

Sum and Difference Identities 6.3



Overview of problems



Example Set: A

Use the sum and difference identities to determine the exact value of each of the following expressions.

1. $\cos\left(\frac{\pi}{4} + \frac{\pi}{3}\right)$

2. $\sin\left(\frac{\pi}{6} + \frac{3\pi}{4}\right)$

3. $\tan\left(\frac{4\pi}{3} + \frac{5\pi}{4}\right)$

4. $\tan(75^\circ)$

5. $\sin(165^\circ)$

6. $\sin\left(\frac{\pi}{12}\right)$

7. $\tan\left(\frac{5\pi}{12}\right)$

Sum and Difference Identities 6.3



Overview of problems

Example Set: B

Find the sum or difference for each question.

1. $\sin(A) = \frac{4}{5}$ and $\sin(B) = \frac{5}{13}$ angle A and B are in quadrant I, Find $\cos(A - B)$

2. $\cos(A) = -\frac{15}{17}$

$\cos(B) = -\frac{3}{5}$ angle A is in quad II, and angle B is quad III, Find $\sin(A + B)$

Use the sum and difference identities to determine the exact value of each of the following expressions.

3.
$$\frac{\tan\left(\frac{5\pi}{16}\right) - \tan\left(\frac{\pi}{16}\right)}{1 + \tan\left(\frac{5\pi}{16}\right)\tan\left(\frac{\pi}{16}\right)}$$

4.
$$\frac{\tan(70^\circ) - \tan(10^\circ)}{1 + \tan(70^\circ)\tan(10^\circ)}$$

Sum and Difference Identities 6.3



Overview of problems

Example Set: C

Use the sum and difference identities to verify the following identities.

1. $\sin\left(\frac{\pi}{2} - x\right) \cos(-x) = \cos^2 x$

2. $\tan(\pi + 2\pi) = 0$

Sum and Difference Identities 6.3



Overview of problems



Example Set: A -**ANSWER KEY**

Use the sum and difference identities to determine the exact value of each of the following expressions.

$$1. \quad \cos\left(\frac{\pi}{4} + \frac{\pi}{3}\right) = \frac{-\sqrt{6} + \sqrt{2}}{4}$$

$$2. \quad \sin\left(\frac{\pi}{6} + \frac{3\pi}{4}\right) = \frac{\sqrt{6} - \sqrt{2}}{4}$$

$$3. \quad \tan\left(\frac{4\pi}{3} + \frac{5\pi}{4}\right) = -\sqrt{3} - 2$$

$$4. \quad \tan(75^\circ) = \sqrt{3} + 2$$

$$5. \quad \sin(165^\circ) = \frac{\sqrt{6} - \sqrt{2}}{4}$$

$$6. \quad \sin\left(\frac{\pi}{12}\right) = \frac{\sqrt{6} - \sqrt{2}}{4}$$

$$7. \quad \tan\left(\frac{5\pi}{12}\right) = \sqrt{3} + 2$$

Sum and Difference Identities 6.3



Overview of problems



Example Set: B -**ANSWER KEY**

Find the sum or difference for each question.

1. $\sin(A) = \frac{4}{5}$ and $\sin(B) = \frac{5}{13}$ angle A and B are in quadrant I, Find $\cos(A - B)$

$$\frac{56}{65}$$

2. $\cos(A) = -\frac{15}{17}$

$\cos(B) = -\frac{3}{5}$ angle A is in quad II, and angle B is quad III, Find $\sin(A + B)$

$$\frac{36}{85}$$

Sum and Difference Identities 6.3



Overview of problems

Use the sum and difference identities to determine the exact value of each of the following expressions.

3.
$$\frac{\tan\left(\frac{5\pi}{16}\right) - \tan\left(\frac{\pi}{16}\right)}{1 + \tan\left(\frac{5\pi}{16}\right)\tan\left(\frac{\pi}{16}\right)}$$

$$\tan\left(\frac{\pi}{4}\right) = 1$$

4.
$$\frac{\tan(70^\circ) - \tan(10^\circ)}{1 + \tan(70^\circ)\tan(10^\circ)}$$

$$\tan(60^\circ) = \sqrt{3}$$

Sum and Difference Identities 6.3



Overview of problems



Example Set: C -ANSWER KEY

Use the sum and difference identities to verify the following identities.

1. $\sin\left(\frac{\pi}{2} - x\right) \cos(-x) = \cos^2 x$

$$\sin\left(\frac{\pi}{2} - x\right) \cos(-x) = \cos^2 x$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\begin{aligned} \sin\left(\frac{\pi}{2} - x\right) &= \sin \frac{\pi}{2} \cos x - \cos \frac{\pi}{2} \sin x \\ &= 1 \cdot \cos x - 0 \cdot \sin x \end{aligned}$$

$$\sin\left(\frac{\pi}{2} - x\right) = \cos x$$

$$\sin\left(\frac{\pi}{2} - x\right) \cos(-x) = \cos^2 x$$

$$\cos x \cos(-x) = \cos^2 x$$

$$\cos(-x) = \cos x$$

$$\cos x \cdot \cos x = \cos^2 x$$

$$\cos^2 x = \cos^2 x$$

Sum and Difference Identities 6.3



Overview of problems

2. $\tan(\pi + 2\pi) = 0$

$$\tan(\pi + 2\pi) = 0$$

$$\tan(\pi + 2\pi) = \frac{\tan \pi + \tan 2\pi}{1 - \tan \pi \tan 2\pi}$$

$$\begin{array}{l} \tan \pi = 0 \\ \tan 2\pi = 0 \end{array} \quad = \frac{0 + 0}{1 - 0 \cdot 0}$$

$$\tan(\pi + 2\pi) = \frac{0}{1}$$

$$\tan(\pi + 2\pi) = 0$$