Topic: One-sided limits

Question: Find the left-hand limit.

$$\lim_{x \to 2^-} \frac{|x-2|}{|x-2|}$$

Answer choices:

- A -1
- **B** 1
- C -2
- D 2

Solution: A

As we approach x = 2 from the left, the function is a constant -1 (the numerator is always positive and the denominator is the same as the numerator except it will always be negative because we are subtracting 2 from values less than 2). Therefore, the limit from the left is -1.

Topic: One-sided limits

Question: Find the right-hand limit.

$$\lim_{x \to 2^+} \frac{|x-2|}{|x-2|}$$

Answer choices:

- A -1
- **B** 1
- C -2
- D 2

Solution: B

As we approach x = 2 from the right, the function is a constant 1 (the numerator is always positive and the denominator is the same as the numerator and is also always positive because we are subtracting 2 from values greater than 2). Therefore, the limit from the right is 1.