

# Linear Systems – FE Electrical Live Training

## Week # 9 – Saturday Session



STUDY FOR FE

Focus of this homework assignment will be on the following topics of 'Linear Systems'.

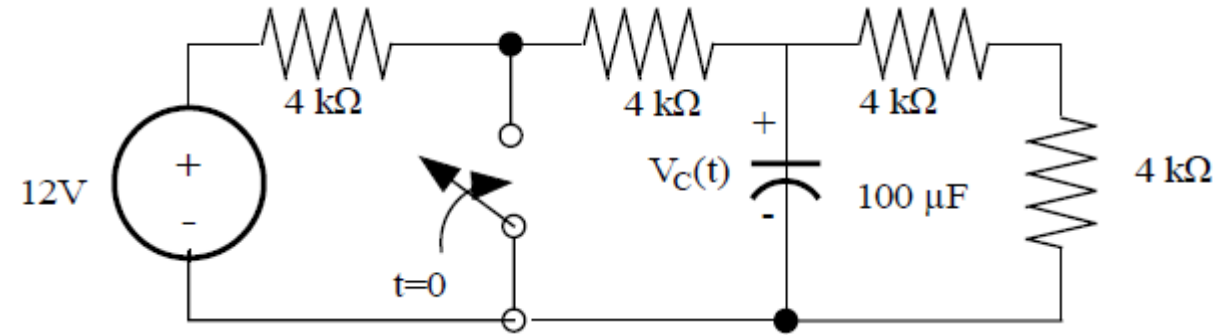
- ☐ Frequency/Transient Response
- ☐ Resonance
- ☐ Laplace Transform
- ☐ Transfer Functions

# Linear Systems



STUDY FOR FE

**HW Problem # 1** – Determine the value of  $V_C(t)$  for  $t > 0$  if the switch has been in open position for a long time before closing at  $t = 0$ .

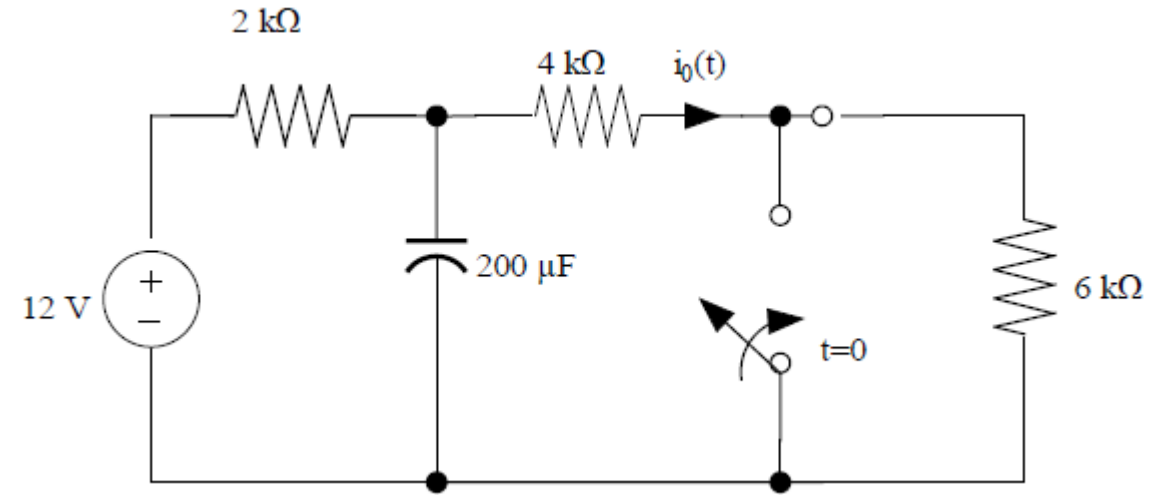


# Linear Systems



STUDY FOR FE

**HW Problem # 2** – Determine the value of  $i_o(t)$  for  $t > 0$  if the switch has been in open position for a long time before closing at  $t = 0$ .

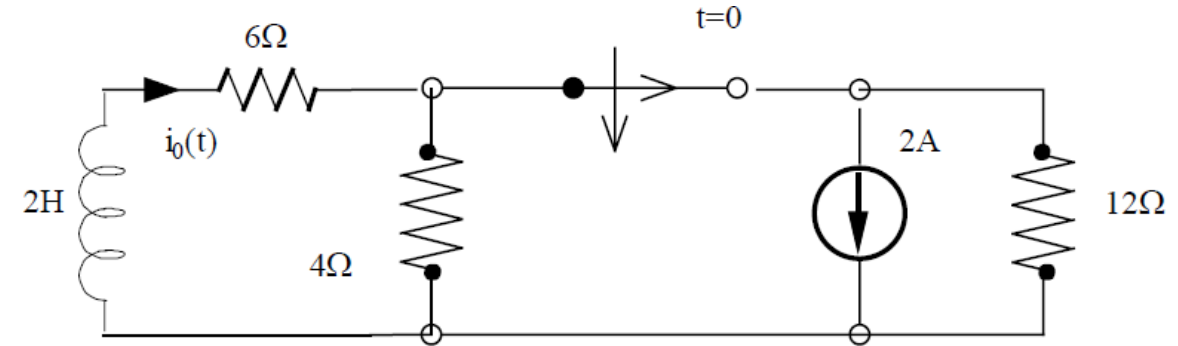


# Linear Systems



STUDY FOR FE

**HW Problem # 3** – Determine the value of  $i_o(t)$  for  $t > 0$  if the switch has been in closed position for a long time before opening at  $t = 0$ .

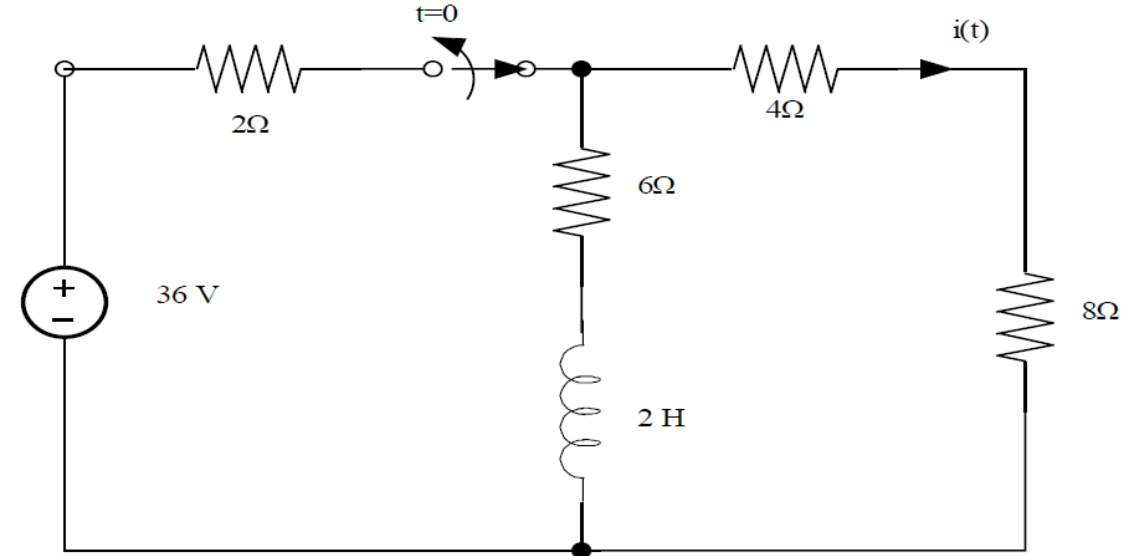


# Linear Systems



STUDY FOR FE

**HW Problem # 4** – Determine the value of  $i_o(t)$  for  $t > 0$  if the switch has been in closed position for a long time before opening at  $t = 0$ .



# Linear Systems



STUDY FOR FE

**HW Problem # 5** – Determine the Laplace Transform of following function.

$$f(t) = \sin^2(2t)$$

# Linear Systems



STUDY FOR FE

**HW Problem # 6** – Determine the Laplace Transform of following function.

$$f(t) = \cos(\omega t + \theta)$$

# Linear Systems



STUDY FOR FE

**HW Problem # 7** – Determine the limit of  $f(t)$  as  $t \rightarrow \infty$  if  $F(s)$  is given below.

$$F(s) = \frac{4}{(s)(s+1)}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 8** – Determine the limit of  $f(t)$  as  $t \rightarrow 0$  if  $F(s)$  is given below.

$$F(s) = \frac{4(s + 1)}{s^2 + 4s + 7}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 9** – Determine the Laplace Transform of following function.

$$f(t) = te^{-a(t-1)}\delta(t-1)$$

# Linear Systems



STUDY FOR FE

**HW Problem # 10** – Determine the Inverse Laplace Transform of following function.

$$F(s) = \frac{s+10}{(s+4)(s+6)}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 11** – Determine the Inverse Laplace Transform of following function.

$$F(s) = \frac{24}{(s+2)(s+8)}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 12** – Determine the Inverse Laplace Transform of following function.

$$F(s) = \frac{1}{s^2(s + 1)}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 13** – Determine the Inverse Laplace Transform of following function.

$$F(s) = \frac{s^2 + 7s + 12}{(s + 2)(s + 4)(s + 6)}$$

# Linear Systems



STUDY FOR FE

**HW Problem # 14** – Determine the Inverse Laplace Transform of following function.

$$F(s) = \frac{10(s+2)}{(s^2 + 4s + 5)}$$

# Linear Systems



STUDY FOR FE

Consider the following transfer function for the next 3 problems.

$$H(s) = \frac{640(s + 1)(0.01s + 1)}{s^2(s + 10)}$$

**HW Problem # 15** – Express the transfer function  $H(s)$  in standard form.

# Linear Systems



STUDY FOR FE

$$H(s) = \frac{640(s + 1)(0.01s + 1)}{s^2(s + 10)}$$

**HW Problem # 16** – Determine the poles and zeros of given transfer function  $H(s)$ .

# Linear Systems



STUDY FOR FE

$$H(s) = \frac{640(s + 1)(0.01s + 1)}{s^2(s + 10)}$$

**HW Problem # 17** – Express the gain of given transfer function  $H(s)$  in dB.

# FE Electrical Live Training

## Linear Systems – Answer Key



STUDY FOR FE

1)  $6e^{\left(-\frac{15t}{4}\right)}V$

2)  $2 + 0.5e^{(-3.75t)}mA$

3)  $\frac{2}{3}e^{(-5t)}A$

4)  $-4e^{(-9t)}A$

5)  $\frac{1}{2s} - \frac{1}{2} \left( \frac{s}{s^2+16} \right)$

6)  $\cos \theta \left[ \frac{s}{[s^2+(\omega t)^2]} \right] - \sin \theta \left[ \frac{\omega t}{[s^2+(\omega t)^2]} \right]$

7) 4

8) 4

9)  $e^{-s}$

10)  $3e^{-4t} - 2e^{-6t}$

11)  $6e^{-2t} - 4e^{-8t}$

12)  $-1 + t + e^{-t}$

13)  $\frac{1}{4}e^{-2t} + \frac{3}{4}e^{-6t}$

14)  $10e^{-2t} \cos(t)$

15)  $\frac{64(s+1)(0.01s+1)}{s^2\left(\frac{s}{10}+1\right)}$

16) Poles: 2<sup>nd</sup> order @ DC 0Hz, and 1<sup>st</sup> order pole at  $s = -10$  rad/s

Zeroes: 1<sup>st</sup> order zeroes at  $s = -1$  rad/s and  $-100$  rad/s

17)  $36.1dB$