

Check up 7

Date _____

For each problem, find all points of relative minima and maxima using the first derivative test.

$$1) \ y = \frac{3}{16}(x-1)^{\frac{4}{3}} + \frac{3}{2}(x-1)^{\frac{1}{3}} + 1$$

For each problem, find all points of relative minima and maxima using the second derivative test.

$$2) \ f(x) = -\frac{x^2}{3x+6}$$

For each problem, find all points of absolute minima and maxima on the given interval.

$$3) \ y = \frac{1}{6}(x+1)^{\frac{7}{3}} - \frac{14}{3}(x+1)^{\frac{1}{3}} - 2; \ [-3, 0]$$

For each problem, find the open intervals where the function is concave up and concave down.

$$4) \ y = \left(\frac{x-1}{x+3} \right)^2$$

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For each problem, find all points of relative minima and maxima using the first derivative test.

$$1) y = \frac{3}{16}(x-1)^{\frac{4}{3}} + \frac{3}{2}(x-1)^{\frac{1}{3}} + 1$$

Relative minimum: $\left(-1, \frac{8 - 9\sqrt[3]{2}}{8}\right)$

No relative maxima.

For each problem, find all points of relative minima and maxima using the second derivative test.

$$2) f(x) = -\frac{x^2}{3x+6}$$

Relative minimum: $\left(-4, \frac{8}{3}\right)$

Relative maximum: $(0, 0)$

For each problem, find all points of absolute minima and maxima on the given interval.

$$3) y = \frac{1}{6}(x+1)^{\frac{7}{3}} - \frac{14}{3}(x+1)^{\frac{1}{3}} - 2; [-3, 0]$$

Absolute minimum: $\left(0, -\frac{13}{2}\right)$

Absolute maximum: $\left(-3, 4\sqrt[3]{2} - 2\right)$

For each problem, find the open intervals where the function is concave up and concave down.

$$4) y = \left(\frac{x-1}{x+3}\right)^2$$

Concave up: $(-\infty, -3), (-3, 3)$ Concave down: $(3, \infty)$