Paper 1: Pure Mathematics Mark Scheme

| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 1 <br> Way 1 | Uses $y=m x+c$ with both $(3,1)$ and $(4,-2)$ and attempt to find $m$ or $c$ | M1 | 1.1b |
|  | $m=-3$ | A1 | 1.1b |
|  | $c=10$ so $y=-3 x+10$ o.e. | A1 | 1.1b |
|  |  | (3) |  |
| Or <br> Way 2 | Uses $\frac{y-y_{1}}{x-x_{1}}=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ with both $(3,1)$ and $(4,-2)$ | M1 | 1.1b |
|  | Gradient simplified to -3 (may be implied) | A1 | 1.1b |
|  | $y=-3 x+10$ o.e. | A1 | 1.1b |
|  |  | (3) |  |
| $\begin{gathered} \text { Or } \\ \text { Way } 3 \\ \hline \end{gathered}$ | Uses $a x+b y+k=0$ and substitutes both $x=3$ when $y=1$ and $x=$ 4 when $y=-2$ with attempt to solve to find $a, b$ or $k$ in terms of one of them | M1 | 1.1b |
|  | Obtains $a=3 b, k=-10 b$ or $3 k=-10 a$ | A1 | 1.1b |
|  | Obtains $a=3, b=1, k=-10$ <br> Or writes $3 x+y-10=0$ o.e. | A1 | 1.1b |
|  |  | (3) |  |
| (7 marks) |  |  |  |
| Notes: |  |  |  |
| M1: Need correct use of the given coordinates <br> A1: Need fractions simplified to -3 (in ways 1 and 2) <br> A1: Need constants combined accurately <br> N.B. Answer left in the form $(y-1)=-3(x-3)$ or $(y-(-2))=-3(x-4)$ is awarded M1A1A0 as answers should be simplified by constants being collected <br> Note that a correct answer implies all three marks in this question |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 2 | Attempt to differentiate | M1 | 1.1a |
|  | $\frac{\mathrm{d} y}{\mathrm{~d} x}=4 x-12$ | A1 | 1.1b |
|  | Substitutes $x=5 \Rightarrow \frac{\mathrm{~d} y}{\mathrm{~d} x}=\ldots$ | M1 | 1.1b |
|  | $\Rightarrow \frac{\mathrm{d} y}{\mathrm{~d} x}=8$ | A1ft | 1.1b |
| (4 marks) |  |  |  |
| Notes: |  |  |  |
| M1: Differentiation implied by one correct term <br> A1: Correct differentiation <br> M1: Attempts to substitute $x=5$ into their derived function <br> A1ft: Substitutes $x=5$ into their derived function correctly i.e. Correct calculation of their $f^{\prime}(5)$ so follow through slips in differentiation |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 3(a) | Attempts $\overrightarrow{A B}=\overrightarrow{O B}-\overrightarrow{O A}$ or similar | M1 | 1.1b |
|  | $\overrightarrow{A B}=5 \mathbf{i}+10 \mathbf{j}$ | A1 | 1.1b |
|  |  | (2) |  |
| (b) | Finds length using 'Pythagoras' $\|A B\|=\sqrt{(5)^{2}+(10)^{2}}$ | M1 | 1.1b |
|  | $\|A B\|=5 \sqrt{5}$ | A1ft | 1.1b |
|  |  | (2) |  |
| (4 marks) |  |  |  |
| Notes: |  |  |  |
| (a) <br> M1: Attempts subtraction but may omit brackets <br> A1: cao (allow column vector notation) |  |  |  |
| M1: Correct use of Pythagoras theorem or modulus formula using their answer to (a) <br> A1ft: $\|A B\|=5 \sqrt{5} \mathrm{ft}$ from their answer to (a) |  |  |  |
| Note that th | rrect answer implies M1A1 in each part of this question |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 4(a) | States or uses $\mathrm{f}(+3)=0$ | M1 | 1.1b |
|  | $4(3)^{3}-12(3)^{2}+2(3)-6=108-108+6-6=0$ and so $(x-3)$ is a factor | A1 | 1.1b |
|  |  | (2) |  |
| (b) | Begins division or factorisation so $x$ $4 x^{3}-12 x^{2}+2 x-6=(x-3)\left(4 x^{2}+\ldots\right)$ | M1 | 2.1 |
|  | $4 x^{3}-12 x^{2}+2 x-6=(x-3)\left(4 x^{2}+2\right)$ | A1 | 1.1b |
|  | Considers the roots of their quadratic function using completion of square or discriminant | M1 | 2.1 |
|  | $\left(4 x^{2}+2\right)=0$ has no real roots with a reason (e.g. negative number does not have a real square root, or $4 x^{2}+2>0$ for all $x$ <br> So $x=3$ is the only real root of $\mathrm{f}(x)=0$ * | A1* | 2.4 |
|  |  | (4) |  |
| (6 marks) |  |  |  |
| Notes: |  |  |  |
| (a) <br> M1: $\quad$ States or uses $f(+3)=0$ <br> A1: See correct work evaluating and achieving zero, together with correct conclusion |  |  |  |
| (b) <br> M1: Needs to have $(x-3)$ and first term of quadratic correct <br> A1: Must be correct - may further factorise to $2(x-3)\left(2 x^{2}+1\right)$ <br> M1: Considers their quadratic for no real roots by use of completion of the square or consideration of discriminant then <br> A1*: A correct explanation |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 5 | $\mathrm{f}(x)=2 x+3+12 x^{-2}$ | B1 | 1.1b |
|  | Attempts to integrate | M1 | 1.1a |
|  | $\int\left(+2 x+3+\frac{12}{x^{2}}\right) \mathrm{d} x=x^{2}+3 x-\frac{12}{x}$ | A1 | 1.1b |
|  | $\left((2 \sqrt{2})^{2}+3(2 \sqrt{2})-\frac{12(\sqrt{2})}{2 \times 2}\right)-(-8)$ | M1 | 1.1b |
|  | $=16+3 \sqrt{2}$ * | A1* | 1.1b |
| (5 marks) |  |  |  |
| Notes: |  |  |  |
| B1: Correct function with numerical powers <br> M1: Allow for raising power by one. $x^{n} \rightarrow x^{n+1}$ <br> A1: Correct three terms <br> M1: Substitutes limits and rationalises denominator <br> A1*: Completely correct, no errors seen |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 6 | Considers $\frac{3(x+h)^{2}-3 x^{2}}{h}$ | B1 | 2.1 |
|  | Expands $3(x+h)^{2}=3 x^{2}+6 x h+3 h^{2}$ | M1 | 1.1b |
|  | So gradient $=\frac{6 x h+3 h^{2}}{h}=6 x+3 h \quad$ or $\quad \frac{6 x \delta x+3(\delta x)^{2}}{\delta x}=6 x+3 \delta x$ | A1 | 1.1b |
|  | States as $h \rightarrow 0$, gradient $\rightarrow 6 x$ so in the limit derivative $=6 x *$ | A1* | 2.5 |
| (4 marks) |  |  |  |
| Notes: |  |  |  |
| B1: Gives correct fraction as in the scheme above or $\frac{3(x+\delta x)^{2}-3 x^{2}}{\delta x}$ <br> M1: Expands the bracket as above or $3(x+\delta x)^{2}=3 x^{2}+6 x \delta x+3(\delta x)^{2}$ <br> A1: Substitutes correctly into earlier fraction and simplifies <br> A1*: Uses Completes the proof, as above ( may use $\delta x \rightarrow 0$ ), considers the limit and states a conclusion with no errors |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 7(a) | $\left(2-\frac{x}{2}\right)^{7}=2^{7}+\binom{7}{1} 2^{6} \cdot\left(-\frac{x}{2}\right)+\binom{7}{2} 2^{5} \cdot\left(-\frac{x}{2}\right)^{2}+\ldots$ | M1 | 1.1b |
|  | $\left(2-\frac{x}{2}\right)^{7}=128+\ldots$ | B1 | 1.1b |
|  | $\left(2-\frac{x}{2}\right)^{7}=\ldots-224 x+\ldots$ | A1 | 1.1b |
|  | $\left(2-\frac{x}{2}\right)^{7}=\ldots+\ldots+168 x^{2}(+\ldots)$ | A1 | 1.1b |
|  |  | (4) |  |
| (b) | Solve $\left(2-\frac{x}{2}\right)=1.995$ so $x=0.01$ and state that 0.01 would be substituted for $x$ into the expansion | B1 | 2.4 |
|  |  | (1) |  |
| (5 marks) |  |  |  |
| Notes: |  |  |  |
| (a)  <br> M1: N <br>  Co <br> B1: Co <br> A1: Co <br> A1: Co | correct binomial coefficient with correct power of 2 and correct ficients may be given in any correct form; e.g. 1, 7, 21 or ${ }^{7} C_{0},{ }^{7} C$ ect answer, simplified as given in the scheme ct answer, simplified as given in the scheme ct answer, simplified as given in the scheme | of $x$. <br> or equiv |  |
| (b) <br> B1: Needs a full explanation i.e. to state $x=0.01$ and that this would be substituted and that it is a solution of $\left(2-\frac{x}{2}\right)=1.995$ |  |  |  |


| Question |  | eme | Marks | AOs |
| :---: | :---: | :---: | :---: | :---: |
| 8(a) | Way 1 <br> Finds third angle of triangle and uses or states $\frac{x}{\sin 60^{\circ}}=\frac{30}{\sin 50^{\circ} "}$ | Way 2 <br> Finds third angle of triangle and uses or states $\frac{y}{\sin 70^{\circ}}=\frac{30}{\sin " 50^{\circ} "}$ | M1 | 2.1 |
|  | So $x=\frac{30 \sin 60^{\circ}}{\sin 50^{\circ}} \quad(=33.9)$ | So $y=\frac{30 \sin 70^{\circ}}{\sin 50^{\circ}} \quad(=36.8)$ | A1 | 1.1b |
|  | Area $=\frac{1}{2} \times 30 \times x \times \sin 70^{\circ}$ | $\frac{1}{2} \times 30 \times y \times \sin 60$ | M1 | 3.1a |
|  | $=478 \mathrm{~m}^{2}$ |  | A1ft | 1.1b |
|  |  |  | (4) |  |
| (b) | Plausible reason e.g. Because the given to four significant figure Or e.g. The lawn may not be fla | angles and the side length are not | B1 | 3.2b |
|  |  |  | (1) |  |
| (5 marks) |  |  |  |  |
| Notes: |  |  |  |  |
| (a) <br> M1: Uses sine rule with their third angle to find one of the unknown side lengths <br> A1: Finds expression for, or value of either side length <br> M1: Completes method to find area of triangle <br> A1ft: Obtains a correct answer for their value of $x$ or their value of $y$ |  |  |  |  |
| (b) <br> B1: As information given in the question may not be accurate to 4 sf or the lawn may not be flat so modelling by a plane figure may not be accurate |  |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 9 | Uses $\sin ^{2} x=1-\cos ^{2} x \Rightarrow 12\left(1-\cos ^{2} x\right)+7 \cos x-13=0$ | M1 | 3.1a |
|  | $\Rightarrow 12 \cos ^{2} x-7 \cos x+1=0$ | A1 | 1.1b |
|  | Uses solution of quadratic to give $\cos x=$ | M1 | 1.1b |
|  | Uses inverse cosine on their values, giving two correct follow through values (see note) | M1 | 1.1b |
|  | $\Rightarrow x=430.5^{\circ}, 435.5^{\circ}$ | A1 | 1.1b |
| (5 marks) |  |  |  |
| Notes: |  |  |  |
| M1: Uses correct identity <br> A1: Correct three term quadratic <br> M1: Solves their three term quadratic to give values for $\cos x$. (The correct answers are $\cos x=\frac{1}{3}$ or $\frac{1}{4}$ but this is not necessary for this method mark) <br> M1: Uses inverse cosine on their values, giving two correct follow through values - may be outside the given domain <br> A1: Two correct answers in the given domain |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 10 | Realises that $k=0$ will give no real roots as equation becomes $3=0$ (proof by contradiction) | B1 | 3.1a |
|  | (For $k \neq 0$ ) quadratic has noreal roots provided $b^{2}<4 a c$ so $16 k^{2}<12 k$ | M1 | 2.4 |
|  | $4 k(4 k-3)<0$ with attempt at solution | M1 | 1.1b |
|  | So $0<k<\frac{3}{4}$, which together with $k=0$ gives $0 \leqslant k<\frac{3}{4} *$ | A1* | 2.1 |
| (4 marks) |  |  |  |
| Notes: |  |  |  |
| B1: Explains why $k=0$ gives no real roots <br> M1: Considers discriminant to give quadratic inequality - does not need the $k \neq 0$ for this mark <br> M1: Attempts solution of quadratic inequality <br> A1*: Draws conclusion, which is a printed answer, with no errors (dependent on all three previous marks) |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 11 (a) <br> Way 1 | Since $x$ and $y$ are positive, their square roots are real and so $(\sqrt{x}-\sqrt{y})^{2} \geq 0$ giving $\quad x-2 \sqrt{x} \sqrt{y}+y \geq 0$ | M1 | 2.1 |
|  | $\therefore 2 \sqrt{x y} \leq x+y$ provided $x$ and $y$ are positive and so $\sqrt{x y} \leq \frac{x+y}{2} *$ | A1* | 2.2a |
|  |  | (2) |  |
| Way 2 Longer method | Since $\quad(x-y)^{2} \geq 0$ for real values of $x$ and $y, x^{2}-2 x y+y^{2} \geq 0$ and so $4 x y \leq x^{2}+2 x y+y^{2} \quad$ i.e. $4 x y \leq(x+y)^{2}$ | M1 | 2.1 |
|  | $\therefore 2 \sqrt{x y} \leq x+y$ provided $x$ and $y$ are positive and so $\sqrt{x y} \leq \frac{x+y}{2} *$ | A1* | 2.2a |
|  |  | (2) |  |
| (b) | Let $x=-3$ and $y=-5$ then LHS $=\sqrt{15}$ and RHS $=-4$ so as $\sqrt{15}>-4$ result does not apply | B1 | 2.4 |
|  |  | (1) |  |
| (3 marks) |  |  |  |
| Notes: |  |  |  |
| (a) <br> M1: Need two stages of the three stage argument involving the three stages, squaring, square rooting terms and rearranging <br> A1*: Need all three stages making the correct deduction to achieve the printed result |  |  |  |
| (b) <br> B1: Chooses two negative values and substitutes, then states conclusion |  |  |  |




| Question | Scheme |  | Marks | AOs |
| :---: | :---: | :---: | :---: | :---: |
| 14(a) | $\log _{10} P=m t+c$ |  | M1 | 1.1b |
|  | $\log _{10} P=\frac{1}{200} t+5$ |  | A1 | 1.1b |
|  |  |  | (2) |  |
| (b) | Way 1: Way 2: <br> As $P=a b^{t}$ then As $\log _{10} P=\frac{t}{200}+5$ then <br> $\log _{10} P=t \log _{10} b+\log _{10} a$ $P=10^{\left(\frac{t}{200}+5\right)}=10^{5} 10^{\left(\frac{t}{200}\right)}$ |  | M1 | 2.1 |
|  | $\log _{10} b=\frac{1}{200}$ or $\log _{10} a=5$ | $a=10^{5}$ or $b=10^{\left(\frac{1}{200}\right)}$ | M1 | 1.1b |
|  | So $a=100000$ or $b=1.0116$ |  | A1 | 1.1b |
|  | Both $a=100000$ and $b=1.0116$ (awrt 1.01) |  | A1 | 1.1b |
|  |  |  | (4) |  |
| (c)(i) | The initial population |  | B1 | 3.4 |
| (c)(ii) | The proportional increase of population each year |  | B1 | 3.4 |
|  |  |  | (2) |  |
| (d)(i) | 300000 to nearest hundred thousand |  | B1 | 3.4 |
| (d)(ii) | Uses $200000=a b^{t}$ with their values of $a$ and $b$ or $\log _{10} 200000=\frac{1}{200} t+5$ and rearranges to give $t=$ |  | M1 | 3.4 |
|  | 60.2 years to 3sf |  | A1ft | 1.1b |
|  |  |  | (3) |  |
| (e) | Any two valid reasons- e.g. <br> - 100 years is a long time and population may be affected by wars and disease <br> - Inaccuracies in measuring gradient may result in widely different estimates <br> - Population growth may not be proportional to population size <br> - The model predicts unlimited growth |  | B2 | 3.5b |
|  |  |  | (2) |  |

## Question 14 continued

## Notes:

(a)

M1: Uses a linear equation to relate $\log P$ and $t$
A1: Correct use of gradient and intercept to give a correct line equation
(b)

M1: Way 1: Uses logs correctly to give log equation; Way 2: Uses powers correctly to "undo" log equation and expresses as product of two powers
M1: Way 1: Identifies $\log b$ or $\log a$ or both; Way 2: Identifies $a$ or $b$ as powers of 10
A1: $\quad$ Correct value for $a$ or $b$
A1: Correct values for both
(c)(i)

B1: Accept equivalent answers e.g. The population at $t=0$
(c)(ii)

B1: So accept rate at which the population is increasing each year or scale factor 1.01 or increase of $1 \%$ per year
(d)(i)

B1: cao
(d)(ii)

M1: As in the scheme
A1ft: On their values of $a$ and $b$ with correct $\log$ work
(e)

B2: As given in the scheme - any two valid reasons

| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 15 | Finds $\frac{\mathrm{d} y}{\mathrm{~d} x}=8 x-6$ | M1 | 3.1a |
|  | Gradient of curve at $P$ is -2 | M1 | 1.1b |
|  | Normal gradient is $-\frac{1}{m}=\frac{1}{2}$ | M1 | 1.1b |
|  | So equation of normal is $(y-2)=\frac{1}{2}\left(x-\frac{1}{2}\right)$ or $4 y=2 x+7$ | A1 | 1.1b |
|  | Eliminates $y$ between $y=\frac{1}{2} x+\ln (2 x)$ and their normal equation to give an equation in $x$ | M1 | 3.1a |
|  | Solves their $\ln 2 x=\frac{7}{4}$ so $x=\frac{1}{2} \mathrm{e}^{\frac{7}{4}}$ | M1 | 1.1b |
|  | Substitutes to give value for $y$ | M1 | 1.1b |
|  | Point $Q$ is $\left(\frac{1}{2} \mathrm{e}^{\frac{7}{4}}, \frac{1}{4} \mathrm{e}^{\frac{7}{4}}+\frac{7}{4}\right)$ | A1 | 1.1b |
| (8 marks) |  |  |  |
| Notes: |  |  |  |
| M1: Differentiates correctly |  |  |  |
| M1: Substitutes $x=\frac{1}{2}$ to find gradient (may make a slip) |  |  |  |
| M1: Uses negative reciprocal gradient |  |  |  |
| A1: Correct equation for normal |  |  |  |
| M1: Attempts to eliminate $y$ to find an equation in $x$ |  |  |  |
| M1: Attempts to solve their equation using exp |  |  |  |
| M1: Uses their $x$ value to find $y$ |  |  |  |
| A1: Any correct exact form |  |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 16(a) | Sets $2 x y+\frac{\pi x^{2}}{2}=250$ | B1 | 2.1 |
|  | Obtain $y=\frac{250-\frac{\pi x^{2}}{2}}{2 x}$ and substitute into $P$ | M1 | 1.1b |
|  | Use $P=2 x+2 y+\pi x$ with their $y$ substituted | M1 | 2.1 |
|  | $P=2 x+\frac{250}{x}-\frac{\pi x^{2}}{2 x}+\pi x=2 x+\frac{250}{x}+\frac{\pi x}{2} *$ | A1* | 1.1b |
|  |  | (4) |  |
| (b) | $x>0$ and $y>0($ distance $) \Rightarrow \frac{250-\frac{\pi x^{2}}{2}}{2 x}>0$ or $250-\frac{\pi x^{2}}{2}>0$ o.e. | M1 | 2.4 |
|  | As $x$ and $y$ are distances they are positive so $0<x<\sqrt{\frac{500}{\pi}}$ * | A1* | 3.2a |
|  |  | (2) |  |
| (c) | Differentiates $P$ with negative index correct in $\frac{\mathrm{d} P}{\mathrm{~d} x} ; x^{-1} \rightarrow x^{-2}$ | M1 | 3.4 |
|  | $\frac{\mathrm{d} P}{\mathrm{~d} x}=2-\frac{250}{x^{2}}+\frac{\pi}{2}$ | A1 | 1.1b |
|  | Sets $\frac{\mathrm{d} P}{\mathrm{~d} x}=0$ and proceeds to $x=$ | M1 | 1.1b |
|  | Substitutes their $x$ into $P=2 x+\frac{250}{x}+\frac{\pi x}{2}$ to give perimeter $=59.8 \mathrm{M}$ | A1 | 1.1b |
|  |  | (4) |  |
| (10 marks) |  |  |  |

## Question 16 continued

## Notes:

(a)

B1: Correct area equation
M1: Rearranges their area equation to make $y$ the subject of the formula and attempt to use with an expression for $P$
M1: Use correct equation for perimeter with their $y$ substituted
A1*: Completely correct solution to obtain and state printed answer

## (b)

M1: States $x>0$ and $y>0$ and uses their expression from (a) to form inequality
A1*: Explains that $x$ and $y$ are positive because they are distances, and uses correct expression for $y$ to give the printed answer correctly

## (c)

M1: $\quad$ Attempt to differentiate $P$ (deals with negative power of $x$ correctly)
A1: Correct differentiation
M1: Sets derived function equal to zero and obtains $x=$
A1: The value of $x$ may not be seen (it is 8.37 to 3 sf or $\sqrt{\left(\frac{500}{4+\pi}\right)}$ )
Need to see awrt 59.8 M with units included for the perimeter

| Question | Scheme |  | Marks | AOs |
| :---: | :---: | :---: | :---: | :---: |
| 17 (a) | Way 1: <br> Finds circle equation $\begin{aligned} & (x \pm 2)^{2}+(y \mp 6)^{2}= \\ & \quad(10 \pm(-2))^{2}+(11 \mp 6)^{2} \end{aligned}$ | Way 2: <br> Finds distance between $(-2,6)$ and $(10,11)$ | M1 | 3.1a |
|  | Checks whether $(10,1)$ satisfies their circle equation | Finds distance between $(-2,6)$ and ( 10,1 ) | M1 | 1.1b |
|  | Obtains $(x+2)^{2}+(y-6)^{2}=13^{2}$ <br> and checks that $(10+2)^{2}+(1-6)^{2}=13^{2} \text { so }$ <br> states that $(10,1)$ lies on $C^{*}$ | Concludes that as distance is the same $(10,1)$ lies on the circle $C$ * | A1* | 2.1 |
|  |  |  | (3) |  |
| (b) | Finds radius gradient $\frac{11-6}{10-(-2)}$ or $\frac{1-6}{10-(-2)}$ |  | M1 | 3.1a |
|  | Finds gradient perpendicular to their radius using $-\frac{1}{m}$ |  | M1 | 1.1b |
|  | Finds (equation and ) $y$ intercept of tangent (see note below) |  | M1 | 1.1b |
|  | Obtains a correct value for $y$ intercept of their tangent i.e. 35 or -23 |  | A1 | 1.1b |
|  | Way 1: Deduces gradient of second tangent | Way 2: Deduces midpoint of $P Q$ from symmetry $(0,6)$ | M1 | 1.1b |
|  | Finds (equation and ) $y$ intercept of second tangent | Uses this to find other intercept | M1 | 1.1b |
|  | So obtains distance $P Q=35+23=58^{*}$ |  | A1* | 1.1b |
|  |  |  | (7) |  |
| (10 marks) |  |  |  |  |

## Question 17 continued

## Notes:

## (a) Way 1 and Way 2:

M1: Starts to use information in question to find equation of circle or radius of circle
M1: Completes method for checking that $(10,1)$ lies on circle
A1*: Completely correct explanation with no errors concluding with statement that circle passes through $(10,1)$
(b)

M1: Calculates $\frac{11-6}{10-(-2)}$ or $\frac{1-6}{10-(-2)}$ (m)
M1: Finds $-\frac{1}{m}$ (correct answer is $-\frac{12}{5}$ or $\frac{12}{5}$ ). This is referred to as $m^{\prime}$ in the next note M1: Attempts $y-11=$ their $\left(-\frac{12}{5}\right)(x-10)$ or $y-1=$ their $\left(\frac{12}{5}\right)(x-10)$ and puts $x=0$, or uses vectors to find intercept e.g. $\frac{y-11}{10}=-m^{\prime}$
A1: One correct intercept 35 or -23

## Way 1:

M1: Uses the negative of their previous tangent gradient or uses a correct $-\frac{12}{5}$ or $\frac{12}{5}$
M1: Attempts the second tangent equation and puts $x=0$ or uses vectors to find intercept e.g. $\frac{11-y}{10}=m^{\prime}$

## Way 2:

M1: Finds midpoint of $P Q$ from symmetry. (This is at $(0,6)$ )
M1: Uses this midpoint to find second intercept or to find difference between midpoint and first intercept. e.g. $35-6=29$ then $6-29=-23$ so second intercept is at $(-23,0)$

## Ways 1 and 2:

A1*: Obtain 58 correctly from a valid method

