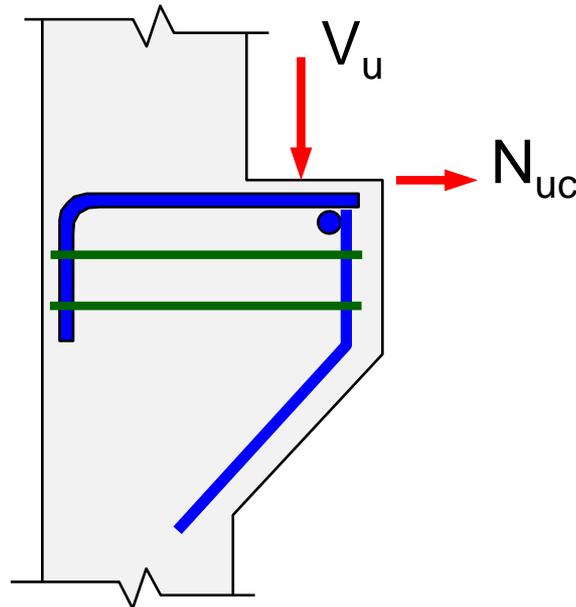


4



Advanced RC Structures

Bracket & Corbel



- Shear Friction
- Structural Action
- Types of Failure
- Design Steps
- Examples

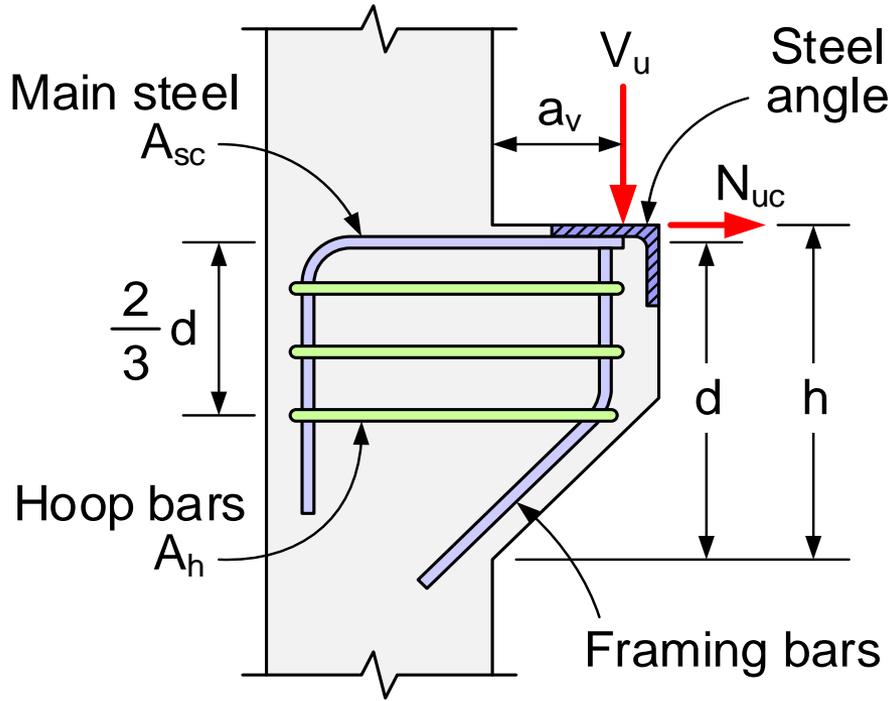
Mongkol JIRAVACHARADET

An ACI Standard

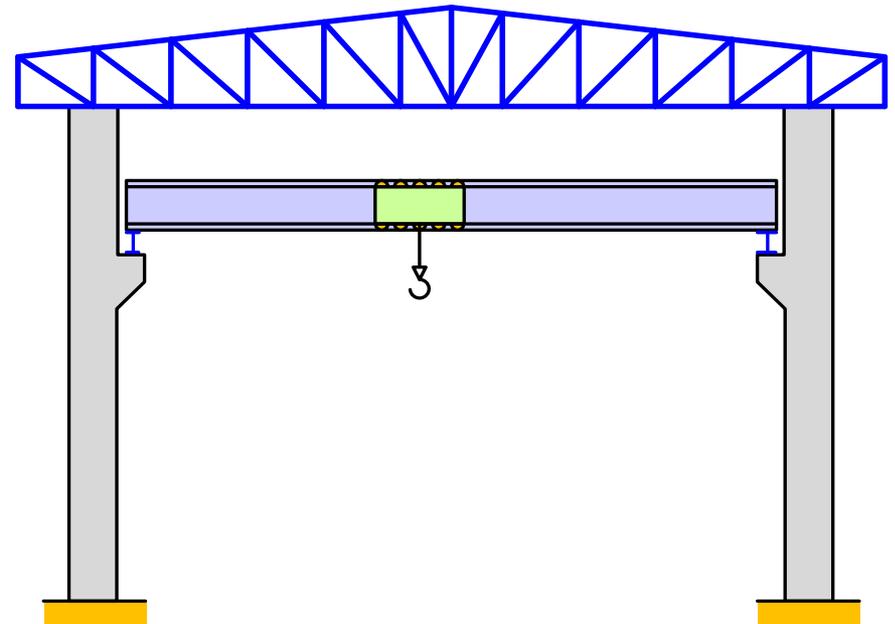
Building Code Requirements For Structural Concrete

- [-] Chapter 16—Connections Between Members
 - 16.1—Scope
 - 16.2—Connections of precast members
 - 16.3—Connections to foundations
 - 16.4—Horizontal shear transfer in composite concrete flexural members
 - 16.5—Brackets and corbels

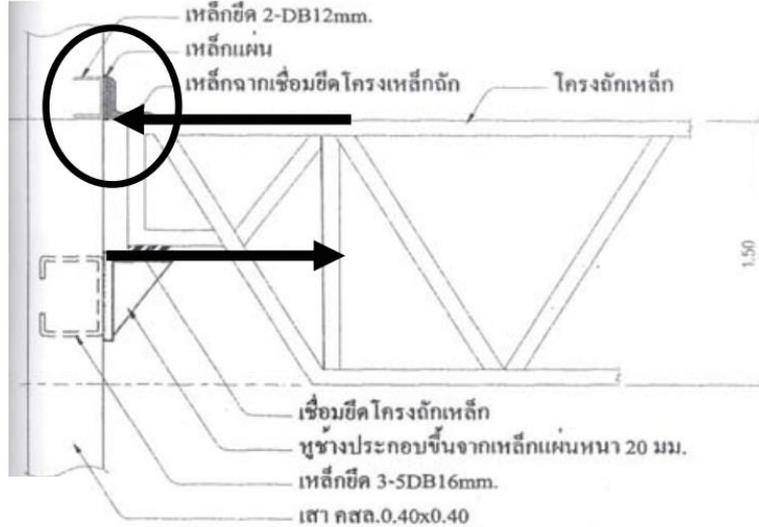
Bracket & Corbel



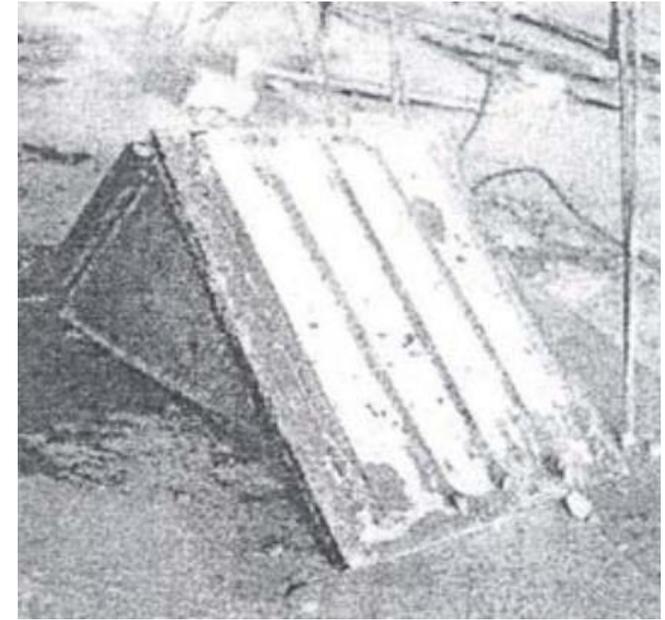
- Short cantilevers that tend to act as simple trusses or deep beams
- Used to support truss, crane or precast beams
- Design for vertical force V_u and horizontal force N_{uc}



Failure of Steel Corbel on RC Column



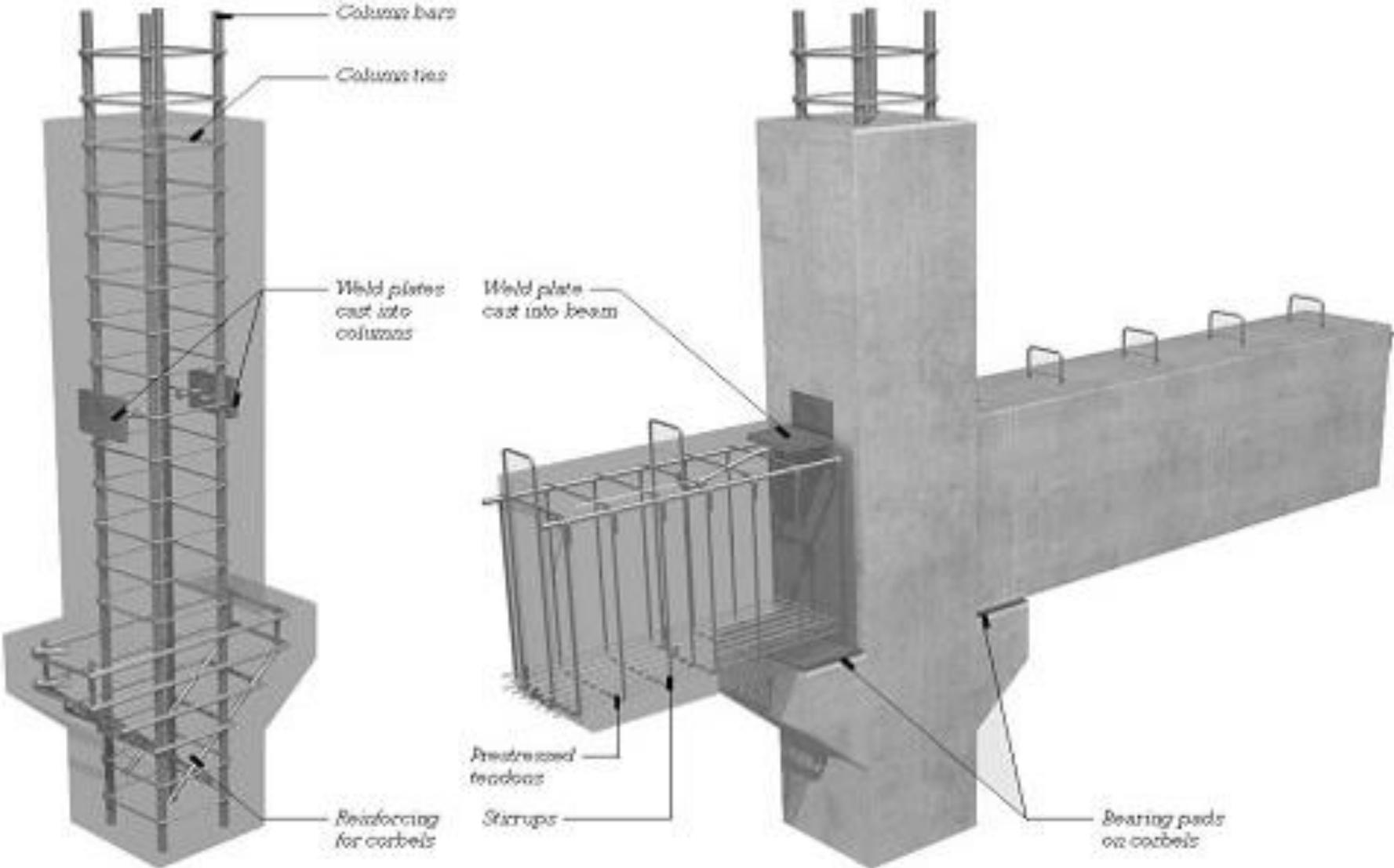
แบบขยายรูปร่างเหล็ก (STEEL BRACKET)



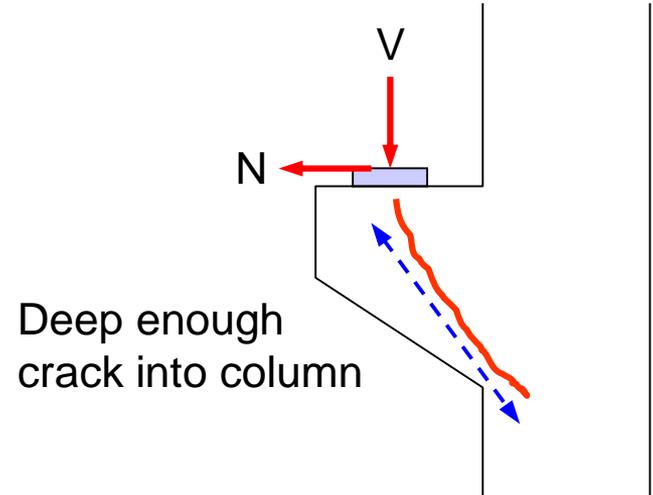
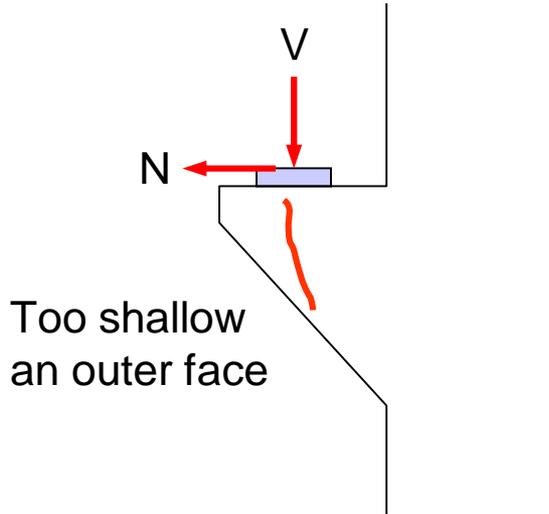
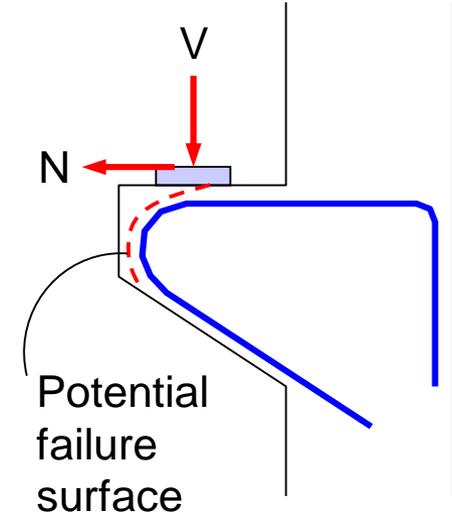
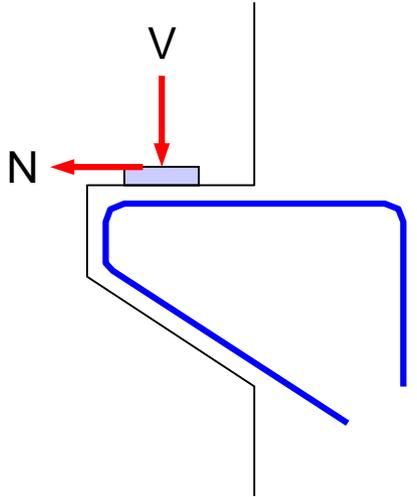
การวิบัติของเหล็กยึดเกิดการขาดที่จุดตัดเหล็ก
(รูปร่างวิบัติ 13ตัวจากทั้งหมด 14ตัว)

Beam-Column Connection

Precast Concrete Structure



Types of Failure



The bracket may fail by

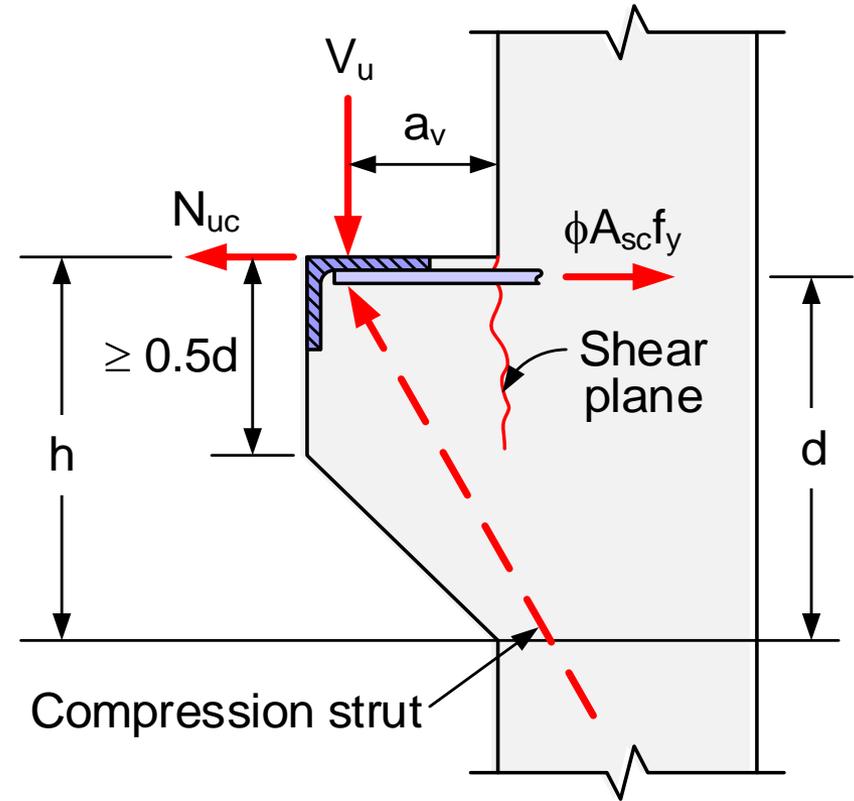
- Shearing along interface between column and bracket
- Yielding of tension tie
- Crushing or splitting of compression strut
- Localized bearing or shearing failure under loading plate

The method of design is valid for

- $a_v/d \leq 1.0$
- $N_{uc} \leq V_u$

For normal weight concrete, V_u/ϕ shall not exceed the least of :

- (a) $0.2f'_c b_w d$
- (b) $(33.8 + 0.08f'_c)b_w d$
- (c) $112.7b_w d$

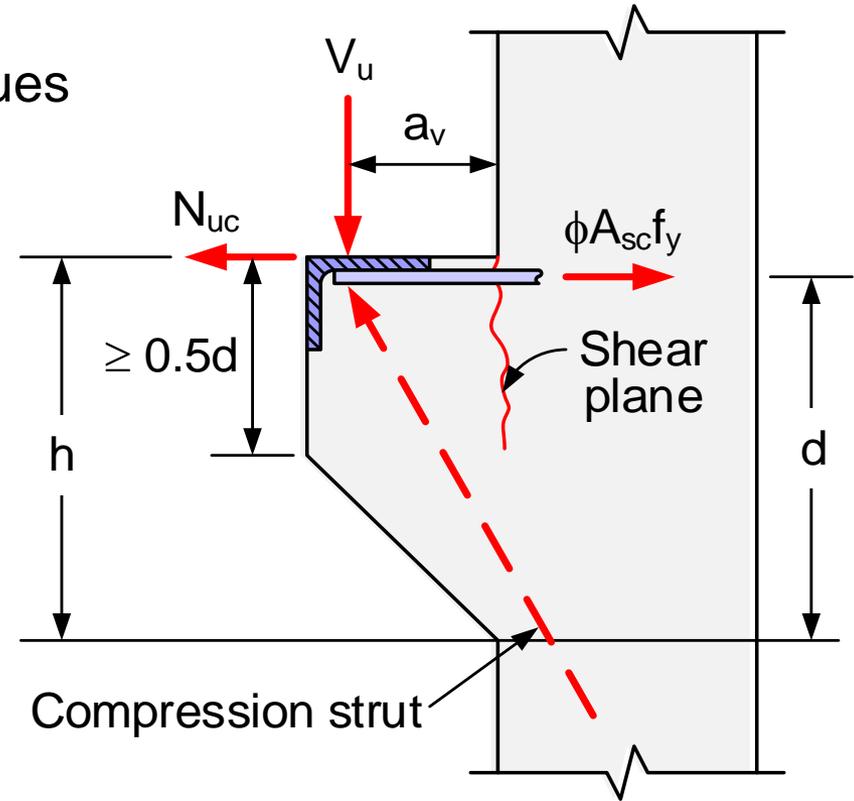


Required Strength

ACI 318-19

- V_u and N_{uc} shall be the maximum values of the factored load combinations
- Horizontal tensile force acting on bracket shall be treated as a live load when computing N_{uc}
- Unless tensile forces are prevented from being applied to the bracket, N_{uc} shall be at least $0.2V_u$
- The factored moment M_u is given by

$$M_u = V_u a_v + N_{uc} (h - d)$$



▶ Design strength $\phi S_n \geq U$:

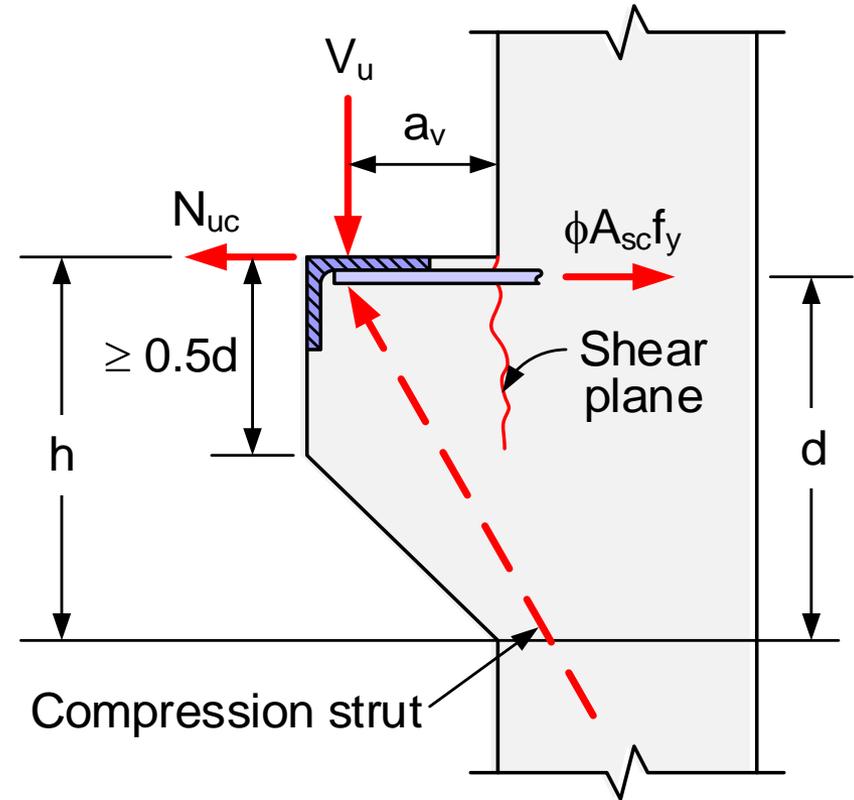
- $\phi N_n \geq N_{uc}$
- $\phi V_n \geq V_{uc}$
- $\phi M_n \geq M_u$

▶ Strength reduction factor $\phi = 0.75$

▶ Nominal tensile strength $N_n = A_n f_y$

▶ Nominal shear strength $V_n = \mu A_{vf} f_y$
for concrete monolithically $\mu = 1.4$

▶ Nominal moment strength $M_n = A_f f_y \left(d - \frac{a}{2} \right) \approx A_f f_y (0.9d)$



- ▶ Steel to resist tensile force: $A_n = \frac{N_{uc}}{\phi f_y}$

- ▶ Steel to resist bending moment:

$$A_f = \frac{M_u}{\phi f_y (d - a/2)}$$

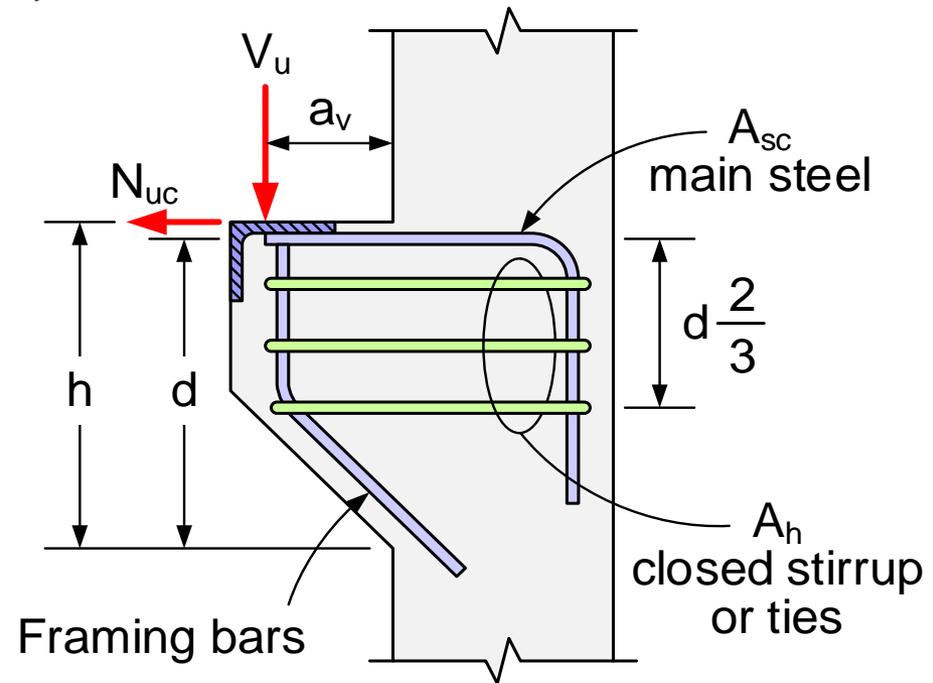
- ▶ Steel to resist shear force:

$$A_{vf} = \frac{V_u}{\phi \mu f_y}$$

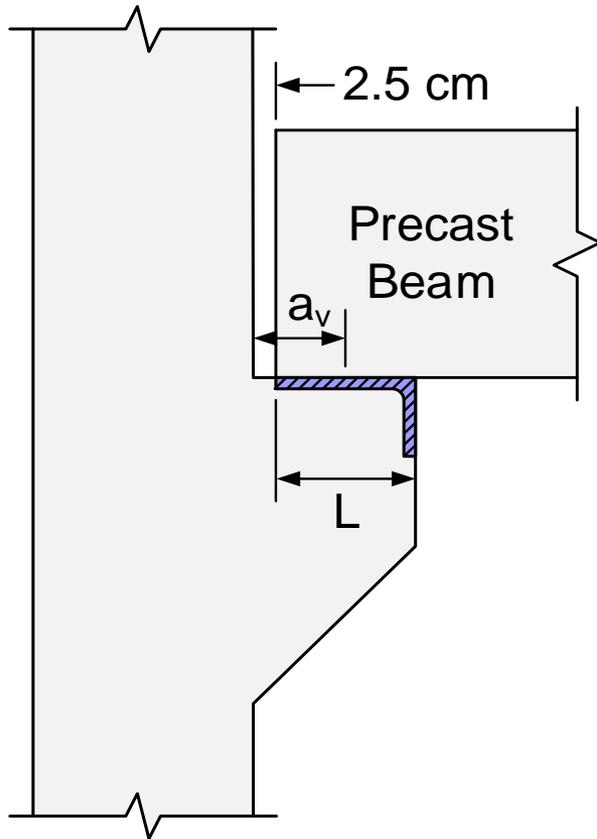
- ▶ Total steel A_{sc} @ top of bracket shall be at least the greatest of :

- $A_f + A_n$
- $(2/3) A_{vf} + A_n$
- $0.04 (f'_c / f_y) b_w d$

- ▶ Total steel A_h of ties shall be at least : $A_h = 0.5 (A_{sc} - A_n)$



ตัวอย่างที่ 1 ออกแบบหูช้างที่ยื่นจากเสากว้าง 35 ซม. รับน้ำหนักคงที่ 14 ตัน น้ำหนักจร 18 ตัน สมมุติให้มีการจัดเตรียมจุดรองรับของคานเสริมเหล็กอัดแรงอย่างเหมาะสมทำให้สามารถขจัดแรงที่จะเกิดในแนวนอน ช่องว่างระหว่างปลายคานและผิวของเสาเท่ากับ 2.5 ซม. กำหนด $f'_c = 240$ กก./ชม.² และ $f_y = 4,000$ กก./ชม.²



วิธีทำ (1) Factored loads:

$$V_u = 1.4 \times 14 + 1.7 \times 18 = 50.2 \text{ ton}$$

$$N_{uc} = 0.2V_u = 0.2 \times 50.2 = 10.0 \text{ ton}$$

Bearing length $V_u / \phi = (0.85f'_c)A_1 = (0.85f'_c)bL$

$$L = \frac{50.2 \times 1,000}{0.70 \times 0.85 \times 240 \times 35} = 10.0 \text{ cm}$$

$$a_v = 5.0 + \frac{1}{2}L = 10.0 \text{ cm}$$

(2) Depth of Bracket : from max. V_u / ϕ criteria

(a) $0.2f'_c b_w d = 48 b_w d \rightarrow$ control

(b) $(33.8 + 0.08f'_c) b_w d = 53 b_w d$

(c) $112.7 b_w d$

From $V_u / \phi = 48 b_w d$

$$\min d = \frac{V_u}{\phi(48b_w)} = \frac{50.2 \times 1,000}{0.75 \times 48 \times 35} = 39.8 \text{ cm}$$

ใช้ความลึก $h = 45$ ซม. $\rightarrow d = 40$ ซม.

$$\frac{a}{d} = \frac{10}{40} = 0.25 < 1.0 \quad \text{OK}$$

(3) Steel Reinforcement :

$$A_{vf} = \frac{V_u}{\phi f_y \mu} = \frac{50.2}{0.75 \times 4.0 \times 1.4} = 12.0 \text{ cm}^2$$

$$A_n = \frac{N_{uc}}{\phi f_y} = \frac{10.0}{0.75 \times 4.0} = 3.33 \text{ cm}^2$$

$$\begin{aligned} M_u &= V_u a_v + N_{uc} (h - d) = 50.2 \times 10 + 10.0(45 - 40) \\ &= 542 \text{ ตั๊น-ซม.} = 5.42 \text{ ตั๊น-เมตร} \end{aligned}$$

$$A_f = \frac{M_u}{\phi f_y j d} = \frac{542}{0.75 \times 4.0 \times 0.9 \times 40} = 5.02 \text{ cm}^2$$

▶ Total steel A_{sc} @ top of bracket shall be at least the greatest of :

$$(a) \quad A_f + A_n = 5.02 + 3.33 = 8.35 \text{ cm}^2$$

$$(b) \quad (2/3)A_{vf} + A_n = (2/3)(12.0) + 3.33 = 11.33 \text{ cm}^2 \rightarrow \text{control}$$

$$(c) \quad 0.04(f'_c/f_y)b_w d = 0.04\left(\frac{240}{4,000}\right)(35)(40) = 3.36 \text{ cm}^2$$

ดังนั้นใช้ A_{sc} : **3-DB25** ($A_s = 14.73 \text{ ซม}^2$)

▶ Total steel A_h of ties shall be at least :

$$A_h = 0.5(A_{sc} - A_n) = 0.5(14.73 - 3.33) = 5.90 \text{ cm}^2$$

เลือกใช้ปลอกปิด **3-DB12** ($A_h = 2(3)(1.13) = 6.79 \text{ ซม}^2$)

เชื่อม DB25

ติดใต้เหล็กฉาก

10 cm

$a = 10 \text{ cm}$

ระยะฝัง = $35 - 5 - 0.8$
= 29.2 ซม.

3-DB25

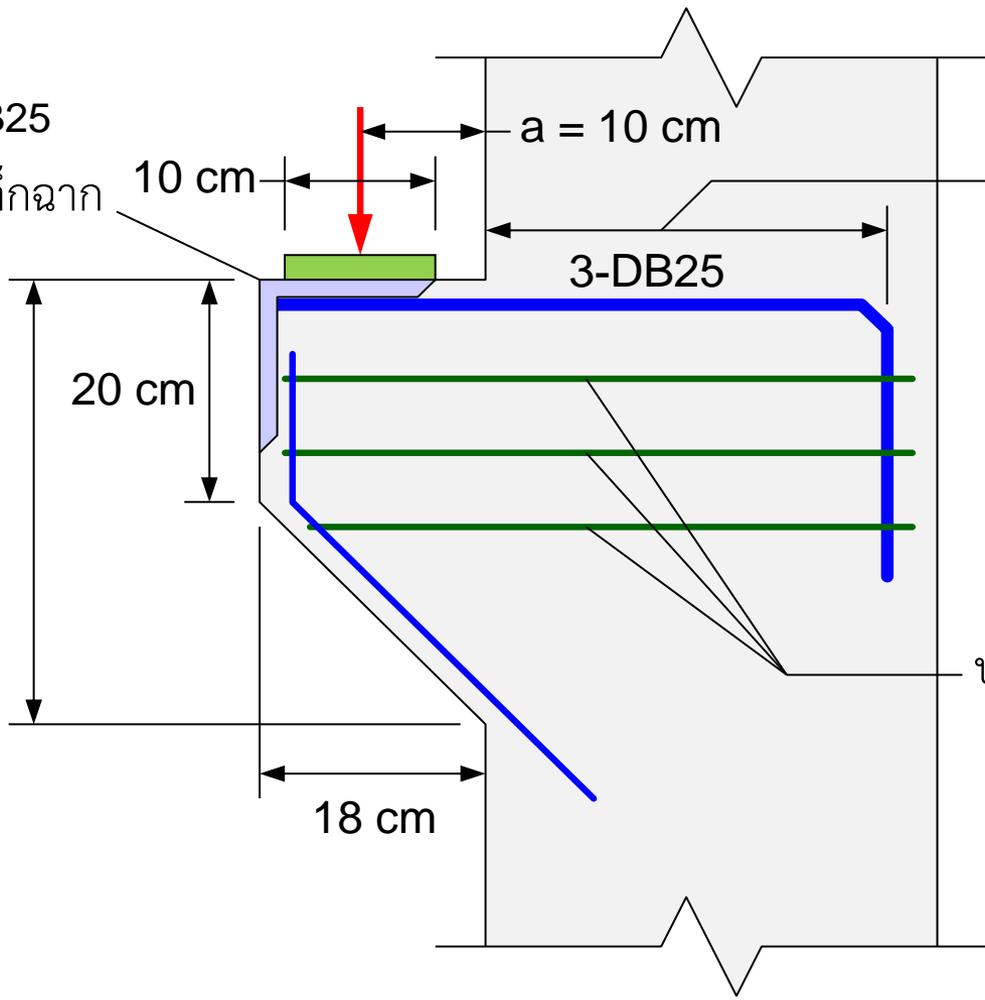
ตรวจสอบว่าเพียงพอหรือไม่?

20 cm

45 cm

ปลอก DB12 @ 7.5 ซม.

18 cm



End of Lecture