

# ACT MATH FORMULAS TO KNOW

## LINES

For a line that goes through two points  $(x_1, y_1)$  and  $(x_2, y_2)$

$$\text{Slope of the line that connects the points, } m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{rise}}{\text{run}}$$

$$\text{Distance Formula} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{Midpoint Formula} = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Slope-Intercept Form:  $y = mx + b$

slope =  $m$ , y-int =  $(0, b)$

Standard Form =  $Ax + By = C$

slope =  $-\frac{A}{B}$ , y-int =  $\left(0, \frac{C}{B}\right)$

Horizontal line:  $y = \#$ ,  $m = 0$

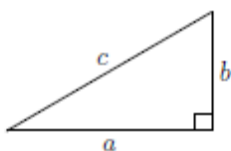
Vertical Line =  $x = \#$ ,  $m = \text{undefined}$

Parallel lines = same slope

Perpendicular lines = slopes are opposite reciprocals (i.e.  $1/3, -3$ )

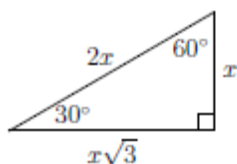
## TRIANGLES

Right triangles:

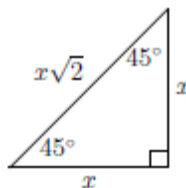


**Pythagorean Theorem**

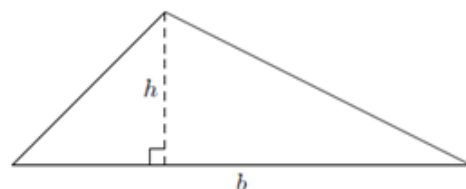
$$a^2 + b^2 = c^2$$



Special Right Triangles



All triangles:



$$\text{Area} = \frac{1}{2} \cdot b \cdot h$$

30-60-90 Right Triangle:

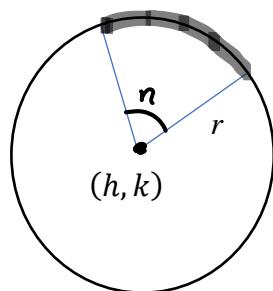
$$\text{Longer Leg} = \text{Shorter leg} \cdot \sqrt{3} \quad \text{---} \quad \text{Hypotenuse} = \text{Shorter leg} \cdot 2 \quad \text{---} \quad \text{Shorter Leg} = \frac{\text{Longer Leg}}{\sqrt{3}} \quad \text{or} \quad \frac{\text{Hypotenuse}}{2}$$

45-45-90 Right Triangle:

$$\text{Hypotenuse} = \text{Leg} \cdot \sqrt{2} \quad \text{or} \quad \text{Leg} = \frac{\text{Hypotenuse}}{\sqrt{2}}$$

## CIRCLES

$$(x - h)^2 + (y - k)^2 = r^2 \quad \text{center} = (h, k) \quad \text{radius} = r$$



$$\text{Circumference} = 2\pi r$$

$$\text{Area} = \pi r^2$$

$$\text{Length of arc} = \left( \frac{n}{360} \right) * 2\pi r$$

$$\text{Area of sector} = \left( \frac{n}{360} \right) * \pi r^2$$

## IMAGINARY NUMBERS:

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

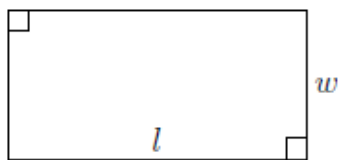
## QUADRATIC FORMULA:

$$\text{For } ax^2 + bx + c = 0, \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

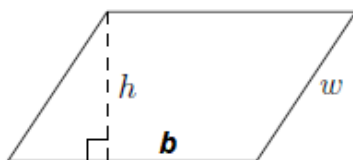
# ACT MATH FORMULAS TO KNOW

## GEOMETRIC SHAPES & FIGURES

Rectangles and Parallelograms:

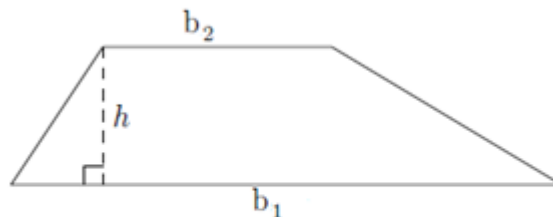


Rectangle  
(Square if  $l = w$ )  
Area =  $lw$   
Perimeter =  $2l + 2w$



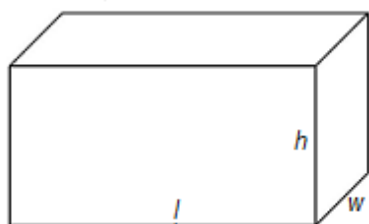
Parallelogram  
(Rhombus if  $b = w$ )  
Area =  $bh$

Trapezoids



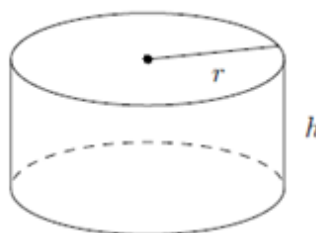
Area of trapezoid =  $\left(\frac{b_1 + b_2}{2}\right) \cdot h$

Solids



Rectangular Solid

Volume =  $lwh$   
Surface Area =  $2lw + 2hw + 2lh$



Right Cylinder

Volume =  $\pi r^2 h$   
Surface Area =  $2\pi r^2 h + 2\pi r^2$

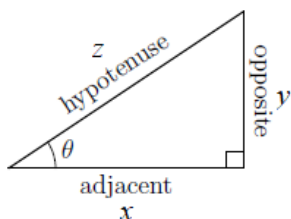
# of Diagonals in  
Regular Polygon  
with n sides:

$$\frac{(n-3)n}{2}$$

or

$$nC_r - n$$

## TRIGONOMETRY



$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{y}{z}$$

“SOH”

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{x}{z}$$

“CAH”

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{y}{x}$$

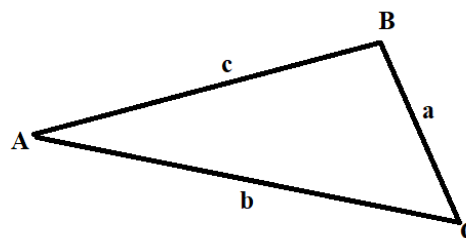
“TOA”

Law of Sines:  $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Law of Cosines:  $b^2 = a^2 + c^2 - 2ac \cos B$

$$c^2 = a^2 + b^2 - 2ab \cos C$$



**MEAN:**  $\text{AVG (MEAN)} = \frac{\text{SUM}}{\text{\# OF ITEMS}}$  or  $\text{AVG} * \text{\# OF ITEMS} = \text{SUM}$

**EXPECTED VALUE** =  $P(x_1)*x_1 + P(x_2)*x_2 + P(x_3)*x_3 + P(x_4)*x_4 + \dots$