## 1.2: Properties of Real Numbers

Real numbers are classified in a variety of ways.
Natural numbers: 1, 2, 3, $\ldots$
Whole numbers: all Natural numbers, and 0 . So, $0,1,2,3, \ldots$
Integers: all Whole numbers, and the negative countable numbers: $\ldots,-3,-2,-1,0,1,2,3, \ldots$
Rational numbers: all Integers, and ratios of integers, so fractions, ending decimals, and repeating decimals

Irrational numbers: cannot be represented by a ratio of integers. They're decimals that continue on without a pattern. Common examples include $\sqrt{ }$ and $\pi$.

## KeyConcept Real Numbers (R)



| Letter | Set | Examples |
| :---: | :--- | :--- |
| Q | rationals | $0.125,-\frac{7}{8}, \frac{2}{3}=0.66 \ldots$ |
| I | irrationals | $\pi=3.14159 \ldots$ <br> $\sqrt{3}=1.73205 \ldots$ |
| Z | integers | $-5,17,-23,8$ |
| W | wholes | $2,96,0, \sqrt{36}$ |
| N | naturals | $3,17,6,86$ |

Ex\#1: Name all of the sets of numbers to which each number belongs.
a) -185
b) $\sqrt{49}$
c) $\sqrt{95}$
d) $-\frac{7}{8}$
e) 0
f) $0.5 \overline{8}$

Real Number Properties (and Examples)

| For any real numbers, $a, b$, and $c$ |  |  |
| :---: | :---: | :---: |
| Property | Addition | Multiplication |
| Commutative | $\mathrm{a}+\mathrm{b}=\mathrm{b}+\mathrm{a}$ | $\mathrm{a} \cdot \mathrm{b}=\mathrm{b} \cdot \mathrm{a}$ |
| Associative | $(\mathrm{a}+\mathrm{b})+\mathrm{c}=\mathrm{a}+(\mathrm{b}+\mathrm{c})$ | $(\mathrm{a} \cdot \mathrm{b}) \cdot \mathrm{c}=\mathrm{a} \cdot(\mathrm{b} \cdot \mathrm{c})$ |
| Identity | $\mathrm{a}+0=\mathrm{a}$ | $\mathrm{a} \cdot 1=\mathrm{a}$ |
| Inverse | $\mathrm{a}+(-\mathrm{a})=0$ | $\mathrm{a} \cdot \frac{1}{a}$ |
| Distributive | $\underline{a}(\mathrm{~b}+\mathrm{c})=\underline{a b}+\underline{a c}$ |  |
|  |  |  |

Ex:\#2: Please name the property illustrated by each of the following.
a) $(6 \cdot 8) \cdot 5=6 \cdot(8 \cdot 5)$
b) $84+16=16+84$
c) $(12+5) 6=12 \cdot 6+5 \cdot 6$

Ex\#3: Please find the additive and multiplicative inverses of each of the following numbers.
a) $\quad-7$
b) $\quad 0.8$ (hint: turn into a fraction)

Ex\#4: Please simplify the following expressions.
a) $\quad-2 a+4 a(8-3 a)$
b) $3(4 x-2 y)-2(3 x+y)$

