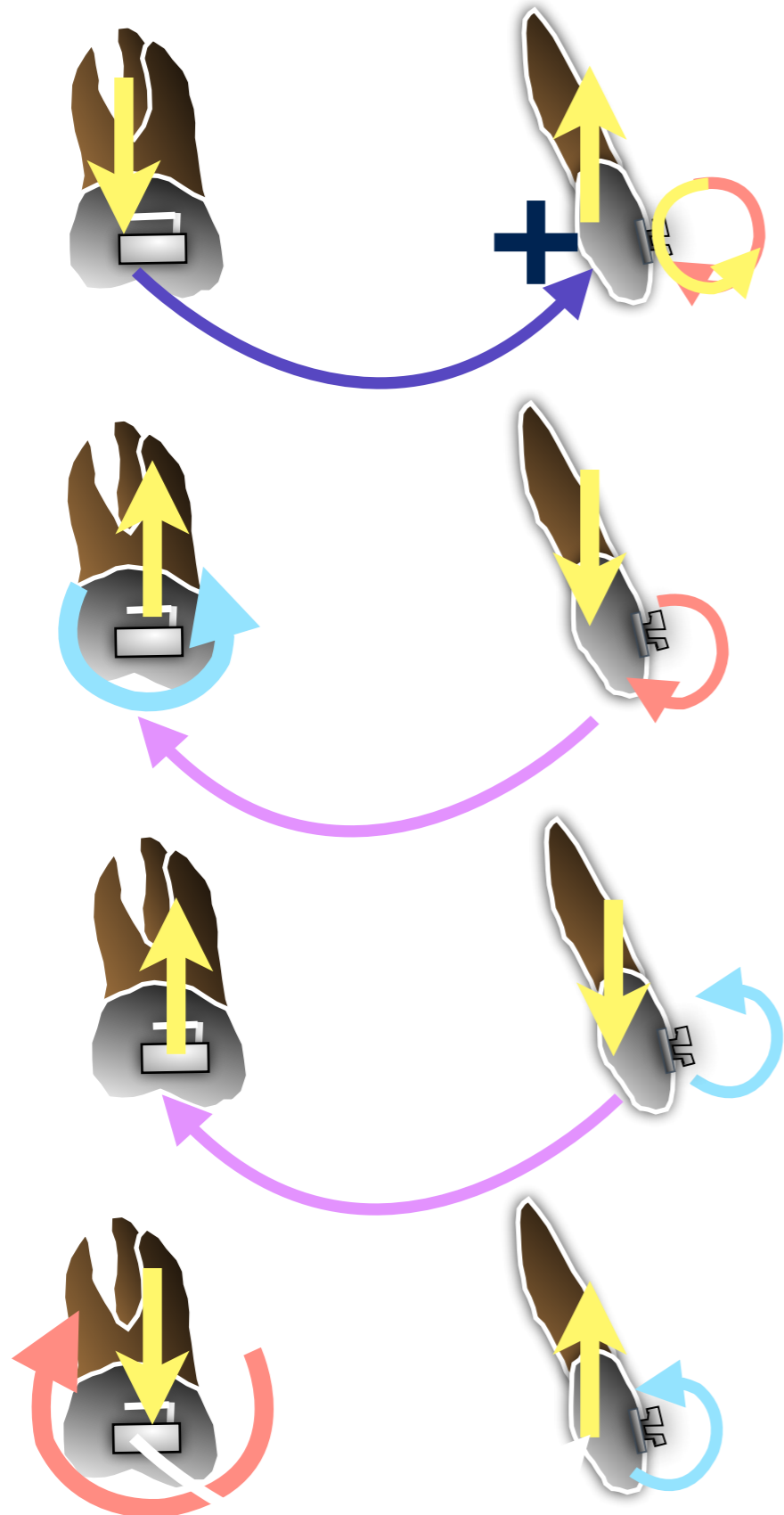
**Extrusion**

**Intrusion**

**Magnitude of forces  
exactly necessary to  
produce a counter  
rotation.**



# Pre-torque 20



**MOMENT : LABIAL ROOT TORQUE OF 1/-**  
**SIDE EFFECT**

- INTRUSION OF 1/-
- EXTRUSION OF 6/-

**MOMENT : LABIAL ROOT TORQUE OF 1/- & MESIAL TIPPING OF 6/-**  
**SIDE EFFECT**

- INTRUSION OF 6/-
- EXTRUSION OF 1/-

**MOMENT : PALATAL ROOT TORQUE OF 1/-**  
**SIDE EFFECT**

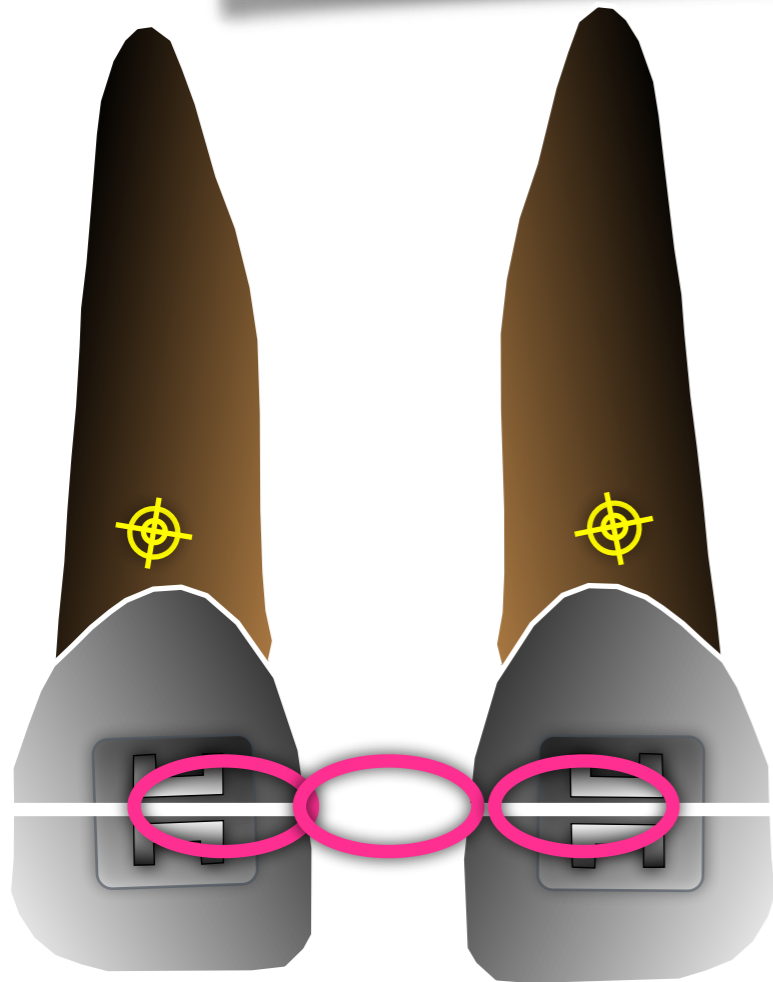
- INTRUSION OF 6/-
- EXTRUSION OF 1/-

**MOMENT : PALATAL ROOT TORQUE OF 1/- & DISTAL TIPPING OF 6/-**  
**SIDE EFFECT**

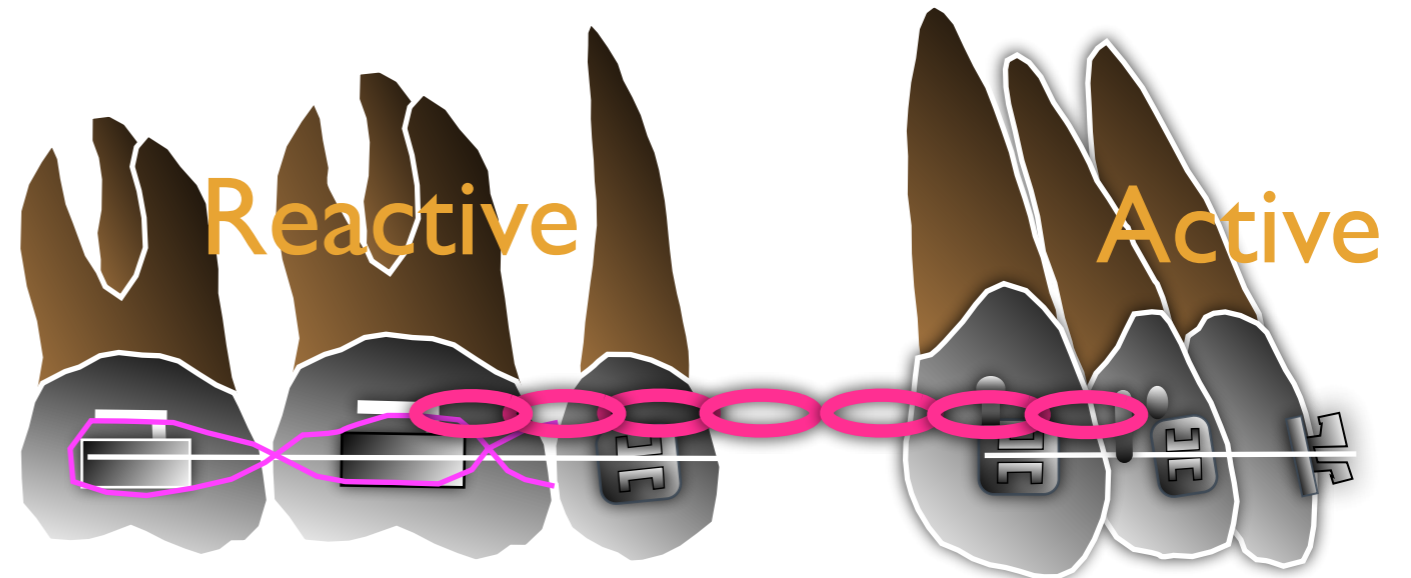
- INTRUSION OF 1/-
- EXTRUSION OF 6/-



# Clinical situation of Active & Reactive



Active/Reactive



**Active Part :**

serves as tooth movement part

**Reactive Part :**

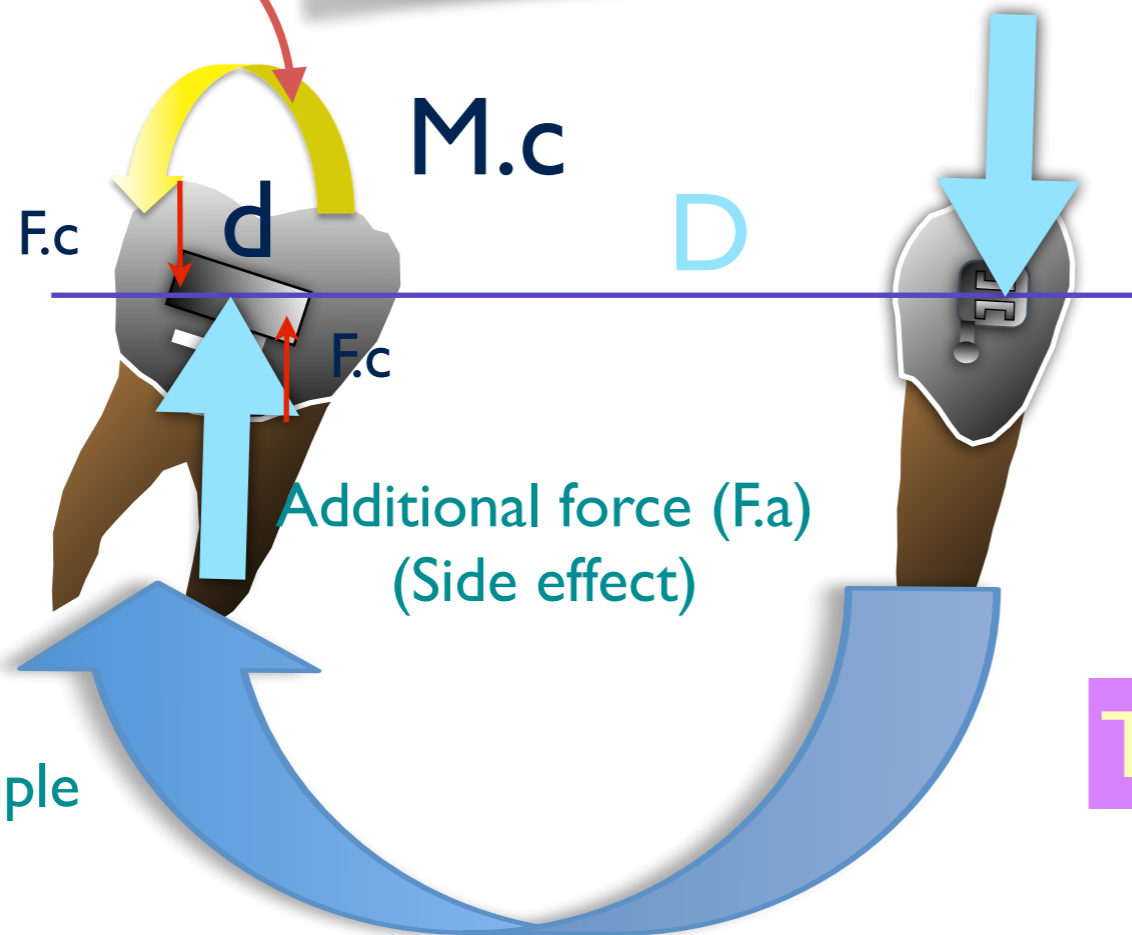
serves as anchorage

**Combination Part :**

serves as both movement and anchorage

# Static Equilibrium

unequal forces  
and moments  
develop



Additional force (F.a) (Side effect)  
develop to obtain equilibrium

Additional couple  
(M.a)

Tooth movement prediction

Static equilibrium

$$M.a = M.c$$

$$F.a \times D = F.c \times d$$

$$F.a/F.c = d/D$$

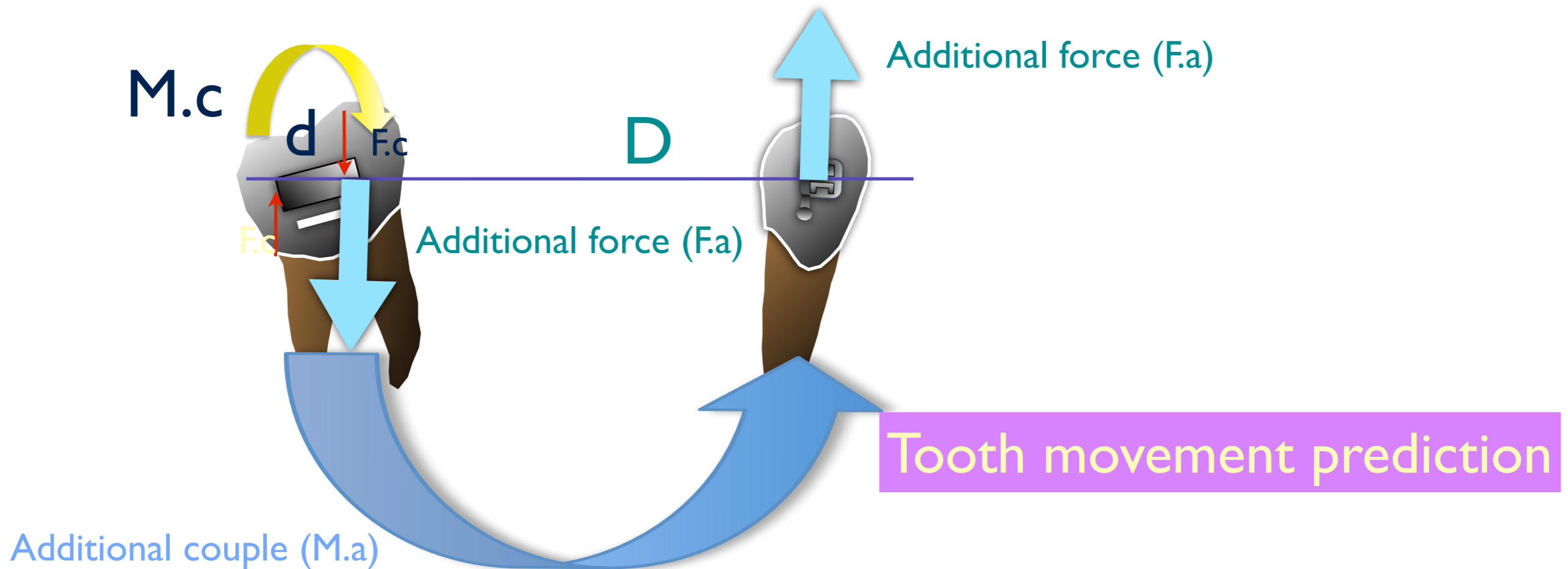
Canine:

Intrusion (Side effect)

Molar:

Distal tipping

Extrusion (Side effect)



Static equilibrium

$$M.a = M.c$$

$$F.a \times D = F.c \times d$$

$$F.a/F.c = d/D$$

Canine:

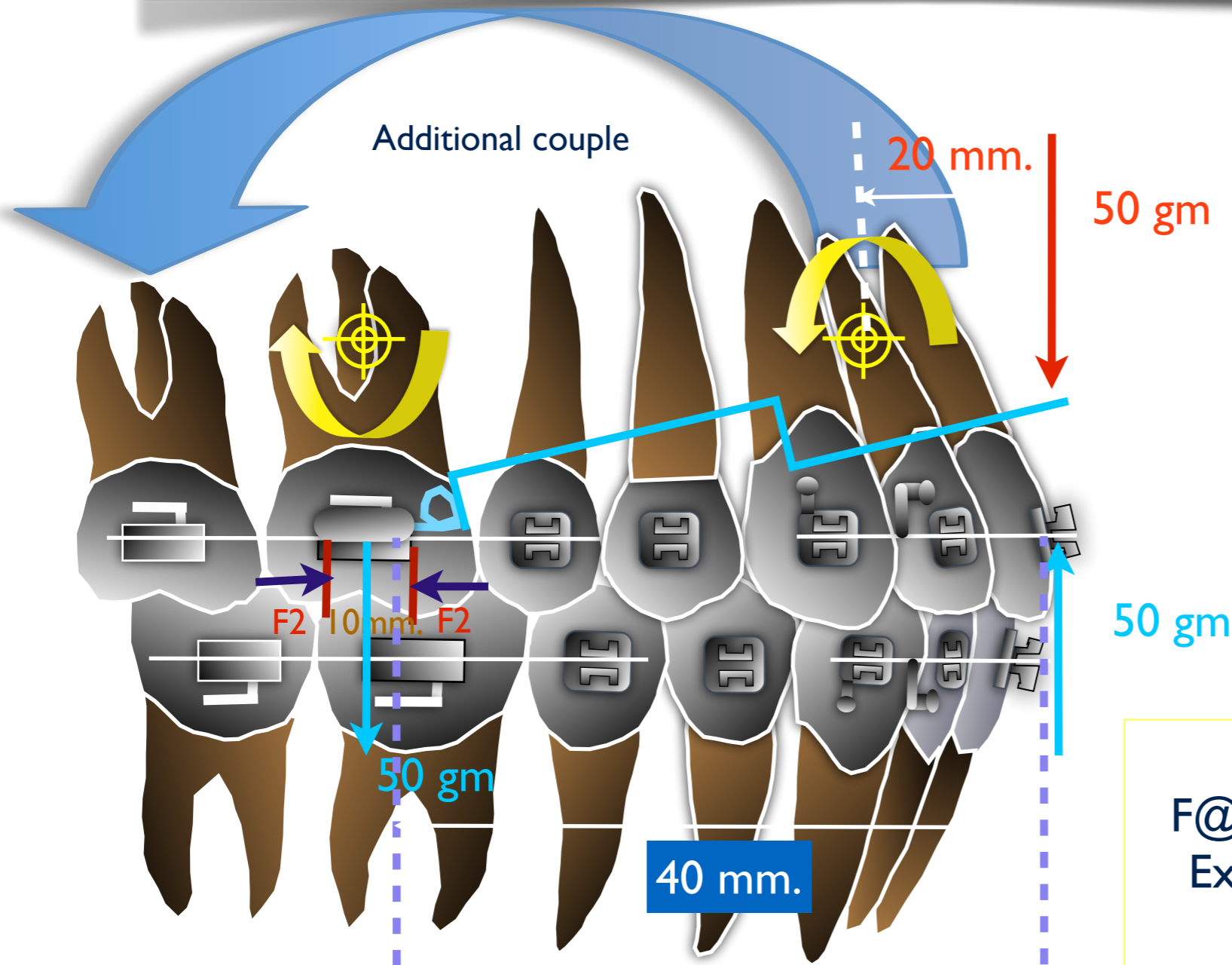
Extrusion

Molar:

Mesial tipping

Intrusion

# Static Equilibrium & Orthodontics



**Force System I**

$M.f1 = 50 \times 20 \text{ gm-mm}$   
 $= 1000 \text{ gm-mm}$   
 $F@CR = 50 \text{ gm. (intrusion)}$

**Force system2**

$M.c2 = F2 \times 10\text{mm.}$   
 $= 10F2 \text{ gm-mm}$

**Additional couple**

$F@CR(\text{ant Intrusion force}) = 50 \text{ gm.}$   
 $\text{Extrusion force @ Molar} = 50 \text{ gm.}$

$M.e \text{ (ad)} = 50 \times 40$   
 $= 2000 \text{ gm-mm}$

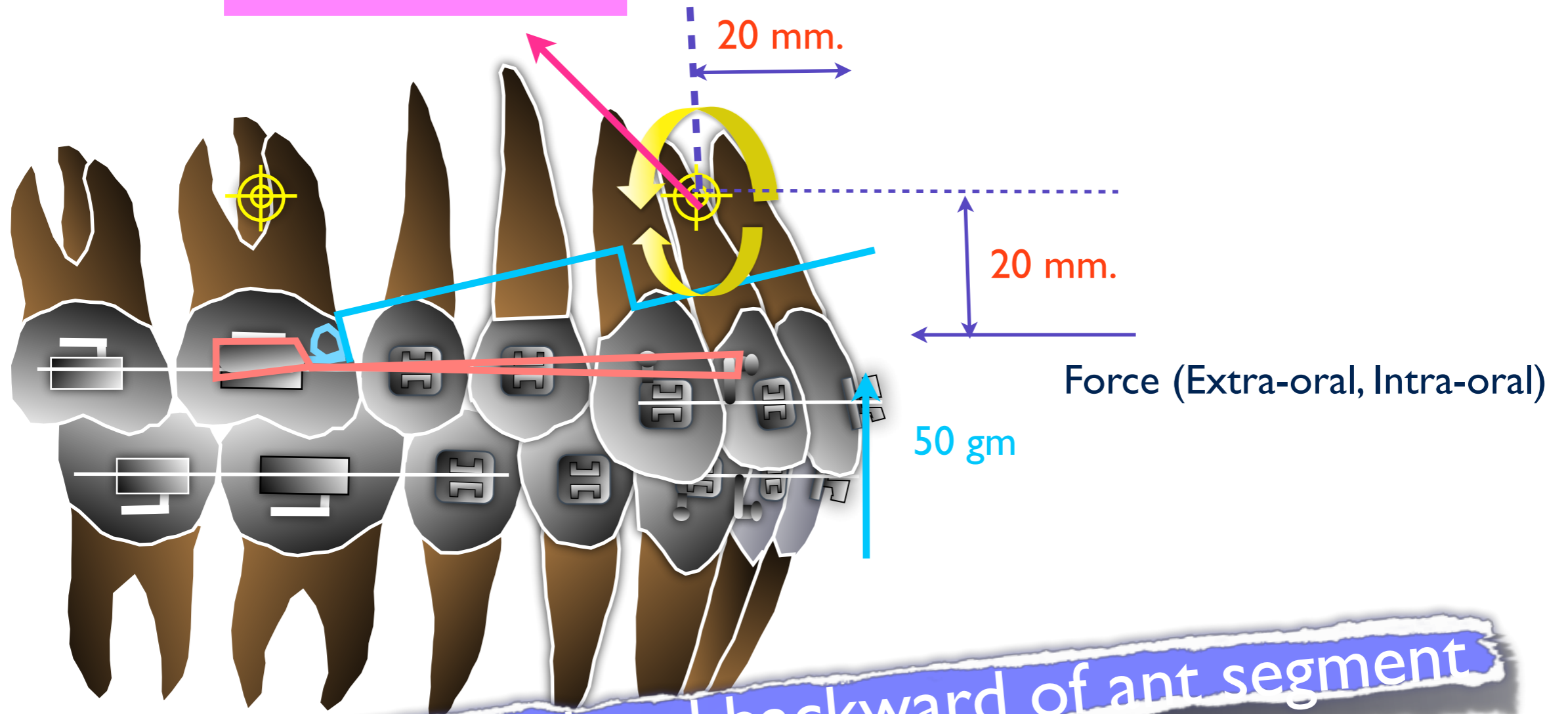
**Static Equilibrium**

$M.f1 + M.e(ad) = M.c2$   
 $1000 + 2000 = 10F2$   
 $F2 = 3000/10 = 300 \text{ gm.}$   
 $M.c2 = 10 \times 300 = 3000 \text{ gm-mm}$



# Force system analysis at anterior segment

Resultant force



Translation upward and backward of ant segment

