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PMI

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Algebra I

Graphing Linear Equations

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Any equation must have at least one variable.

Linear equations have either one or two variables and may also have a constant.

The variables in a linear equation are not raised to any power (beyond one); they are not squared, cubed, etc.

The standard form of a linear equation is

$$Ax + By = C$$

Where:

- x and y are variables
- *A* and *B* are coefficients and *C* is a constant
- A, B and C are integers
- · $A \ge 0$

There are an infinite number of solutions to a linear equation.

In general, each solution is an ordered pair of numbers representing the values for the variables that make the equation true.

For each value of one variable, the value of the other variable is determined.

The fact that the solutions of linear equations are part of an infinite set of ordered pairs led to the idea that those pairs could be treated as points on a graph, and that those points would then form a line.

This reasoning is why these types of equations are called "Linear Equations."

The idea of merging algebra and geometry led to analytic geometry in the mid 1600's.

Analytic Geometry

- is a powerful combination of algebra and geometry.
- was independently developed and published in France during 1637 by René Descartes and Pierre de Fermat.
- The Cartesian Plane is named for Descartes.



How would you describe to someone the location of these five points so they could draw them on another piece of paper without seeing your drawing?

Discuss.

Math Practice

Adding this Cartesian coordinate plane makes the previous task simple since the location of each point can be given by just two numbers:

an *x*- and *y*-coordinate, written as an ordered pair (x, y).



With the Cartesian Plane providing a graphical description of locations on the plane, solutions of equations (noted in ordered pairs) can be analyzed using algebra.



The Cartesian Plane is formed by the intersection of the *x*-axis and *y*-axis, which are perpendicular. It's also called a Coordinate Plane or an *XY* Plane.

The <u>x-axis</u> is horizontal (side-to-side) and the <u>y-axis</u> is a vertical (up and down).

The axes intersect at the <u>origin</u>, (0, 0).



An ordered pair represents a solution to a linear equation, and a point on the plane.

The numbers represent the *x*- and *y*- coordinates, (x, y).

The point (4, 8) is shown.



A <u>linear equation</u> has an infinite set of solutions.

Graphing the pairs of xand y values which satisfy a linear equation forms a line (hence the name "linear" equation).



One way to graph the line that represents the solutions to a linear equation is to use a table to find a few sets of solutions.

Since a line is uniquely defined by any two points, finding three or more points provides the line and a check to make sure the points are correct.



Let's graph the line

y = 2x + 3

We'll make a table, pick some *x*-values and then calculate the matching *y*-values to create ordered pairs to graph.

We can pick any values for x, but we will choose them so that the resulting points:

- · are easy to plot.
- are far enough apart to allow us to draw an accurate line.







While we only need two points to determine the line, it's good to check with some extra points.

Use the equation to fill in the *y*-values in the table.





These are just a few points on the line.

There are an infinite number of ordered pairs that satisfy the equation.



Let's draw the line that represents the infinite set of solutions to this equation.

$$y = 2x + 3$$

The arrows on both ends of the line indicate that it continues forever in both directions.

Because it is a line, it includes an infinite number of points representing all the real numbers.







Note: click to reveal

Click on the points that are integers and the line to graph

- 1 Given the equation, y = 2x 5, what is y when x = 0?
- ○**A** -7
- **○**B -5
- OC −3
- $\bigcirc \mathsf{D} = 0$
- OE I need help



https://njctl.org/video/?v=7ZH9ROiOr_w

- 2 Given an equation of y = 2x 5, what is y if $x = \frac{1}{2}$?
 - ○A -5
 - Ов −4
 - OC −1
 - **OD** 7
 - OE I need help



https://njctl.org/video/?v=5vHwy0E5JeM

3 Is (3, -5) on the line y = 2x - 12?

- OA Yes
- OB No
- ○C Not enough information
- ○D I need help





https://njctl.org/video/?v=AFdcmY86gVU

4 Which point is on the line 4y - 2x = 0?

$$\bigcirc A (-2,1) \bigcirc B (0,1) \bigcirc C (-2,-1) \bigcirc D ^{(1,2)}$$

 \bigcirc E I need help



https://njctl.org/video/?v=_prlhQTNF94

5 Which point lies on the line whose equation is 2x - 3y = 9?

$$\bigcirc A$$
 (0,3)
 $\bigcirc B$ (-3,1)
 $\bigcirc C$ (-3,0)
 $\bigcirc D$ (6,1)

 \bigcirc E I need help



https://njctl.org/video/?v=cHDzJjEErqM

6 Point (k, -3) lies on the line x - 2y = -2.

What is the value of *k*?

- ○A -8
- ⊙в -6
- **○C** 6
- OD 8
- OE I need help



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Graphing Linear Equations Using Intercepts



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x- and *y*- intercepts

To graph a line, two points are required. One technique uses the *x*- and *y*- intercepts.

The *x*-intercept is where a graph of an equation passes through the *x*-axis. The coordinates of the *x*-intercept are (a, 0), where *a* is any real number.

The *x*-intercept of the linear equation shown is (2, 0).



x- and *y*- intercepts

required. One technique uses the *x*- and *y*- intercepts. The *y*-intercept is where a graph of an equation passes through the *y*-axis. The coordinates of the *y*-intercept are (0, b), where b is any real number.

The *y*-intercept of the linear equation shown is (0, -2).



7 What is the *y*-intercept of this line?



8 What is the *x*-intercept of this line?



9 What is the *y*-intercept of this line?



https://njctl.org/video/?v=6kIYu90VIIU

10 What is the *y*-intercept of this line? A(-1,0))B (1,0) Hŧ)C (0,1) D(0,-1)Т JE I need help X Ð 10 1 5 10

https://njctl.org/video/?v=TWOXhjUUctw

11 What is the *x*-intercept of this line?



12 What is the *x*-intercept of this line?



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Graphing Linear Equations Using Intercepts

The technique of using intercepts works well when an equation is written in Standard Form.

Recall that a linear equation written in standard form is Ax + By = C, where A, B, and C are integers and $A \ge 0$.



https://njctl.org/video/?v=FY0lWItpNqw
Example: Find the *x*- and *y*-intercepts in the equation 3x + 5y = 15. Then graph the equation.

x-intercept: Let y = 0: 3x + 5(0) = 15 3x + 0 = 15 3x = 15x = 5 so the x-intercept is (5,0).

y-intercept: Let x = 0: 3(0) + 5y = 15 0 + 5y = 15 5y = 15y = 3 so the y-intercept is (0,3).

Example: Find the *x*- and *y*-intercepts in the equation 3x + 5y = 15. Then graph the equation.

x-intercept is $\frac{}{Click}$ y-intercept is $\frac{}{Click}$

Click on the points & the line in the coordinate plane to reveal.



Example: Find the *x*- and *y*-intercepts in the equation 4x - 3y = 12. Then graph the equation.

x-intercept: Let y = 0:

y-intercept: Let x = 0:





Example: Find the *x*- and *y*-intercepts in the equation 4x - 3y = 12. Then graph the equation.

x-intercept is $\frac{}{Click}$

y-intercept is

Click on the points & the line in the coordinate plane to reveal.



Does anyone see a shortcut to finding the *x*- and *y*- intercepts?How could your shortcut make the problem easier?

Given the equation 4x - 3y = 12, another way to look at the intercept method is called the "cover-up method."

If y = 0, we can cover -3y up (because zero times anything is 0) and solve the remaining equation.

$$4x - 3y = 12_{-}$$
 press $-3y$

that leaves us with

Click

Then solve for *x*.

the *x*-intercept is

Click

If x = 0, we can cover that up and solve the remaining equation.



Try This:

Find the *x*- and *y*intercepts of y = 3x - 9. Then graph the equation.

Click on the points & the line in the coordinate plane to reveal.



- 13 Given the equation $y = \frac{1}{2}x 7$, what is the *x*-intercept?
 - $\bigcirc A$ (3.5,0) $\bigcirc B$ (14,0)
 - ^OC (0,3.5)
 - OD (0,14)
 - \bigcirc E I need help



Answer

https://njctl.org/video/?v=5x5ELpRaGLc

- 14 Given the equation $y = \frac{1}{2}x 7$, what is the *y*-intercept?
 - $\bigcirc A (0,-7)$ $\bigcirc B (14,0)$ $\bigcirc C (0,7)$ $\bigcirc D (0,14)$
 - ○E I need help



https://njctl.org/video/?v=cWPmI7YQE1I

- 15 Given the equation y-3 = 4(x+2), what is the *x*-intercept?
 - $O_{A}(11,0)$
 - ○B (2,0)
 - ^OC (−3,0)
 - ○D (-2.75,0)
 - ○E I need help



https://njctl.org/video/?v=7TdjzyvAL3w

16 Given the equation y-3 = 4(x+2), what is y-intercept?

 $\bigcirc A$ (0,11) $\bigcirc B$ (0,2) $\bigcirc C$ (0,-3) $\bigcirc D$ (0,-2.75) $\bigcirc E$ I need help





https://njctl.org/video/?v=m7QoLR40oz4

- 17 Given the equation x + 3y = 3, what is the *y*-intercept?
 - $O_{A(3,0)}$
 - ^OB (0, 1)
 - ^OC (0, 4)
 - ^OD (0, 3)
 - ○E I need help



https://njctl.org/video/?v=K80OnkftVb4

- 18 Given the equation x + 3y = 3, what is the *x*-intercept?
 - ○A (3,0)
 ○B (0,1)
 ○C (0,4)
 ○D (0,3)
 - OE I need help



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Horizontal and vertical lines are different from slanted lines in the coordinate plane.

A vertical line goes "up and down."

Select random points on each line shown to the left.

What are the similarities and differences between the points on the vertical lines?



Discuss!

Notice that each point on the line furthest to the left all have *x*-coordinates of -7. Examples of points on this line are (-7,2), (-7,0),(-7,-3), etc.

The same holds true for the points on all of the vertical lines that follow. What is the common *x*-coordinate shared on the remaining lines?



A **vertical line** has the equation x = a, where *a* is the *x*-intercept and the common *x*-coordinate shared by all of the points on the line.

Notice that no "y" is contained in the equation.



A horizontal line goes "sideways."

Select random points on each line shown to the left.

What are the similarities and differences between the points on the horizontal lines?

Discuss!



Notice that each point on the top line have *y*coordinates of 10. Examples of points on this line are (-5,10), (-2,10), (0,10), etc.

The same holds true for the points on all of the horizontal lines that follow. What is the common *y*-coordinate shared on the remaining lines?



A **horizontal line** has the equation y = b, where bis the *y*-intercept and the common *y*-coordinate shared by all of the points on the line.

Notice that no "x" is contained in the equation.



19 Is the following equation that of a vertical line, a horizontal line, neither, or cannot be determined?

$$y = 4$$

- ○A Vertical
- B Horizontal
- OC Neither
- O D Cannot be determined
- OE I need help



https://njctl.org/video/?v=6eepxxqH-Zc

20 Is the following equation that of a vertical line, a horizontal line, neither, or cannot be determined?

$$x + 2y = 9$$

- QA Vertical
- **OB** Horizontal
- ○C Neither
- **OD** Cannot be determined
- OE I need help



https://njctl.org/video/?v=KkLWm1co6Sk

21 Is the following line that of a vertical, a horizontal, neither, or cannot be determined?

$$x = -23$$

- QA Vertical
- **B** Horizontal
- OC Neither
- **OD** Cannot be determined
- OE I need help



https://njctl.org/video/?v=AUm2VhzHjrk

Answer

22 Is the following equation that of a vertical line, a horizontal line, neither, or cannot be determined:

$$2x - 3 = 0$$

- QA Vertical
- **B** Horizontal
- OC Neither
- OD Cannot be Determined
- OE I need help



https://njctl.org/video/?v=WjeEkEaP2Qo

- 23 Which statement describes the graph of x = 3?
 - $\bigcirc A$ It passes through the point (0,3)
 - \bigcirc B It is parallel to the *y*-axis
 - \bigcirc C It is parallel to the *x*-axis
 - OD I need help



https://njctl.org/video/?v=DJJWr4ikucE

24 The intercepts method (cover-up method) of graphing could NOT have been used to graph which of the following lines?



25 Which of the following equations can't be graphed using the intercepts method?

$$V = -3 \qquad \forall y = 4x + 7$$

$$V = 4x + 7$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = -3x \qquad \forall x = 2y - 8$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 2y - 8$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V = 3x - 4y = 12$$

$$V = 4x + 7$$

$$V =$$

Answer





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Slope of a Line



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Slopes and Points

It's possible, and often easier, to graph lines using a slope and a point as opposed to a table.

Also, it's not difficult to write an equation for a line from finding the slope and a point from a graph.

Let's first define *slope*, and then we can use that idea.

The **slope** of a line is a number that describes both the direction and steepness of a line. The letter *m* is typically used as the variable for slope.

The slope of a line can have 4 types of direction:

- positive: rising from left to right
 negative: falling from left
- negative: falling from left to right
- zero: horizontal
- undefined: vertical
- To measure the steepness of a line we use the ratio of "rise" over "run."



The "rise" is the change in the value of the *y*-coordinate while the "run" is the change in the value of the *x*-coordinate.

The symbol for "change" is the Greek letter delta, " Δ ," which just means "change in."

So the slope is equal to the change in *y* divided by the change in *x*, or Δy divided by Δx ... delta *y* over delta *x*.

$$m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$



$$m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

In this case:

The rise is from 4 to 11 $\Delta y = 11 - 4 = 7$

And the run is from 2 to 8, $\Delta x = 8 - 2 = 6$

So the slope is

$$m = \underline{\Delta y} = \underline{7}$$
$$\underline{\Delta x} = 6$$



Any points on the line can be used to calculate its slope, since the slope of a line is the same everywhere.

The values of Δy and Δx may be different for other points, but their ratio will be the same.

You can check that with the red and green triangles shown here.

$$m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$



Slope is also referred to as a constant rate of change. Here is an application of slope:

A road might rise 1 foot for every 10 feet of horizontal distance.



The ratio, $\frac{1}{10}$, which is also called slope, is a measure of the

steepness of the hill. Engineers call this use of slope **grade** and measure the grade with percentages. The grade of the road above is 10%.
Slope

Horizontal and vertical lines have special slopes. A horizontal line has a slope of 0, and a vertical line has an undefined slope. Let's see what makes these slopes special.

Two points on the horizontal line are (0, 4) and (3, 4). If we look at the graph, the Δy is 0 and the Δx is 3,

SO
$$m = \frac{0}{3} = 0$$
.

Slope of horizontal & vertical lines using Rise & Run



Slope

Horizontal and vertical lines have special slopes. A horizontal line has a slope of 0, and a vertical line has an undefined slope. Let's see what makes these slopes special.

Two points on the vertical line are (7, 0) and (7, 2). If we look at the graph, the Δy is 2 and the Δx is 0, so...

 $m = \frac{2}{0} =$ undefined because you can't divide by 0.

Slope of horizontal & vertical lines using Rise & Run



- 26 The slope of the indicated line is:
 - ○A negative
 - \bigcirc B positive
 - \bigcirc C zero
 - $^{\bigcirc}$ D undefined
 - ○E I need help





https://njctl.org/video/?v=ZxaVmzQ9gcE

27 The slope of the indicated line is:

- ○A negative
- ○B positive
- \bigcirc C zero
- OD undefined
- ○E I need help





https://njctl.org/video/?v=e3nlqCjF9nA

28 The slope of the indicated line is:

- ○A negative
- \bigcirc B positive
- \bigcirc C zero
- ○D undefined
- \bigcirc E I need help





https://njctl.org/video/?v=HZkMNeZX09s

29 The slope of the indicated line is:

- ○A negative
- \bigcirc B positive
- \bigcirc C zero
- \bigcirc D undefined
- \bigcirc E I need help





https://njctl.org/video/?v=Jg0skDh5wBw

- 30 The slope of the indicated line is:
 - ○A negative
 - ○B positive
 - ○C zero
 - \bigcirc D undefined
 - ○E I need help





https://njctl.org/video/?v=WrgIU7Ryseo

- 31 The slope of the indicated line is:
 - ○A negative
 - OB positive
 - ○C zero
 - \bigcirc D undefined
 - ○E I need help



Answer



https://njctl.org/video/?v=QRJ_MuQ3Jkg







https://njctl.org/video/?v=iV9i8hE2xGg

33 What's the slope of this line?

$$\bigcirc A \ m = -\frac{1}{2}$$
$$\bigcirc B \ m = \frac{1}{2}$$
$$\bigcirc C \ m = 2$$
$$\bigcirc D \ m = -2$$

 \bigcirc E I need help





https://njctl.org/video/?v=fjsrKWIYmNc

of this line? $\bigcirc A m = 6$ $\bigcirc \mathsf{B} \ m = 1$ \bigcirc **C** m = 0**D** undefined \bigcirc E I need help





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35 What's the slope of this line?

$$\bigcirc A \ m = -\frac{3}{5}$$
$$\bigcirc B \ m = \frac{3}{5}$$
$$\bigcirc C \ m = -\frac{5}{3}$$
$$\bigcirc D \ m = \frac{5}{3}$$

 \bigcirc E I need help





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https://njctl.org/video/?v=m3BcuVoX4So

- 37 What is the slope of this line?
- $\bigcirc A m = 3$
- $\bigcirc \mathsf{B} \ m = 1$
- \bigcirc **C** m = 0
- \bigcirc D undefined
- ○E I need help





https://njctl.org/video/?v=pi16cFdRems

38 What is the slope of the line passing through the indicated points?



○E I need help







Answer

Slope

Let's try an example that does not have a graph.

Calculate the slope of the line that passes through (-5, 4) and (5, 0).

First identify (-5, 4) as your (x_1, y_1) and (5, 0) as your (x_2, y_2) .

Second, substitute your numbers into the slope formula for their assigned variables.

$$\frac{0-4}{5-(-5)} = \frac{0-4}{5+5} = \frac{-4}{10} = \frac{-2}{5}$$



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39 What is the slope of the line through A(-2,1)

and B(3, -1)? $\bigcirc A m = -\frac{2}{5}$ \bigcirc B m = -2 $\bigcirc \mathbf{C} \quad m = 0$ **D** undefined \bigcirc ○ E I need help



https://njctl.org/video/?v=GMoj9-tyvRY

40 What is the slope of MN given M(1,7) and N(3,-4)?

$$\bigcirc A \quad m = -\frac{6}{7}$$
$$\bigcirc B \quad m = -\frac{2}{11}$$
$$\bigcirc C \quad m = -\frac{11}{2}$$
$$\bigcirc D \quad m = -\frac{7}{6}$$

\bigcirc E I need help



https://njctl.org/video/?v=tKuQsMYp5h4

- 41 What is the slope of the line containing (-1, 7) and (3, -7)? $\bigcirc A \quad m = -7$ $\bigcirc B \quad m = -\frac{7}{2}$ $\bigcirc C \quad m = \frac{7}{2}$
- Answer

 \bigcirc E I need help

 \bigcirc D m = 2



https://njctl.org/video/?v=pJFHjRuL2Mc

42 What is the slope of the line that passes through the points (3,5) and (-2,2)?

 $O_{A \frac{1}{5}}$

 $O_{\mathsf{B}} \frac{3}{5}$

 $OC\frac{5}{3}$

OD5

○E I need help



https://njctl.org/video/?v=Up1DD3EpsmY

43 A straight line with a slope of 5 contains the points (1, 2) and (3, k). Find the value of k.

- $\bigcirc A \ k = 12$
- $\bigcirc \mathsf{B} \ k = 5$
- $\bigcirc \mathbf{C} \quad k = 2$
- $\bigcirc \mathsf{D} \ k = 0$
- \bigcirc E I need help



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Constant Rate of Change

Slope formula can be used to find the **constant rate of change** in a "real world" problem.

When traveling on the highway, drivers will set the cruise control and travel at a constant speed this means that the distance traveled is a constant increase.

The graph at the right represents such a trip. The car passed mile-marker 60 at 1 hour and mile-marker 180 at 3 hours. Find the slope of the line and what it represents.

 $m = \frac{180 \text{ miles} - 60 \text{ miles}}{3 \text{ hours} - 1 \text{ hour}} = \frac{120 \text{ miles}}{2 \text{ hours}} = \frac{60 \text{ miles}}{\text{hour}}$

So the slope of the line is 60 and the rate of change of the car is 60 miles per hour.





Constant Rate of Change

If a car passes mile-marker 100 in 2 hours and mile-marker 200 in 4 hours, then how many miles per hour is the car traveling?

Use the information to write ordered pairs (2, 100) and (4, 200).

44 If a car passes mile-marker 90 in 1.5 *hours* and mile-marker 150 in 3.5 *hours*, how many miles per hour is the car traveling?

 $\bigcirc A$ 60 miles per hour

 \bigcirc B 30 miles per hour

 \bigcirc C 2 miles per hour

 \bigcirc D 40 miles per hour

○E I need help



https://njctl.org/video/?v=z6VrrwLx6_0

45 How many meters per second is a person running if they are at 10 *meters* in 6 *seconds* and 100 *meters* in 15 *seconds*?

- \bigcirc A 90 meters per second
- $\bigcirc \mathsf{B}$ 10 meters per second
- \bigcirc C 9 meters per second
- \bigcirc D 0.9 meters per second
- ○E I need help





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A useful form of the equation of a line is the pointslope form. It's equation is $y - y_1 = m(x - x_1)$.

It's based on the use of the slope and any point that is on the line.

This equation is the most effective when you are given the slope and a point on the line because you can use it to write the equation in multiple forms.

Let's get started.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Point-slope form starts using the definition of slope, in which two points on a line are given by the ordered pairs

$$(x_1, y_1)$$
 and (x_2, y_2) .

As a first step, let's just name the coordinates for the second point (x, y) rather than (x_2, y_2) .

That will be true for any point on the line, not just one point, and will allow us to write an equation for all points on the line.

Then our slope formula becomes:

$$m = \frac{y - y_1}{x - x_1}$$

$$m = \frac{y - y_1}{x - x_1}$$

Now let's solve that equation for *y* using what we've learned about solving equations.

Try it yourself, before we show you our answer.

(**Hint**: Remember to treat the denominator $(x - x_1)$ like it's in parentheses.)

$$m = \frac{y - y_1}{x - x_1}$$

 $m(x-x_1) = y - y_1$ Multiply both sides by $(x-x_1)$ to get rid of the fraction.

 $y - y_1 = m(x - x_1)$ The last step is to switch the expressions to the opposite sides of the equals sign.

$$y - y_1 = m\left(x - x_1\right)$$

Point-Slope Form where:

- m is the slope,
- · (x_1, y_1) is any of the infinite points that satisfy the equation.

$$y - y_1 = m\left(x - x_1\right)$$

If you are provided a graph of a line, you can calculate m and locate a point directly from the graph.

That allows you to write the equation of the line directly, which you can then use to find any other needed points.

For instance, if I know that the equation of a line is y-2=2(x-1), then one point on the line is (1,2) and the slope of the line is 2. Using this information, I can find a second point, and then draw the line.



I do this by recognizing that the slope of 2 means that if I go up 2 units on the *y*-axis I have to go 1 unit to the right on the *x*-axis.

Or if I go up 10, I have to go over 5 units, etc.



Then I draw the line through any two of those points.

This method is the easiest to use if you just have to draw a line given a point and slope.




Using Point-Slope to Draw a Line

Example: Given the equation

 $y+4=\frac{1}{3}(x+2)$

Determine the point on the line and the slope. The point on the line is <u>click</u>

The slope is ______

Graph the line representing the equation.

Click on the point to reveal it. Click slightly above it to show the slope. Click on the new point. Click in between to reveal the line.



46 What is the slope of y-3 = 4(x+2)?

- $\bigcirc A \quad m = 2$
- $\bigcirc \mathsf{B} \quad m = 4$
- \bigcirc C m = -3
- $\bigcirc \mathsf{D} \quad m = 8$
- OE I need help



https://njctl.org/video/?v=bmCwg4j9XeU

47 Which point is on the line y-3 = 4(x+2)?

$$\begin{array}{c} \bigcirc \mathsf{A} \\ (-3,2) \\ \bigcirc \mathsf{B} \\ (3,-2) \\ \bigcirc \mathsf{C} \\ (2,-3) \\ \bigcirc \mathsf{D} \end{array}$$

○E I need help



https://njctl.org/video/?v=uZK7jukoCJs

48 What is the slope and a point on the line y+5=-3(x-4)?

○E I need help



https://njctl.org/video/?v=Pfm_vI_Zc24

49 Which is the slope and a point on the line

$$y-1=\frac{1}{3}(x)?$$

$$\bigcirc A \qquad m = \frac{1}{3}; (-1, 0)$$
$$\bigcirc B \qquad m = -\frac{1}{3}; (0, -1)$$
$$\bigcirc m = \frac{1}{2}; (0, 1)$$

$$\bigcirc C$$

$$m = \frac{1}{2};$$

$$m = \frac{1}{3}; (0,$$

$$\bigcirc \mathsf{D}$$
 m is undefined; (0,1)



https://njctl.org/video/?v=2hW4RxiaVzA

50 Which line represents y + 5 = -3(x-4)?

 $\bigcirc \mathsf{A}$ Line A

 $\bigcirc \mathsf{B}$ Line *B*

 \bigcirc C Line C

 \bigcirc D Line D

 \bigcirc E I need help



Answer



https://njctl.org/video/?v=AjQ0uuSBpuE

51 Which line represents $y+1 = -\frac{1}{2}(x+5)$?

A Line A
B Line B
C Line C
D Line D
E I need help





https://njctl.org/video/?v=iptLDRXdvLM

52 Which line represents y-6=3(x+4)?

A Line A
B Line B
C Line C
D Line D
E I need help



Answer



https://njctl.org/video/?v=wH8d5lxNP3U

$$y - y_1 = m\left(x - x_1\right)$$

You can determine and graph equations in point-slope form even when you are given limited information.

For example, if you are given the slope (m) and any point (x_1, y_1) , then by substituting the point into the equation for x_1 and y_1 and the slope for m, you have the equation of the line with no additional work required.



https://njctl.org/video/?v=A8-XUx5zrYU

$$y - y_1 = m\left(x - x_1\right)$$

Or, if you are given any two points, it's always possible to determine the slope, m.

By then substituting one of those points in for x_1 and y_1 , write the equation of a line from two points.

Let's clarify the steps required by doing some examples for both cases.

$$y - y_1 = m\left(x - x_1\right)$$

Example:

Write the equation of a line in point-slope form that has a slope of 7 and passes through the point (-9, 3).

We already know that the slope is 7, or m = 7.

We also know that a point that the line passes through is (-9, 3), which represent (x_1, y_1) respectfully.

By substituting these numbers into our equation, we have:

$$y-3 = 7(x-(-9))$$
 or

y-3=7(x+9), which is our equation in point-slope form.

Example:

$$y - y_1 = m\left(x - x_1\right)$$

Write the equation of a line in point-slope form that passes through the points (5, -9) and (3, 0).

This time, we do not know the slope, so we need to calculate it.

$$m = \frac{0 - (-9)}{3 - 5} = \frac{9}{-2} = -\frac{9}{2}$$

We also know that a point that the line passes through is (5, -9), which represent (x_1, y_1) respectfully.

By substituting these numbers into our equation, we have:

$$y - (-9) = -\frac{9}{2}(x-5)$$
 which simplifies to $y+9 = -\frac{9}{2}(x-5)$.

$$y - y_1 = m\left(x - x_1\right)$$

Example:

Write the equation of a line in point-slope form that passes through the points (5, -9) and (3, 0).

You might be asking if the equation on the previous slide is the only answer. Actually, you can also write the equation in point-slope form using the other point (3, 0) as (x_1, y_1) . Therefore, the equation could also be:

$$y - 0 = -\frac{9}{2}(x - 3)$$
, which simplifies to $y = -\frac{9}{2}(x - 3)$.

Point-Slope Form
$$y - y_1 = m(x - x_1)$$

Example:

Write the equation of a line in point-slope form that passes through the points (5, -9) and (3, 0).

The reason that we have two possible answers is because they would both simplify into the same equation in Standard Form. The work for each equation is below.

$$y+9 = -\frac{9}{2}(x-5) \qquad y = -\frac{9}{2}(x-3)$$

$$y+18 = -9(x-5) \qquad 2y = -9(x-3)$$

$$2y+18 = -9x+45 \qquad 2y = -9x+27$$

$$9x+2y+18 = 45 \qquad 9x+2y = 27$$

$$9x+2y = 27$$

53 What is the equation of the line in point-slope form if its slope is -2 and it passes through the point (9, -7).

○A
$$y-7 = -2(x-9)$$

○B $y+7 = -2(x+9)$
○C $y+7 = -2(x-9)$
○D $y-7 = -2(x+9)$
○E I need help



https://njctl.org/video/?v=DgaE5iazZZc

54 What is the equation of the line in point-slope form if its slope is 5 and it passes through the point (-1, -4).

○A
$$y-4 = 5(x-1)$$

○B $y+4 = 5(x+1)$
○C $y+4 = 5(x-1)$
○D $y-4 = 5(x+1)$
○E I need help



https://njctl.org/video/?v=TSTkCqqgapg

55 What is the equation of the line in point-slope form if its

slope is $-\frac{4}{9}$ and it passes through the point (3, 8).

$$\bigcirc A \quad y - 8 = -\frac{4}{9}(x - 3)$$

$$\bigcirc B \quad y + 8 = -\frac{4}{9}(x + 3)$$

$$\bigcirc C \quad y + 8 = -\frac{4}{9}(x - 3)$$

$$\bigcirc D \quad y - 8 = -\frac{4}{9}(x + 3)$$



 \bigcirc E I need help

https://njctl.org/video/?v=S9bzjygcZ5A

56 What is the equation of the line in point-slope form that passes through the points (3, 8) and (-2, -2).

○A y+8=2(x+3)
○B y-8=2(x-3)
○C y+2=
$$\frac{1}{2}(x+2)$$

○D y-2= $\frac{1}{2}(x-2)$

○E I need help



https://njctl.org/video/?v=2bB4afALucg

57 What is the equation of the line in point-slope form that passes through the points (7, 9) and (5, -1).

$$\bigcirc A \ y - 9 = 5(x - 7)$$

$$\bigcirc B \ y - 1 = 5(x - 5)$$

$$\bigcirc C \ y + 1 = \frac{1}{5}(x - 5)$$

$$\bigcirc D \ y - 9 = \frac{1}{5}(x - 7)$$

○E I need help



https://njctl.org/video/?v=xCVrFXRxPF0

58 What is the equation of the line in point-slope form that passes through the points (4, -7) and (-2, -3).

Answei

$$\bigcirc A \ y - 7 = -\frac{3}{2}(x+4)$$

$$\bigcirc B \ y - 3 = -\frac{3}{2}(x-2)$$

$$\bigcirc C \ y + 3 = -\frac{2}{3}(x+2)$$

$$\bigcirc D \ y - 7 = -\frac{2}{3}(x-4)$$

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○E I need help



https://njctl.org/video/?v=sjYbZfMWvn0

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Another very useful form of the equation of a line is the slope-intercept form.

It's based on the use of the slope and the *y*-intercept of a line.

Similar to point-slope, we are going to start by showing a derivation proof of slope-intercept form.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Let's start with the definition of slope, in which two points on a line are given by the ordered pairs

 (x_1,y_1) and (x_2, y_2) .

As a first step, let's just name the coordinates for the second point (x,y) rather than (x_2, y_2) .

That will be true for any point on the line, not just one point, and will allow us to write an equation for all points on the line.

Then our slope formula becomes:

$$m = \frac{y - y_1}{x - x_1}$$

$$m = \frac{y - y_1}{x - x_1}$$

Now let's solve that equation for y using what we've learned about solving equations.

Try it yourself, before we show you our answer.

(**Hint:** Remember to treat the denominator $(x - x_1)$ like it's in parentheses.)

 $m = \frac{y - y_1}{x - x_1}$ Multiply both sides by $(x - x_1)$ to get rid of the fraction.

 $m(x-x_1) = y - y_1$ Now, add y_1 to both sides.

 $m(x-x_1) + y_1 = y$ Now switch the sides.

 $y = m(x - x_1) + y_1$ This is fine, and allows us to graph a line given any point (x_1, y_1) .

But, one additional step is taken to get the most useful equation for a line.

 $y = m(x - x_1) + y_1$ Use the *y*-intercept for (x_1, y_1) .

The *y*-intercept is the point where the line crosses the *y*-axis.

The coordinates of that point are (0, b).

y = mx + b

- *x* is zero anywhere on the *y*-axis
- We name the y-intercept "b."

Then, this becomes: y = mx + b

$$y = mx + b$$

Slope-Intercept Form is where:

- m is the slope,
- b is the y-intercept (0, b)
- (x, y) is any of the infinite points that satisfy the equation.

y = mx + b

This is the form of the equation of a line that is most often used.

If you are provided a graph of a line, you can calculate m and read b directly from the graph.

That allows you to write the equation of the line directly, which you can then use to find any other needed points.

The line shown in the coordinate plane to the left has a *y*-intercept at the point (0, -2) and has a slope

of $\frac{2}{3}$. Therefore, the

equation of this line is

$$y = \frac{2}{3}x - 2.$$



Example: Write the equation for the line shown in the graph to the right.

The slope of the line (m) is

click

click

The *y*-intercept of the line (*b*) is $\underline{\qquad}$

Therefore the equation of the line in slope intercept form is



Example: Write the equation for the line shown in the graph to the right.

The slope of the line (m) is

click

click

The *y*-intercept of the line (*b*) is $\underline{\qquad}_{click}$

Therefore the equation of the line in slope intercept form is



59 What is the equation of the graphed line?

 $\bigcirc A \qquad y = 3x - 1$ $\bigcirc B \qquad y = 3x$ $\bigcirc C \qquad y = 3x + 1$ $\bigcirc D \qquad y = \frac{1}{3}x + 1$

QE I need help







60 Which equation is that of the graphed line?



QE I need help



Answer



https://njctl.org/video/?v=n62Hdx1tlPs

61 Which equation is that of the graphed line?

$$\bigcirc A \qquad y = 3x - 1$$
$$\bigcirc B \qquad y = 3x$$
$$\bigcirc C \qquad y = 3x + 1$$
$$\bigcirc D \qquad y = \frac{1}{3}x$$

QE I need help





https://njctl.org/video/?v=s9PDW6MLK6c

62 Which equation is that of the graphed line?







Answer

https://njctl.org/video/?v=LzozyfdJTTc

Graphing a Line Using Slope-Intercept Form

Having the equation of a line in slope-intercept form also allows us to quickly graph a line, using the *y*-intercept and the slope.

For instance, if we know that the equation of the line is

 $y = -\frac{1}{2}x + 5$

then we can graph the *y*-intercept (0, 5) and use the slope of $-\frac{1}{2}$ to count the

number of spaces, down 1 unit and right 2 units (or up



one and left 2 units), to get an additional point on the line.



https://njctl.org/video/?v=bFOHbTSr8mo
Graphing a Line Using Slope-Intercept Form

Then we draw the line through any two of those points.

This method is the easiest to use if you just have to draw a line given the *y*-intercept and slope.



63 What is the slope of the linear equation below?

 $y = -\frac{3}{2}x - 5$ $\bigcirc A 5$ OB −5 $\bigcirc C \frac{3}{2}$ $OD -\frac{3}{2}$ ○E I need help



https://njctl.org/video/?v=5-Usujvun2U

64 What is the *y*-intercept of the linear equation below?

$$P = -\frac{3}{2}x - 5$$

$$O = (0, -5)$$

$$O = (0, \frac{3}{2})$$

$$O = (0, -\frac{3}{2})$$

 \bigcirc E I need help



https://njctl.org/video/?v=4ICLPILGwDo

65 Which line in the graph below represents the linear

equation
$$y = -\frac{3}{2}x - 5$$
?

⊖A Red

- OB Blue
- OD Black
- OE I need help



Answer



https://njctl.org/video/?v=MsUJczHETPY

66 What is the slope of the linear equation below?

$$\bigcirc A \quad 5$$

$$\bigcirc B \quad -5$$

$$\bigcirc C \quad \frac{2}{3}$$

$$\bigcirc D \quad -\frac{2}{3}$$

OE I need help



https://njctl.org/video/?v=2Hz9Px9gvLs

67 What is the *y*-intercept of the linear equation below?

 $\bigcirc A (0, 5)$ $y = \frac{2}{3}x + 5$ $\bigcirc B (0, -5)$ $\bigcirc C \left(0, \frac{2}{3}\right)$

 $\bigcirc D \left(0,-\frac{2}{3}\right)$

○E I need help



https://njctl.org/video/?v=uO-wB9tdQl4

68 Which line in the graph below represents the linear equation

$$y = \frac{2}{3}x + 5$$
?

⊖A Red

- OB Blue
- \bigcirc C Purple
- OD Black
- ○E I need help



Answer



https://njctl.org/video/?v=4ptUuIIgwM8

y = mx + b

You can also determine and graph equations in slope-intercept form even when you are given limited information.

For example, if you are given the slope (m) and any point (x, y), then by substituting the point into the equation for x and y, you can solve for b.

Then, you can write the equation of a line when given the slope and a point that the line passes through.



https://njctl.org/video/?v=MrjEcXgOheA

y = mx + b

Or, if you are given any two points, it's always possible to determine the slope, m.

By then substituting one of those points in for x and y, you can solve for b.

Then, you can write the equation of a line from two points.

Let's clarify the steps required by doing some examples for both cases.

y = mx + b

Example:

Write the equation of a line in slope-intercept form that has a slope of 8 and passes through the point (3, 10).

We already know that the slope is 8, or m = 8.

We also know that a point that the line passes through is (3, 10), which represent (x, y) respectfully.

By substituting these numbers into our equation, we have:

10 = 8(3) + b

$$y = mx + b$$

Now, we can solve for b.

10 = 8(3) + b Multiply 8 and 3. 10 = 24 + b Subtract 24 from both sides. -14 = bb = -14 Switch the order.

Our equation is then y = 8x - 14.

Example:

y = mx + b

Write the equation of a line in slope-intercept form that has a slope of 8 and passes through the point (3,10).

This problem can also be solved using point-slope and using the rules of algebra to get it into slope-intercept form. We have our point (3,10) as (x_1, y_1) and our slope of 8. If I substitute the numbers into point-slope, we will get this equation:

y-10 = 8(x-3) Distribute the 8 to x and -3. y-10 = 8x-24 Addition of 10 to both sides y = 8x-14

y = mx + b

Example:

Write the equation of a line in slope-intercept form that passes through the points (4,0) and (6,5).

This time, we do not know the slope, so we need to calculate it.

$$m = \frac{5-0}{6-4} = \frac{5}{2}$$

We also know that a point that the line passes through is (4,0), which represent (x, y) respectfully.

By substituting these numbers into our equation, we have:

$$0 = \frac{5}{2}(4) + b$$

Slope-Intercept Form y = mx + b

Now, we can solve for b.

$$0 = \frac{5}{2}(4) + b$$
 Multiply $\frac{5}{2}$ and 4.

$$0 = 10 + b$$
 Subtract 10 from both sides.

$$-10 = b$$

$$b = -10$$
 Switch the order.

Our equation is then $y = \frac{5}{2}x - 10$.

y = mx + b

Example:

Write the equation of a line in slope-intercept form that passes through the points (4,0) and (6,5).

This problem can also be solved using point-slope and using the rules of algebra to get it into slope-intercept form. We can select one of our

points as (x_1, y_1) and our slope that we calculated was $\frac{5}{2}$. Let's use

(4,0). If we substitute the numbers into point-slope, we will get this equation:

$$y-0=\frac{5}{2}(x-4)$$

Distribute the slope & drop the 0.

$$y = \frac{5}{2}x - 10$$

- 69 What is the equation of the line that passes through the point (-3, -7) and has a slope of 4?
 - A y = 4x + 25○ B y = 4x + 5○ C y = -3x + 5
 - $\bigcirc \mathsf{D} \ y = 7x 17$
 - OE I need help



70 What is the equation of the line that passes through the

point
$$(6, -2)$$
 and has a slope of $\frac{5}{6}$?
 $\bigcirc A \quad y = \frac{5}{6}x - 7$

$$\bigcirc B \ y = \frac{5}{6}x + 7.67$$

$$\bigcirc$$
 C $y = 6x - 7$

$$\bigcirc D \ y = -2x + 7.67$$

○E I need help



https://njctl.org/video/?v=GgstSLpBaFM

71 What is the equation of the line that passes through the point (-1, -8) and has a slope of $-\frac{1}{2}$?

$$\bigcirc A \quad y = -\frac{1}{2}x - 8.5$$

$$\bigcirc \mathsf{B} \ y = -\frac{1}{2}x + 4$$

$$\bigcirc C \quad y = -\frac{1}{2}x - 5$$

$$\bigcirc D \ y = -\frac{1}{2}x - 7.5$$





Answei

72 What is the equation of the line that passes through the points (-1, -8) and (2, 1)?

$$\bigcirc A \quad y = \frac{1}{3}x - \frac{1}{3}$$
$$\bigcirc B \quad y = \frac{1}{3}x + \frac{5}{3}$$
$$\bigcirc C \quad y = 3x - 5$$
$$\bigcirc D \quad y = 3x - 1$$
$$\bigcirc E \quad I \text{ need help}$$



https://njctl.org/video/?v=t7wbz5uZSJ0

73 What is the equation of the line that passes through the points (7,0) and (3,2)?

○A
$$y = -\frac{1}{2}x + \frac{7}{2}$$

○B $y = -\frac{1}{2}x + 7$
○C $y = -2x + 7$
○D $y = -2x + 8$
○E I need help



https://njctl.org/video/?v=lukLOJnB81w

74 What is the equation of the line that passes through the points (-3, -5) and (3, 2)?

$$\bigcirc A \qquad y = \frac{6}{7}x + \frac{17}{7}$$
$$\bigcirc B \qquad y = \frac{6}{7}x - \frac{4}{7}$$
$$\bigcirc C \qquad y = \frac{7}{6}x - 8.5$$
$$y = \frac{7}{6}x - 1.5$$
$$\bigcirc D$$



I need help

https://njctl.org/video/?v=kd2ahb7m_NU



Students use a linear equation, slope, and *x* and *y* intercepts to aim a marble launch tube so the marble will cross a specified set of Cartesian coordinates and hit the "target"!





https://njctl.org/video/?v=vBnQkZaThb4

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Throughout this unit, you have learned how to calculate the slope of a line and write the equation of a line in three different forms. What if you are given the equation of a line, and they ask you to find the slope? or an intercept?

Depending on what form the equation is in, the information might be easy to find. Sometimes, it might require some algebraic steps to manipulate the equation into the desired form.

Example:

What is the slope of the equation 8x - 10y = 40?

This equation is in standard form, which can be used to find the intercepts. It doesn't tell you the slope, though. So we have to manipulate it using what we know from algebra.

Which form(s) of a linear equation can help us find the slope of this line?

click to reveal

Which form(s) of a linear equation would be the most appropriate for this situation? Why?

Example: (cont.)

What is the slope of the equation 8x - 10y = 40?

$$8x - 10y = 40$$

$$-10y = -8x + 40$$
 Subtract 8x from both sides.

$$y = \frac{4}{5}x - 4$$
 Divide both sides (or all terms) by -10.

Therefore, the slope of the equation is $\frac{1}{click}$

Example:

Write the equation of the line with an *x*-intercept of 5 and a *y*-intercept of 10.

Since two points are given, we can use the slope formula. The two points are (5, 0) and (0, 10).

Since this problem does not specify a form for the equation, you can select any form that you desire. The equation of the line in point-slope form, using the *x*-intercept, is

Or you could also use the *y*-intercept to write the equation in pointslope form:

Or since you have the *y*-intercept and you calculated the slope, you could have written the equation in slope-intercept form:

Example: Write the equation $y - 7 = \frac{3}{4}(x+4)$ in standard form.

Then determine the *x*- and *y*-intercepts.

We need to get this equation into Ax + By = C, where $A \ge 0$. Therefore, we need to use our inverse operations.

$$y-7 = \frac{3}{4}(x+4)$$
 Multiply both sides of the equation by the LCD

$$4(y-7) = 3(x+4)$$
 Distributive Property

$$4y-28 = 3x+12$$
 Subtract $3x$ from both sides.

$$-3x+4y-28 = 12$$

$$-3x+4y=40$$
 Add 28 to both sides.

$$-3x+4y = 40$$
 Multiply all terms by -1, because $A \ge 0$.

$$3x-4y = -40$$

Math Practice

Example: Write the equation $y - 7 = \frac{3}{4}(x+4)$ in standard form.

Then determine the *x*- and *y*-intercepts.

Standard Form:

x-intercept: y = 0

 \searrow

y-intercept:
$$x = 0$$



75 What is the slope of the line formed by the equation below?

$$3x - 7y = 9$$

$$\bigcirc A$$

$$\bigcirc B \quad \frac{-\frac{3}{7}}{\frac{3}{7}}$$

$$\bigcirc C \quad \frac{-\frac{7}{3}}{\frac{7}{3}}$$

$$\bigcirc D$$

Answer



\bigcirc E I need help

https://njctl.org/video/?v=G7OsN-zCihY

76 What is the slope of the line formed by the equation below? 5x + 9y = 45JΑ $\frac{1}{5}$ $\frac{9}{5}$ Answer ΟB $\begin{array}{c} -\frac{5}{9} \\ \frac{5}{9} \end{array}$

⊇E I need help

https://njctl.org/video/?v=tZND-BBQtkg

77 What is the equation of a line that has an *x*-intercept of 2 and a *y*-intercept of 7?

$$\bigcirc A \quad y = -\frac{7}{2}(x-2)$$
$$\bigcirc B \quad y = -\frac{7}{2}x+7$$
$$\bigcirc C \quad 7x+2y=14$$

All of the aboveE I need help



https://njctl.org/video/?v=GA1z7C09TFg

78 Which equation represents y + 6 = 2(x-1) in Standard Form?



 igodoldrightarrow E I need help



https://njctl.org/video/?v=sO5JJIEtDKY

79 Which equation represents $y = -\frac{3}{5}x + 9$ in Standard Form?

$$\bigcirc A \quad 3x - 5y = -45$$

$$\bigcirc B \quad 3x + 5y = 45$$

$$\bigcirc C \quad 5y = -3x + 9$$

$$\bigcirc D \quad y - 2 = -\frac{3}{5}(x - 5)$$

 \bigcirc E I need help



https://njctl.org/video/?v=3RN2Yz6M-Ss

80 What is the equation of a line that has an *x*-intercept of 5 and a *y*-intercept of -7?

$$\bigcirc A \quad y = \frac{7}{5}x + 5$$
$$\bigcirc B \quad y = \frac{7}{5}x - 7$$
$$\bigcirc C \quad 7x - 5y = 70$$

 $\bigcirc\,$ All of the above

\bigcirc E I need help



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Comparing Rates of Change

To **compare the rates of change** of two different types of functions, we find the rate of change of each and compare their absolute values.

For example, if a graph has a slope of -4 and an equation has a slope of 3, the slope of the graph is steeper because the absolute value of -4 is greater than the absolute value of 3, i.e. |-4| > |3|.

Since the graph has a steeper slope it also has a larger rate of change.



https://njctl.org/video/?v=wSHxZxzZ3Eg
Comparing Rates of Change





Slope =

Ň

Let's compare a verbal model and a table.

A Chris and Shari are going to have a bowling party. It costs \$10 to rent a lane and \$2 per pair of shoes.



Which has the greater rate of change?

A Chris and Shari are going to have a bowling party. It costs \$10 to rent a lane and \$2 per pair of shoes.

Let's model this with a function.

The initial cost is \$10 to rent a lane, a constant. The cost for shoes changes depending on the amount of people.

Let *x* be the number of people bowling and *y* represent the cost. This makes the cost of the shoes 2x.

So the cost equation is y = 10 + 2x.

Its rate of change =



В	x	2	4	6	8	10	12	
	У	7	13	19	25	31	37	

We can use the slope formula to find the rate of change.



14

41

Comparing rates from a table and a verbal model.

A Chris and Shari are going to have a bowling party. It costs \$10 to rent a lane and \$2 per pair of shoes.

B	x	2	4	6	8	10	12	14
	У	7	13	19	25	31	37	41

Which has the greater rate of change?

The rate of change of A = 2 and the rate of change of B = 3. 2 < 3

Therefore, B has the greater rate of change.

81 Which has the greater rate of change?

$$\bigcirc A \quad y = \frac{1}{3}x + 5$$

 \bigcirc B The school store is selling book covers 2 for \$1.

 \bigcirc C I need help



https://njctl.org/video/?v=04-i5g_mWsQ

82 Which has the greater rate of change?

$$\bigcirc A \ y = x - 4$$

ОB	x	-9	-6	-3	0	3	6	9
	У	-4	-3	-2	-1	0	1	2

Answer

○C I need help



https://njctl.org/video/?v=x3fCGpaZ7Dk

83 Which has the greatest rate of change?

- $\bigcirc A \{(1, 3), (2, 4), (3, 5), (4, 6), (5, 7)\}$
- ○B Ryan and Andrew jump down the stairs 3 steps at a time.

$$\bigcirc C \quad y = \frac{1}{8}x - 2$$



 \bigcirc E I need help



- 84 Which has the greatest rate of change?
 - \bigcirc A cable company charges \$12 for every 2 premium channels.
 - $\bigcirc B \quad y = 5x + 6$
 - $\bigcirc C \{(9, 3), (6, 2), (3, 1), (0, 0), (-3, -1)\}$



OE I need help

Function Notation

- Sometimes, you will see an equation in the form f(x) = mx + binstead of y = mx + b. This can occur because every linear equation is a function.
- A function is a relationship that exists when every x value has exactly one y value. When this happens, nothing changes mathematically. Yet, instead of writing y mathematicians use f(x), read "f of x."

For example:

* $y \Leftrightarrow f(x)$ given that y is a function.

y=5x+7 becomes f(x)=5x+7

f(x) = 5x+7 is still a line with a slope of 5 and a *y*-intercept of (0,7).



Since we haven't yet covered the material for functions, it would be easiest for you, at this point, to switch the f(x) to y and solve the equation from there.

https://njctl.org/video/?v=CIEKi8fSF1c

Function Notation

The letter f is often used to name a function, but other letters, such as g and h, could also be used.

For example:
$$f(x) = 5x + 7$$
$$g(x) = 8x - 3$$
$$h(x) = 9x + 1$$

f, g, and h are all examples of linear functions.

Since we haven't yet covered the material for functions, it would be easiest for you, at this point, to substitute y for f(x), g(x), h(x), etc. and solve the equation from there.

Solving Linear Equations

Example: The graph shown to the right represents the function

$$f(x) = -\frac{7}{3}x + 14$$

For what value of $x \operatorname{does} f(x) = 0$?

If we start with the advice that we started with, substituting y in for f(x), we get the equation

$$y = -\frac{7}{3}x + 14$$



Solving Linear Equations

Example: (cont.)The graph shown to the right represents the function

$$f(x) = -\frac{7}{3}x + 14$$

For what value of $x \operatorname{does} f(x) = 0$?

$$f(x) = -\frac{7}{3}x + 14$$

If f(x)=0, that means that y=0. This occurs when the graph crosses the *x*-axis, giving us our *x*-intercept. Looking at the graph, we see that our *x*-intercept is (6, 0), so the value of *x* is 6.



85 The graph shown below represents the function g(x) = 2x - 8. For what value of x does g(x) = 0? $\bigcirc A - 8$ t $\bigcirc B 8$ $\bigcirc C 4$ Answer ○D -4 \bigcirc E I need help x θ 10 -10

https://njctl.org/video/?v=cREuOVg97gM

86 The graph shown below represents the function

$$h(x) = -\frac{1}{3}x + 2$$

For what value of x does h(x)=0?

 $\bigcirc A 6$

○B -6

OC 2

○D -2

○E I need help







87 The graph shown below represents the function

$$j(x) = -\frac{3}{5}x - 3$$

For what value of x does j(x) = 0? $\bigcirc A 3$ $\bigcirc B -3$ $\bigcirc C 5$ $\bigcirc D -5$ \bigcirc E I need help



https://njctl.org/video/?v=cB0ofUGXyMU

Scatter Plots and the Line of Best Fit



https://njctl.org/video/?v=Hh6KbMyuBcY

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A **scatter plot** is a graph that shows a set of data that has two variables.

Time Studying	Test Score
45	89
30	78
50	90
60	92
40	85
48	87
55	95
35	82

Test Score vs. Time Spent Studying (55, 95)95 (60, 92)90 <u>(50, 90)</u> (45, 88)**Test Score (4<u>8, 87</u>) (40, 85)** 85-(35, 82) 80 **(30, 78**) X 30 50 40 60

Time spent studying

There are three types of linear association that are possible for scatter plots. What are they?



Teacher Note

What type of linear association does the graph have to the right?

What connection do you see between linear association and the slope of a line?



Ň-

Math Practice

88 What type of scatter plot is shown in the graph below?

Ice Cream Sales vs. Temperature

non-linear JА 500 linear with positive $\supset \mathbf{B}$ association Ð linear with negative $\frac{3}{5}$ 400 association $\bigcirc C$ Answer Cream linear without) D association <u>8</u>200, ○ E I need help X 80 7î 60 Temperature (^oF)

/njctl.org/video/?v=C9tEINVsHNo

89 What kind of association is shown in the graph?

- ⊖A non-linear
- B linear with positive association
- C linear with negative association
- D linear without association
- OE I need help

https://njctl.org/video/?v=9 N0XEganLo



of clothing layers worr 3 Number $\mathbf{20}$ 40 60 80 Temperature(^oF)

Number of Clothing Layers Worn vs. Temperature

Answer

X

90 What kind of association is shown in the graph?

- ○A non-linear
- B linear with positive association
- C linear with negative association
- D linear without association
- OE I need help



Answer

Shoe Size vs. Height



- What association is shown in this graph? 91
- non-linear) A
- linear with positive ЭВ association
- linear with negative 200-C association
- linear without Π association
- I need help) F





Answer

https://njctl.org/video/?v=m92PqXlynlo

Height (in.)

92 Which of the following scenarios would produce a linear scatter plot with a *negative* association?

- \bigcirc A Miles driven and money spent on gas
- B Number of pets and how many shoes you own
- $^{\bigcirc}$ C Work experience and income
- $^{\bigcirc}$ D Time spent studying and number of bad grades
- OE I need help



https://njctl.org/video/?v=AIULWzldUto

93 Which of the following would have *no* association if plotted on a scatter plot?

- \bigcirc A Number of toys and calories consumed in a day
- \bigcirc B Number of books read and reading scores
- $^{\bigcirc}$ C Length of hair and amount of shampoo used
- $^{\bigcirc}\,\mathrm{D}\,$ Person's weight and calories consumed in a day

OE I need help



https://njctl.org/video/?v=tG4HyWhZnRg

Draw a Line

Notice that the points form a linear like pattern. To draw a **line of best fit**, use two points so that the line is as close as possible to the data points.

Our line is drawn so that it fits as close as possible to the data points. The number of points above and below the line should be about the same. There are 3 points above our line and 3 points below our line. This line was drawn through (35, 82) and (50, 90).





Using the line of best fit shown in the graph to:

- Predict the test score of someone who spends 32 minutes studying.
- Predict the test score of someone who spends 58 minutes studying.



Answer

Prediction Equation

Use the two points that formed the line to write an equation for the line.



Prediction Equation

Use the two points that formed the line to write an equation for the line.

Find the slope (m).

$$m = \frac{90 - 82}{50 - 35}$$
$$m = \frac{8}{15}$$



Prediction Equation

Use the two points that formed the line to write an equation for the line.

Find the equation of the line.

$$y - 90 = \frac{8}{15}(x - 50)$$
$$y - 90 = \frac{8}{15}x - \frac{80}{3}$$
$$y = \frac{8}{15}x + \frac{190}{3}$$

where *y* is the score for *x* minutes of studying

The equation formed is called a **Prediction Equation**.



Extrapolation

Prediction Equations can be used to predict other related values.

$$y = \frac{8}{15}x + \frac{190}{3}$$

If a person studies 15 *minutes*, what would be the predicted score?

$$S = \frac{8}{15} (15) + \frac{190}{3} \approx 71.3$$

This is an **extrapolation**, because the time was outside the range of the original times.

Interpolation

If a person studies 42 minutes, what would be the predicted score?

$$S = \frac{8}{15} (42) + \frac{190}{3} \approx 85.7$$

This is an **interpolation**, because the time was inside the range of the original times.

What is Wrong?

Interpolations are more accurate because they are within the set.

The farther points are away from the data set the less reliable the prediction.

Using the same prediction equation, consider:

If a person studies 120 minutes, what will be there score?

$$S = \frac{8}{15} (120) + \frac{190}{3} \approx 127.3$$

What is wrong with this prediction?

What is the Prediction?

If a student got an 80 on the test, what would be the predicted length of their study time?

$$80 = \frac{8}{15}x + \frac{190}{3}$$
$$16.7 = \frac{9}{15}x$$
$$31.25 = x$$

The student studied about 31 minutes.

Shoe Size vs. Height

- Draw the line of best fit for our data.
- Determine the equation for the line of best fit.
- Predict the height of a person who wears a size 8 shoe.
- Predict the shoe size of
 a person who is 50
 inches tall.


Shoe Size vs. Height

Draw the line of best fit for our data. *Click on the graph to reveal the line of best fit.*

Determine the equation for the line of best fit.

Find the slope.







Shoe Size vs. Height

Predict the height of a person who wears a size 8 shoe.

Predict the shoe size of a person who is 50 inches tall.



94 Consider the scatter graph to answer the following: Which two points would give the best line of fit?



https://njctl.org/video/?v=F_y5YT3KFNs

95 Consider the scatter graph to answer the following: Which two points would give the best line of fit?





96 Consider the scatter graph to answer the following.What is the slope of the line of best fit going through *A* and *D*?



https://njctl.org/video/?v=u4PbRDhlkBQ

97 Consider the scatter graph to answer the following. What is the *y*-intercept of the line of best fit going through A and D?

 $\bigcirc A 9$ ⊖B 10 OC 11)D 12 ○E I need help



Answer



https://njctl.org/video/?v=I3s-4a3eQzY

- ⁹⁸ Consider the scatter plot to answer the following. Using the line of best fit shown in the graph below, what would the prediction be if x = 7? Is this an interpolation or extrapolation?
 - OA 5, interpolation
 - \bigcirc B 5, extrapolation
 - \bigcirc C 6, interpolation
 - \bigcirc D 6, extrapolation
 - E I need help



Answer

https://njctl.org/video/?v=jFAMZFbea9M

- 99 Consider the scatter graph to answer the following. Using the line of best fit shown in the graph below, what would the prediction be if x = 14? Is this an interpolation or extrapolation?
 - $\bigcirc A$ -4, interpolation
 - \bigcirc B -4, extrapolation
 - \bigcirc C -2, interpolation
 - \bigcirc D -2, extrapolation
 - OE I need help



Answer



https://njctl.org/video/?v=d469D-tO39A

- 100 Consider the scatter graph to answer the following: Using the line of best fit shown in the graph below, what would the prediction be if y = 11? Is this an interpolation or extrapolation?
- OA 1, interpolation
- \bigcirc B 1, extrapolation
- OC 2, interpolation
- $\bigcirc D$ 2, extrapolation
- OE I need help





Answer

https://njctl.org/video/?v=0Tggsam1p6s

101 In the previous questions, we began by using the table at the right. Which of the predicted values (7,5) or (14, -2) will be more accurate and why?

\bigcirc A (7,5); it is an interpolation

- \bigcirc B (7,5); there already is a 5 and a 7 in the table
- \bigcirc C (14, -2) it is an extrapolation
- \bigcirc D (14, -2); the line is going down and will become negative

x	у
3	9
5	7
6	5
8	4
9	3
10	1



OE I need help

https://njctl.org/video/?v=i8ogkkiqnJc



Students measure the height of a burning candle, graph the data and find the line of best fit.

PARCC Sample Questions

The remaining slides in this presentation contain questions from the PARCC Sample Test.

After finishing this unit, you should be able to answer these questions.

Good Luck!

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102 Which points are on the graph of the equation -3x + 6y + 5 = -7? Select all that apply.

A (-3, 6) D (6, -3) B (-2, 0) E (8, 2) C (0, -2)

□A A, E □C C, E □B B, C □D B, D

E I need help

https://njctl.org/video/?v=GPVJmhc9QIQ

From PARCC Sample Test - Non-calculator - Response Format





https://njctl.org/video/?v=jqjfl9-8dgk

From PARCC Sample Test - Non-calculator

104 Graph the equation 6x-4y=12 on the *xy*-coordinate plane. Identify the *x*-intercept of the graph.

○ A (2, 0)
○ B (0, 2)
○ C (0, -3)
○ D (-3, 0)
○ E I need help



Answer



https://njctl.org/video/?v=U48huWWzYiY

From PARCC Sample Test - Non-calculator

105 The ordered pairs (20, -29.5), (21, -31) and

(22, -32.5) are points on the graph of a linear equation. Graph the line that shows all of the ordered pairs in the solution set of this linear equation.

- ○A Red
- OB Blue
- ○C Purple
- OD Black
- ○E I need help



https://njctl.org/video/?v=pFBFgahOLbA



Answer

From PARCC Sample Test - Calculator

Glossary and Standards

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Constant Rate of Change

A rate that describes how one quantity changes in relation to another. This rate never changes.





Direct Variation

A relationship between two variables in which one is a constant multiple of the other. When one variable changes the other changes in proportion to the first.





Extrapolation

A data point that is outside the range of data.



Back to

Grade

A unit engineers use to measure the steepness of a hill.



Horizontal Line

A line whose direction is left and right. All of the y-coordinates on the line are equal.



Interpolation

A data point that is inside the range of data.



Back to

Line of Best Fit

A line on a graph showing the general direction that a group of points seem to be heading. Trend line.



Negative Slope

When a line falls down from left to right.



Point-Slope Form

The point-slope equation for a line is $y - y_1 = m (x - x_1)$ where *m* is the slope and (x_1, y_1) is a point on the line.



Back to

Positive Slope

When a line rises from left to right.



Prediction Equation

An equation that is created using the line of best fit. A line that can predict outcomes using the given data.



Back to

Scatter Plot

A graph of plotted points that show the relationship between two sets of data.



Slope

How much a line rises or falls. Steepness of a line. The ratio of a line's rise over its run.



Back to

Slope-Intercept Form

One type of straight line equation that utilizes the slope and y-intercept to graph.



Standard Form

Standard form looks like Ax + By = C,

where A, B and C are integers and A > 0.



Undefined Slope

When a line does not run at all as one reads from bottom to top on the *y*-axis.



Vertical Line

A line whose direction is only up and down.

All of the *x*-coordinates on the line are equal.



x-Intercept

Where a line crosses the *x*-axis.



Back to

y-Intercept

Where a line crosses the *y*-axis.


Zero Slope

When a line does not rise at all as one reads it from left to right on the *x*-axis.



Back to

Throughout this unit, the Standards for Mathematical Practice are used.

- MP1: Making sense of problems & persevere in solving them.
- MP2: Reason abstractly & quantitatively.
- MP3: Construct viable arguments and critique the reasoning of others.
- MP4: Model with mathematics.
- MP5: Use appropriate tools strategically.
- MP6: Attend to precision.
- MP7: Look for & make use of structure.
- MP8: Look for & express regularity in repeated reasoning.

Additional questions are included on the slides using the "Math Practice" Pull-tabs (e.g. a blank one is shown to the right on this slide) with a reference to the standards used.

If questions already exist on a slide, then the specific MPs that the questions address are listed in the Pull-tab.